Structural and optical properties of visible active photocatalytic WO₃ thin films prepared by reactive dc magnetron sputtering

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Nanostructured tungsten trioxide films were prepared by reactive dc magnetron sputtering at different working pressures $P_{\text{tot}} = 1\text{--}4$ Pa. The films were characterized by scanning electron microscopy, x-ray diffraction, Rutherford backscattering spectroscopy, Raman spectroscopy, and ultraviolet–visible spectrophotometry. The films were found to exhibit predominantly monoclinic structures and have similar band gap, $E_g \approx 2.8$ eV, with a pronounced Urbach tail extending down to 2.5 eV. At low P_{tot} , strained film structures formed, which were slightly reduced and showed polaron absorption in the near-infrared region. The photodegradation rate of stearic acid was found to correlate with the stoichiometry and polaron absorption. This is explained by a recombination mechanism, whereby photoexcited electron–hole pairs recombine with polaron states in the band gap. The quantum yield decreased by 50% for photon energies close to E_g due to photoexcitations to band gap states lying below the O₂ affinity level.

I. INTRODUCTION

Research on photocatalytic (PC) materials has attracted much interest as a sustainable method for pollutant degradation, water splitting, and synthetic fuel production.^{1–3} Nanocrystalline forms of wide band gap semiconducting oxides, and primarily, the anatase form of TiO₂, is by far the most studied of these materials.^{1,4} TiO₂ requires, however, ultraviolet (UV) light to excite the chemically active valence electrons to the conduction band, and solar-based conversion is thus limited to $\sim 4\%$ of the sunlight. Since it is desirable to exploit also visible light, a second generation of efficient UV–visible active PC materials is currently sought, where, e.g., low-dimensional doped TiO₂, WO₃, and mixed metal oxides, with and without additions of noble metals for enhanced electron–hole pair separation, have received considerable attention.^{5–8} WO₃ is a promising material for a wide range of environmental and energy applications. The electrochromic effect of WO₃ has been widely studied, and the material is much used in fabrication of smart windows.^{9–11} PC oxidation for indoor air purification and self-cleaning is today considered in several applications in the built environment.^{12,13} Recently, WO₃ has drawn attention because of its high efficiency in PC activity under daylight illumination^{14–17} and its ability to photodegrade a wide range of environmental pollutants.^{16,18,19} Nano-WO₃ is reported to have much higher PC activity compared to bulk WO₃ photoelectrodes.^{5,20} This is related to the different mechanism of charge separation and charge

transport in the nanocrystalline semiconductor films, which is a subject of continuing discussion.²¹

The PC activity depends on the electronic structure, which is related to crystal structure and surface morphology. WO₃ exists in several phases, which differ with respect to each other by the tilting and displacement of the atoms in the octahedral building blocks that comprise the WO₃ structure. The thermodynamically favored phase is reported to change with temperature (at standard pressure) for crystalline bulk WO₃ as follows: monoclinic *Pc* (ϵ -WO₃) up to 230 K, triclinic *P1* (δ -WO₃) 230–300 K, monoclinic *P2₁/n* (γ -WO₃) 300–623 K, orthorhombic *Pnma* (β -WO₃) 623–1020 K, tetragonal *P4/ncc* (α -WO₃) 1020–1171 K, and, finally, tetragonal *P4/nmm* (α -WO₃) to the melting point at 1700 K.^{22–26} The stability of each of these phases is modified by preparation procedures. For nanocrystalline thin films, the detailed growth conditions are critical, including type of substrate, temperature, and pressure. Apart from high surface area, which is beneficial in many environmental applications, nano-WO₃ exhibits structures and morphologies with unique properties that do not exist in bulk. The small size of grains in a material can substantially influence charge transport, electronic band structure, and optical properties. Nano-WO₃ is readily reduced, and nonstoichiometry is reported to involve structural changes.^{27–29} Substoichiometry gives rise to polarons, which change the optical properties and increase the absorption in the near-infrared (NIR) spectral region.^{29,30} For small values of substoichiometry, x , crystals of WO_{3–x} are reported to undergo a structural phase transition from the room temperature δ phase to the low temperature ϵ phase at $T \sim 250$ K.³¹ The δ phase shows metallic behavior, and the ϵ phase has insulating properties for the electron/hole carriers.³² Reported values for the electronic band gap of

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nano-WO₃ vary considerably from $E_g = 2.6$ to 3.25 eV,^{33,34} and this is probably due to a combination of one or several of the effects discussed above. Further, the small size of nano-WO₃ crystallites will enhance the surface energy of the system.^{35,36} With higher surface energy, the melting point and temperature for phase transitions decrease.³⁷

In this article, we report on the preparation and characterization of the structural, optical, and PC properties of nano-WO₃ films made with reactive dc magnetron sputtering. This method offers freedom in deposition conditions and is suitable to span a large parameter space to address some of the issues discussed above. In particular, the physical properties of nano-WO₃ films have been studied as a function of working pressure, P_{tot} . The photodegradation of stearic acid (SA) was measured to determine the degradation rate and quantum yield for the different nano-WO₃ films prepared at different P_{tot} .

II. EXPERIMENTAL SECTION

A. Sample preparation

Nanocrystalline tungsten oxide thin films were prepared by reactive dc magnetron sputtering using a versatile deposition system based on a Balzers UTT 400 unit (Balzers AG, Balzers, Liechtenstein). The sputter target was a 5-cm-diameter plate of W with 99.95% purity (Plasmatronics, Inc., Livermore, CA). Sputtering was conducted in a plasma of Ar and O₂. The purity of the gases was 99.998%, and the sputtering power was set to 200 W with the substrates positioned 13 cm from the target. The total working pressure was varied between $P_{\text{tot}} = 1.3, 2.0, 3.3,$ and 4.0 Pa, respectively. The substrate temperature was maintained at $T_s = 553$ K, and the O₂/Ar gas flow ratio was kept fix at 0.43. The deposition time was set at 35 min, and the sample holder was rotating with constant speed to obtain uniform thickness of the films. The samples were subsequently postannealed at $T_a = 673$ K for 1 h. Films were sputtered on 13-mm-diameter CaF₂ substrates (Crystran Ltd., Poole, UK). The CaF₂ substrates were cleaned with deionized water and ethanol before sputtering.

B. Material characterization

The surface morphology and grain sizes of the formed nanostructures were characterized with scanning electron microscopy (SEM), using a LEO 1550 FEG instrument (LEO Electron Microscopy Ltd., Cambridge, UK) with in-lens detector operating at 10 kV.

The crystalline structure of the films was determined by x-ray diffraction (XRD). For thin films, grazing incidence x-ray diffraction (GIXRD) was used (Siemens D5000 Th-2Th, PANalytical B.V., Almelo, Netherlands), using Cu K α ($\lambda = 1.54051$ Å) radiation. Scans were taken in the range from 10 to 90° (2 θ). Broadening of the diffraction peaks due to the average grain size, L , and strain, ε , are present

simultaneously and were extracted from experimental data using the Williamson–Hall method³⁸:

$$\cos(\theta)(\beta_c - \beta_i) = \frac{k\lambda}{L} + \langle \varepsilon^2 \rangle^{1/2} \sin(\theta) \quad , \quad (1)$$

where $\varepsilon = \Delta L/L$ is the strain in the $[hkl]$ direction, $k \approx 0.9$ is the geometric shape factor for a spherical scatterer, λ is the x-ray wave length, β_c the full width at half maximum, FWHM, of the XRD peak, β_i the instrumental broadening, and θ the diffraction angle. The program XPERT PRO was used to remove the contribution from the Cu K α_2 line and determine β_c . Peaks in the diffractograms were fitted to a weighted superposition of the Gauss and Cauchy functions.

Raman spectra were recorded in backscattering geometry using a confocal Raman microscope (HR800 Labram; Horiba Jobin-Yvon, Lille, France). A 514-nm Ar laser was directed through a 50x long working distance objective (NA = 0.45), using a 600 grooves/mm grating, yielding a spectral resolution of approximately 3.5 cm^{-1} . A low laser power (5 mW) was used to ensure that no structural modifications of the samples occurred due to local laser heating. The spectra were calibrated against the Si peak at 520.7 cm^{-1} of a Si(110) wafer.

Composition, stoichiometry, and density were determined using the Rutherford backscattering spectroscopy (RBS) on films deposited on C substrates. The measurements were carried out at the Uppsala Tandem Accelerator Laboratory using ⁴He ions at energy of 2 MeV. An azimuthal angle $\alpha = 7^\circ$ was applied to avoid the risk of channeling into the crystals. The ions were backscattered at an angle of 172°. Data were analyzed with the program SIMNRA, which yielded the number of atoms per cm² (N_s) and the number of atoms in a formula unit (N). For a perfect stoichiometric film, the number of atoms in a WO₃ unit is $N = 4$, and for understoichiometric films, $N = 4 - X$, where X is the number of missing O atoms. Film density, δ , was calculated from the formula:

$$\rho = \frac{MN_s}{NdN_A} \quad , \quad (2)$$

where M is the mass per mol of formula unit, N_A is the Avogadro constant, and d is the film thickness (in cm).

Optical properties were measured with a Perkin-Elmer Lambda 900 double-beam UV/Vis/NIR spectrophotometer (PerkinElmer, Waltham, MA) equipped with an integrating sphere and a Spectralon reflectance standard. The absorbance, $A(\lambda)$, was determined from measured transmittance, $T(\lambda)$, and reflectance, $R(\lambda)$, according to:

$$A(\lambda) = 1 - T(\lambda) - R(\lambda) \quad , \quad (3)$$

and using appropriate corrections for diffuse scattering and instrument calibration.³⁹

The film thickness, d , was determined both from surface profilometry (Tencor Alpha Step 200, SPEC,

Santa Clara, CA) and calculated from the interference fringes seen in optical transmittance data, following the method of Swanepoel⁴⁰:

$$d = \frac{\lambda_1 \lambda_2}{2(\lambda_1 n_2 - \lambda_2 n_1)} \quad (4)$$

where n_1 and n_2 are the refractive indices at two adjacent transmittance maxima at λ_1 and λ_2 , respectively. The refractive index of the CaF₂ substrate, s , was determined from transmittance measurements of the bare substrate. From the transmittance maxima, T_M , and minima, T_m , of the interference fringes seen in the spectrum for WO₃ thin films on CaF₂ substrates, a refraction number, N , was calculated according to:

$$N = 2s \frac{T_M - T_m}{T_M T_m} + \frac{s^2 + 1}{2} \quad (5)$$

The refractive index, n , of the films was then calculated from the equation:

$$n = [N + (N^2 - s^2)^{1/2}]^{1/2} \quad (6)$$

From $T(\lambda)$ and $R(\lambda)$, the absorption coefficient, $\alpha(\lambda)$, can be determined according to⁴¹:

$$\alpha(\lambda) = \frac{1}{d} \ln \left(\frac{1 - R(\lambda)}{T(\lambda)} \right) \quad (7)$$

where d is the thickness of the film.

C. Photodegradation measurements

Photodegradation of SA (C₁₈H₃₆O₂; Merck, Darmstadt, Germany) was measured with Fourier transform infrared (FTIR) spectroscopy operated in transmission mode using a Bruker IFS66v/S spectrometer (Bruker, AZ Wormer, Netherlands). FTIR spectra were recorded with 4 cm⁻¹ resolution using 30 s scan time per spectrum and 30 s dwell time between consecutive spectra. Application of SA was done following earlier reported methods to determine self-cleaning properties of TiO₂.^{42,43} SA was applied to the surface of the WO₃ films by pipetting 10 mm³ of 0.8 mM methanol solution followed by spin coating at 1500 rpm. FTIR spectra were, after appropriate baseline corrections, integrated between 2700 and 3000 cm⁻¹, which contains the v(C-H) vibrations in SA. The number of SA molecules per cm² per integrated absorbance unit (1 A.U.) in this wave number region has previously been reported to be $N_{\text{I.A.U.}} = 3.17 \times 10^{15}$ molecules/cm² for TiO₂.⁴² The number of SA adsorption sites on the WO₃ surface were estimated using an organic dye molecule D35 (C₅₄H₅₈N₂O₆S; Merck; $M_w = 863.11$ g/mol) as previously reported.⁴⁴ D35 has one anchoring carboxyl group just like SA. A sample of WO₃ thin film was immersed for

12 h in 0.2 mM solution of dye dissolved in ethanol. Absorbance spectra were measured using a Perkin-Elmer Lambda 900 double-beam UV/Vis/NIR spectrophotometer. The absorbance of the bare WO₃ thin film on a CaF₂ substrate was subtracted to obtain the absorbance due to D35. To calibrate the absorbance, a dye solution of 0.01 mM in ethanol was recorded on a HR-2000 Ocean Optics fiber optics spectrophotometer (Ocean Optics, Dunedin, FL). A normal quartz cuvette (1 cm path length) was used for the measurement of dye solution. From the Beer-Lambert's law, $I = I_0 \times 10^{-\epsilon cd}$, where ϵ is the extinction coefficient ($\epsilon_{\text{D35}} = 31300$ M⁻¹/cm), c the concentration, and d the thickness, the D35 concentration on the WO₃ film was determined to 0.0013 mM, which corresponds to 0.0013 μmol/cm² or 7.82×10^{14} molecules/cm².

A Hg arc lamp operated at 300 W was used as irradiation source. Band-pass filters (Oriol Instruments, Stratford, CT) centered at 546, 436, 406, and 313 nm, respectively, each with a bandwidth of $\Delta\lambda = 10$ nm, were used to measure the photodegradation rate at different wave lengths in the band gap region. To reduce the infrared part of the lamp spectrum, the light was first directed through a 75-mm-long water filter (Milli-Q water, 18.2 MΩ). The light was collected into a fused silica fiber bundle and directed onto the sample cell through a CaF₂ window at an angle of 25° to the surface normal. The photon power was measured to be 102 mW/cm² in the spectral range between 300 and 800 nm using a thermopile detector (Ophir, North Andover, MA).

A lower limit of the quantum yield, Φ (assuming all absorbed photons in the film reach the surface), was calculated according to:

$$\Phi = \frac{N_{\text{I.A.U.}} A_0 k_{\text{dec}}}{\int F(\lambda) (1 - e^{-\alpha(\lambda)d}) d\lambda} \quad (8)$$

where A_0 is the integrated absorbance between 2700 and 3000 cm⁻¹ due to SA at $t = 0$ min, k_{dec} is the degradation rate (s⁻¹), $F(\lambda)$ is the photon flux (s⁻¹/cm²), $(1 - e^{-\alpha(\lambda)d})$ is the absorption in the WO₃ film, and d is the film thickness.

In a second experiment, simulated solar light was used using a Xe arc lamp source operated at 200 W and filtered through a set of air mass filters (AM1.5). The light source setup was otherwise identical to the one described above. The photon power was measured to be 100 mW/cm² in the wave length range 300–800 nm in these experiments.

III. RESULTS AND DISCUSSION

A series of WO₃ thin films were prepared by reactive dc magnetron sputtering at different working pressures (Table I). All samples showed high optical transparency after postannealing at $T_a = 673$ K for 1 h. The samples sputtered at low working pressure, $P_{\text{tot}} = 1.3$ and 2.0 Pa,

showed a light bluish color, whereas films prepared at $P_{\text{tot}} = 3.3$ and 4.0 Pa showed a slight yellow to red coloring.

A. Scanning electron microscopy

Figure 1 shows SEM images of sputtered nano-WO₃ films prepared at low and high P_{tot} , respectively. It is evident from Fig. 1(a) that films with rectangular shaped

TABLE I. Summary of process parameters and physical properties of nano-WO₃ films fabricated by reactive dc magnetron sputtering.

Sample	Working pressure, P_{tot} (Pa)	Gas flow ratio O ₂ /Ar	Grain size ^a (nm)	Thickness ^b (nm)	Refractive index, n	Density (g/cm ³)
a	1.3	0.43	15	1112	2.14	6.58
b	2.0	0.43	28	872	2.07	N/A
c	3.3	0.43	49	460	2.1	N/A
d	4.0	0.43	55	400	2.01	6.38

^aFrom Eq. (1).

^bFrom Eq. (4).

^cFrom Eq. (6) at $\lambda = 550$ nm.

(a)

(b)

FIG. 1. SEM images of nano-WO₃ thin films sputtered at (a) $P_{\text{tot}} = 1.3$ Pa and (b) $P_{\text{tot}} = 4.0$ Pa. The films were sputtered at $T_s = 553$ K and postannealed at $T_a = 673$ K for 1 h.

structures are formed at low P_{tot} . Inspection of the images reveals that sizes of these structures are approximately between 30 and 60 nm. At $P_{\text{tot}} = 4.0$ Pa, the films appear to consist of structures with rounder shapes [Fig. 1(b)]. The underlying substrate is clearly seen in the cracks between the structures, which is consistent with lower deposition rate with increasing P_{tot} and hence thinner films. The image indicates a relatively porous morphology, where the grain boundaries are smeared out.

B. Rutherford backscattering spectroscopy

Figure 2 shows spectra from RBS measurements of films prepared at low and high P_{tot} , respectively. Also shown in Fig. 2 are corresponding simulated spectra using SIMNRA, from which the stoichiometry and density of the films were obtained.⁴⁵ In all cases, the nano-WO₃ films exhibited a stoichiometry of WO_{3-x} with $|x| < 0.1$. However, within the uncertainty in these calculations (4%), the variation in x of nano-WO₃ films due to different P_{tot} could not be distinguished. The calculated density was determined to be $\delta = 6.58$ g/cm³ and $\delta = 6.38$ g/cm³ for films prepared at $P_{\text{tot}} = 1.3$ and 4.0 Pa, respectively. The RBS results show that high sputtering rates (i.e., low P_{tot}) result in more dense films, while low sputtering rates (i.e., high P_{tot}) result in films with lower density. Compared with the bulk density of WO₃ ($\delta = 7.14$ g/cm³), it is seen that the film porosity is between 8% and 11%, i.e., the films are rather compact. These results qualitative corroborate the SEM results presented above.

C. X-ray diffraction

Figure 3 depicts XRD spectra of nano-WO₃ films at different P_{tot} . The structural distortions of the corner-sharing WO₆ octahedra comprising the WO₃ unit cell are quite complex and make definitive assignments of WO₃ phases from XRD data alone rather difficult, despite the apparent simple stoichiometry of WO₃. In Fig. 3, the most interesting part of the spectra, acquired between $2\theta = 10^\circ$ and 90° , is extracted. The first diffraction peaks in Fig. 3 correspond to reflection from the (002), (020), and (200) planes, respectively, and are in good agreement with reported diffractograms for the δ -WO₃ and monoclinic γ -WO₃ phases.⁴⁶ These two phases are very similar with respect to angular distortions and atomic distances and are thus expected to have similar thermodynamic stability. Indeed, both phases have been reported to coexist at room temperature and are sensitive to the way the samples are prepared, e.g., T_s , T_a , and P_{tot} .^{46–48} However, the (002) diffraction angle in ϵ -WO₃ at 23.19° is close to the corresponding reflections in the γ -WO₃ and δ -WO₃ phases,²⁹ which occur at 23.12° ,⁴⁶ and the experimental value of the peak at 23.15° may indicate mixing of the low temperature monoclinic ϵ -WO₃ phase at low P_{tot} . Supporting this argument is the observation of the peak at 24.25° ,

FIG. 2. RBS spectra of nano-WO₃ thin films on carbon substrates, sputtered at (a) $P_{\text{tot}} = 1.3$ Pa and (b) $P_{\text{tot}} = 4.0$ Pa, respectively.

FIG. 3. XRD patterns of the nano-WO₃ thin films prepared at different $P_{\text{tot}} = 1.3 - 4.0$ Pa. Circles correspond to diffraction peaks due to γ -WO₃ [(from the left (002), (020), (200), (-202), (022) and (202)]. Squares correspond to diffraction peaks due to ϵ -WO₃ [(from the left (002), (110), (-112), (200) and (112)].

which is shifted to lower diffraction angles compared with references for the monoclinic γ -WO₃ (200) planes at 24.37° and triclinic δ -WO₃ (200) planes at 24.33° .⁴⁶ This may be due to a feature from the low temperature monoclinic phase ϵ -WO₃ (110) planes at 24.11° . Finally, it is apparent that the intensity of the peak corresponding to the (020) planes decreases relative to peaks from diffraction planes of (002) and (200) with increasing P_{tot} . In the range $2\theta = 33-35^\circ$, the highest intensity occurs at $P_{\text{tot}} = 1.3$ Pa, and the diffractogram resembles the ϵ -WO₃ phase, which has an analogous XRD pattern, and a dominant peak at 33.34° , corresponding to the (-112) reflection,²⁹ again supporting significant ϵ -WO₃ phase mixing at low P_{tot} . With increasing P_{tot} , the relative intensity of the (-112) reflection decreases compared to the adjacent peak from diffraction planes of

(202) at 34.08° , which eventually dominates the XRD spectrum at $P_{\text{tot}} = 4.0$ Pa, and corresponds to reflection in either the δ -WO₃ or the γ -WO₃ phase, which is reported to occur at 34.08° and 34.17° , respectively. Which one of these latter two phases is most abundant cannot be determined from the XRD data. The phase transitions in nano-WO₃ films occur gradually rather than abruptly, as in bulk WO₃, and result in a range of coexisting phases depending on exact preparation conditions. However, previous reports have shown that the temperature range of coexisting δ and ϵ phases is much larger than the simultaneous existence of δ and γ phases,⁴⁶ which may indicate that the ϵ and δ phases are the dominant phases in our nano-WO₃ films.

In Fig. 3, it is seen that the intensity of the diffraction peaks in the $22.5-24.5^\circ$ range increases with increasing P_{tot} , whereas the intensity of the peaks in the range $33-35^\circ$ decreases. We conclude that the nano-WO₃ exhibits a preferred growth direction depending on P_{tot} , which changes with increasing pressure from the [202] and [-112] directions to the [020] and [200] directions.

Average grain size and strain were calculated from the broadening of the diffraction peaks using Eq. (1). Figure 4 shows a Williamson–Hall plot, where the experimental data are fitted by straight lines. The strain was obtained from the slope of the lines and the grain size from their intersection with the y-axis. It is seen that strain is significant for films sputtered at 1.3 Pa with $\epsilon \approx 3.6\%$, while it is $\epsilon \approx 1.7\%$ for films sputtered at 4.0 Pa. The high strain in the film sputtered at 1.3 Pa is probably caused by imperfections such as oxygen vacancies, phase mixing with the ϵ -phase, and may also be related to its higher density. The average grain sizes are given in Table I. The linear fit is more uncertain for the sample prepared at 1.3 Pa due to overlapping reflection peaks, which are difficult to unambiguously separate.

FIG. 4. Williamson-Hall plot using data on diffraction angle and broadening from experimental XRD spectra. Fits to Eq. (1) are given by the straight lines. The approximate linear relations indicate strain effects in films sputtered at 1.3 Pa, $\varepsilon = 3.6\%$ with average grain size $L = 15$ nm and at 4.0 Pa, $\varepsilon = 1.7\%$ and $L = 55$ nm.

Low P_{tot} and hence high sputter rate, i.e., high kinetic energy of the particles bombarding the surface, may result in slight compression of the films, which is reported to influence the WO₃ structure and phase.⁴⁷ Under these sputter conditions, significant amounts of oxygen vacancies may also be created, which give rise to polarons (see below).³⁴ In nano-WO₃ thin films, both grain size and substrate interactions are suggested to change the relative thermodynamic stability of WO₃ phases.³⁷ A transition to a compressed phase can be obtained either by using high external pressure or by accumulating internal compressive strain due to polarons.^{23,47} It has been reported that slightly reduced WO_{3-x}, with $x \approx 0.05$, promotes formation of the ε phase,²⁹ qualitatively consistent with our data. There is no change of the octahedral tilt angle between the δ -WO₃ and ε -WO₃ phases. Instead, the position of the central W atom is shifted in ε -WO₃, which develops a spontaneous polarization along the a -axis in the unit cell. Of all WO₃ phases, ε -WO₃ is the only structure, which is noncentrosymmetric. This results in variations of the O-W-O atom distance along the [110] direction, which affect the electrical and optical properties of the ε -phase. In particular, higher E_g for ε -WO₃ relative to δ -WO₃ has been reported.²⁴

D. Raman spectroscopy

Figure 5 shows Raman spectra of nano-WO₃ films prepared at different P_{tot} . Peaks 6 and 7 are typical for crystalline WO₃ and are common to several WO₃ phases. These correspond to the symmetric and asymmetric $\nu(\text{O}-\text{W}-\text{O})$ stretching modes.^{49,50} Peak 6 has a shoulder at lower wave numbers, which has a maximum at approxi-

FIG. 5. Raman spectra of nano-WO₃ films prepared at different P_{tot} . Peaks are labeled 1 = 125 cm⁻¹, 2 = 136 cm⁻¹, 3 = 184 cm⁻¹, 4 = 274 cm⁻¹, 5 = 323 cm⁻¹, 6 = 715 cm⁻¹, and 7 = 807 cm⁻¹.

mately 645 cm⁻¹, characteristic for the monoclinic ε -phase.^{50,51} It should be noted that this vibrational band also has been discussed in the literature as being due to hydrated tungsten oxide.^{49,52} Our combined RBS, XRD, and Raman spectroscopy data give, however, no evidence of hydrated tungsten oxide, and this can therefore be ruled out. Peaks 2, 4, and 5 correspond to the $\delta(\text{W}-\text{O}-\text{W})$ bending vibrations in monoclinic γ and triclinic δ phases.⁵¹ The intensity of peak 5 can be correlated to the amount of the monoclinic γ -phase according to some reports.⁵⁰ The relatively large intensity of peak 5 and the relatively broad peaks 6 and 7 compared to bulk data may also be indicative of the nanoporosity in the films. A relatively high intensity of the band at approximately 330 cm⁻¹ is, e.g., reported for W₁₈O₄₉ compounds.⁵³

Peak 1 agrees with previous reports of the presence of ε -WO₃ phase,⁵³ consistent with XRD data, but we note that a similar peak has previously also been interpreted as being due to the triclinic δ -phase.⁴⁷ However, the presence of a small peak at 184 cm⁻¹ (peak 3), which previously has been assigned to the ε phase,⁴⁸ supports the interpretation of peak 1 as being due to an ε phase. In spectrum obtained at $P_{\text{tot}} = 2.0$ Pa in Fig. 5, the intensity of peak 1 is observed to decrease together with the shoulder at 645 cm⁻¹, compared with spectrum obtained at 1.3 Pa. Simultaneously, the intensity of peak 2 increases, which indicates a higher fraction of the δ or γ phase as P_{tot} increases. In comparison with XRD data in Fig. 3, we see that similar changes occur between $P_{\text{tot}} = 1.3$ and 2.0 Pa, where the (002) peak increases. We conclude that a structural transition occurs somewhere between these two values of P_{tot} , where the relative fraction of δ or γ phase increases at the expense of the ε -phase.

A weak vibration at 940 cm⁻¹ is observed at 3.3 Pa and 4.0 Pa in Fig. 5, which can be assigned either to the W-O surface mode⁵⁴ or a $\nu(\text{W}=\text{O})$ mode due to terminal

W = O surface groups, which are reported to be located at about 950 cm⁻¹.^{37,52} Since this peak appears on the thinner films, which have higher porosity, it is tempting to attribute it to surface W = O species. It qualitatively correlates with the SEM, RBS, and XRD results above, i.e., the films become more porous with increasing P_{tot} . This is also qualitatively supported by the concomitant increase of the FWHM of peak 6 and 7, which indicates a decrease of the structural order in the films.

E. UV-vis spectroscopy

Absorption in the films was calculated from transmittance and reflectance measurements. Figure 6 shows the absorption coefficient in the wave length range 300–2500 nm for nano-WO₃ films prepared at different P_{tot} . The oscillations, mainly present in the 500–1000 nm wave length range, are interference fringes that are not compensated for by Eq. (7). $T(\lambda)$ is measured at normal incidence and $R(\lambda)$ at a slightly different angle. It is obvious that there is significant absorption in the NIR region, exhibiting a broad peak maximum centered at about 1500 nm, consisting of (at least) two absorption bands. With increasing P_{tot} , the NIR absorption decreases. At $P_{\text{tot}} = 3.3$ and 4.0 Pa, only two weaker NIR bands are observed at 1200 and 1600 nm. The absorption in this range has earlier been attributed to polarons.^{55,56} Maxima near 1450 and 1800 nm have previously been observed in a substoichiometric WO_{3-x} ϵ phase, as reported by Salje.³⁰ These peaks were ascribed to two types of polarons that occur simultaneously, one extended mobile type and the other more localized.

From the results above, a slightly substoichiometric and strained film structure, which consists of a small amount of the ϵ phase, is inferred at low P_{tot} . Both the strain and the ϵ phase gradually disappeared at higher P_{tot} , as evidenced by XRD and Raman spectroscopy. The strength of the polaron

FIG. 6. The absorption coefficient α in the wave length range 300–2500 nm for nano-WO₃ thin films prepared at different P_{tot} between 1.3 and 4.0 Pa.

absorption indicates that $x \approx 0.01$ at 1.3 Pa and decreases with increasing P_{tot} , in fair agreement with the RBS results. This estimate was obtained from a comparison with published polaron absorption strengths for Li-WO₃ thin films.⁵⁷ It is thus evident that optical transmittance and reflectance measurements are much more sensitive to detect small substoichiometries than RBS.

In a simple model, the band gap can be approximated from the slope of the absorbance. We refer to a forthcoming publication for a detailed account of the nature of the interband excitations in WO₃ and the existence of band gap states in nano-WO₃ films. Here, it suffices to note that band gap states contribute significantly to the absorption just below the optical band edge. Figure 7 shows that all absorbance curves meet at ~ 447 nm or ~ 2.78 eV. The band-to-band excitations of electrons from the valence band to the conduction band are seen as the steep slope in the short wave length range 300–445 nm. At ~ 447 nm, the inclination of the slope clearly changes, as marked by the dashed lines in Fig. 7. This marks the demarcation energy, which may be used to approximate the transition between the Urbach tail,⁵⁹ and the absorption due to electronic interband transitions. The demarcation energies deduced from the analysis are shown in Table II. The small absorption in the range 448–500 nm is

FIG. 7. Absorbance of nano-WO₃ films prepared at different P_{tot} between 1.3 and 4.0 Pa around the optical band edge in the wave length region 300–600 nm.

TABLE II. Band gap energy, E_g , deduced from UV-vis spectrophotometry and crystalline phases derived from XRD and Raman spectroscopy for nano-WO₃ thin films.

Sample	E_g (nm)	E_g (eV)	Phase
a	447	2.77	γ and/or δ , ϵ
b	448	2.77	γ and/or δ , ϵ
c	446	2.78	γ and/or δ
d	446	2.78	γ and/or δ

due to states in the band gap. These states can be caused by the mixing of phases and variations in bond lengths and angles (here evidenced by mixed phases inferred from XRD and Raman spectroscopy data), grain boundaries (here, the grain sizes deduced from XRD are generally smaller than SEM structures, suggesting that the SEM structures contain several grains), or strain effects (here inferred from XRD data and polaron absorption at low P_{tot}). Localized band gap states give rise to a new regime beyond the extended band edges. Photoexcited electrons and holes can interact with these localized states and contribute to photoinduced processes. In Sec. III. F, we explore whether these contribute to photodegradation of SA in comparison with interband excitations across the band edge.

F. Photodegradation of SA

Figure 8 shows the photodegradation of SA as a function of solar light irradiation time in a log-linear plot. It is apparent that the initial decay of the integrated SA absorbance between 2700 and 3000 cm⁻¹ as a function of irradiation time obeys first-order kinetics. In comparison with previous work on SA spin coated on TiO₂ using similar procedures, where multilayer SA was inferred,⁴² the first-order reaction kinetics indicates that the SA coverage in our case is in the monolayer regime. This is also quantitatively supported by the measured absorbance on the nano-WO₃ films, using the calibrated value for the integrated absorbance unit,⁴² and comparing with the estimated number of surface sites from the D35 titration measurements presented above. With

FIG. 8. Semilogarithmic plot of the normalized absorbance due to SA as a function of irradiation time for nano-WO₃ films prepared at different P_{tot} : (A) 4.0 Pa and (B) 1.3 Pa. A is the integrated absorbance between 2700 and 3000 cm⁻¹ due to the $\mu(\text{C-H})$ bands at time, t , and A_0 is the absorbance at $t = 0$. Simulated solar light (AM1.5) was used as light source.

these estimates, we obtain a maximum SA coverage of approximately 0.5 monolayer.

From Fig. 8, it is clear that k_{dec} is more than twice as high at $P_{\text{tot}} = 4.0$ Pa compared to 1.3 Pa, under otherwise identical conditions. These observations correlate with the findings above that the low P_{tot} nano-WO₃ films exhibit mixed phase structures, which are associated with strong polaron absorption due to the presence of a substoichiometric and strained film structure. This suggests that even the presence of small amounts of excess electrons in the band gap at approximately 1 eV below conducting band (CB), which give rise to the polaron absorption bands in Fig. 6, effectively can quench photoexcited electron-hole pairs. We propose a possible mechanism that may be responsible for the quenching of photoexcited electron-hole pairs in slightly substoichiometric WO₃. In Fig. 9, we schematically depicted this mechanism. Here, electrons populating localized polaron states rapidly recombine with photoexcited holes. Subsequently, photoexcited CB electrons repopulate these states. This is a relatively fast process compared with the interfacial charge transfer processes of CB electrons to the affinity level on adsorbed O₂. The efficiency of this process depends on the character of the polarons and how extended these states are. The small substoichiometry deduced from the polaron absorption may nevertheless, despite its low value $x \approx 0.01$, affect e-h pair recombination if the spatial extension of the polaron is large. This shows the importance of precise control of the materials synthesis to prepare photoactive WO₃ nanostructures.

Figure 10 shows the PC SA degradation rate, k_{dec} , and the quantum yield, Φ , calculated by means of Eq. (8)

FIG. 9. Schematic pictures of the electronic states in WO₃ responsible for photodegradation of organic molecules in air. (a) Excitation of a VB electron to the CB in stoichiometric WO₃ and interfacial charge transfer (O₂ reduction and organic oxidation) to adsorbed molecules at the surface. (b) Electron-hole pair excitation in substoichiometric WO_{3-x} with localized polaron states ~ 1 eV below CB gives rise to an electron-hole pair recombination process. The numbers indicate the sequence of reactions. The dashed square represents the location of band gap states responsible for the visible light photoactivity.

FIG. 10. Quantum yield (left ordinate) and degradation rate k_{dec} (right ordinate) as a function of photon energy (upper abscissa) and wave length (lower abscissa) for a nano-WO₃ film prepared at $P_{\text{tot}} = 3.3$ Pa.

TABLE III. Quantum yield and photodegradation rate of nano-WO₃ film prepared at $P_{\text{tot}} = 3.3$ Pa at different excitation wave lengths.

Wave length (nm)	Photon energy (eV)	$\Phi (\times 10^{-5})$	$k_{\text{dec}} (\text{min}^{-1})$
313	3.95	3.1	0.032
406	3.04	3.1	0.013
436	2.84	1.5	0.011
546	2.27	0	0

at different wave lengths for a nano-WO₃ film prepared at $P_{\text{tot}} = 3.3$ Pa. It is seen that k_{dec} decreases continuously up to 436 nm and is zero at 546 nm. Visible light active photodegradation is proved by the nonzero $k_{\text{dec}} = 0.011 \text{ min}^{-1}$ at 436 nm, about one-third of the value at UV photon energies (313 nm).

Table III summarizes the photodegradation data. It is, however, more instructive to look at Φ . The low Φ values compared to measurements in colloidal solutions can be attributed to the inefficient collection of photoexcited electron-hole pairs in the SA/nano-WO₃ film system, where excitations deep in the film must diffuse to the surface of the film to take part in SA photodegradation. Nevertheless, we find that Φ is about 50% lower at 436 nm than at UV energies and is equal at 406 and 313 nm. This suggests that there exists an energy threshold comparable to the demarcation energy estimated from the absorbance data. This gives further support that E_g is around 2.8 eV, in good agreement with previous reports.^{60,61} Further, a possible explanation of the lower Φ at 436 nm, may be that the states giving rise to absorption at $h\nu < 2.9$ eV, lie below the affinity level of O₂, so that only hole oxidation occurs at these smaller energies. Hence, in this model, the photooxidation reaction is not truly PC at these low photon energies, a hypothesis that warrants further studies.

IV. CONCLUSION

Nanostructured WO₃ films were prepared using reactive dc magnetron sputtering at different working pressures, P_{tot} . At high P_{tot} , stoichiometric nano-WO₃ films are formed, which exhibit a structure consisting of δ -WO₃, possibly coexisting with γ -WO₃. At low P_{tot} , the nano-WO_{3-x} films are slightly substoichiometric ($|x| < 0.1$), exhibit significant strain, have higher density, and contain significant amounts of the ϵ -WO₃ phase. These films are also associated with strong polaron absorption. The optical properties of nano-WO₃ films prepared at low and high P_{tot} , respectively, are very different despite their structural similarities and are manifested in their different color and NIR absorption. The energy band gap, defined by the demarcation energy, is, however, similar, $E_g \approx 2.8$ eV (445 nm). The existence of band gap states was inferred from weak absorption in the 450–500 nm region. Comparisons of the photodegradation rate at different P_{tot} showed that photodegradation rate was significantly reduced at low P_{tot} . This is attributed to substoichiometry and existence of a strained ϵ phase characterized by an efficient recombination process, whereby excess localized electrons in the band gap recombine with photoexcited electron-hole pairs. Wave length-resolved photodegradation measurements of SA showed that the nano-WO₃ films were visible light active up to wave lengths of at least 436 nm. A lower bound for the quantum yield was determined to be approximately 3×10^{-5} for films prepared at high P_{tot} at photon energies larger than the band gap energy. The quantum yield dropped to 50% above the band gap, at 436 nm, which is tentatively attributed to inefficient O₂ reduction due to photon absorption into low lying band gap states.

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