

# First-principles calculations into $\text{LiAl}(\text{NH}_2)_4$ and its derivative hydrides for potential sodium storage

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## ABSTRACT

In this work, we have employed the first-principles quantum physics method to investigate the light-metal based  $\text{LiAl}(\text{NH}_2)_4$  and its modified compounds as conversion electrode materials for sodium-ion batteries on the basis of state-of-the-art Density Functional Theory. The pure  $\text{LiAl}(\text{NH}_2)_4$  possesses an average voltage of 0.294 V (versus  $\text{Na}^+/\text{Na}^0$ ) and a theoretical specific capacity of 1093.77  $\text{mA h g}^{-1}$  for sodium storage. Among the modified materials, the  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  has the most excellent electrochemical properties with a theoretical specific capacity of 1249.57  $\text{mA h g}^{-1}$  and a low average voltage of 0.087 V (versus  $\text{Na}^+/\text{Na}^0$ ) for potential anode applications. The diffusion behavior of Na-ion is also improved in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  whether at 300 K or at 400 K, which indicates the prospective rate capability. The diffusion coefficient of Na-ion is obviously increased to  $3.667 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$  (in modified material) from  $1.500 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$  (in pristine material) at 400 K. The diffusion of Na-ion is calculated to be very fast in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  with a kinetic barrier of 0.31 eV. This work will provide impetus to the quantum design and experimental development of complex hydride materials for metal-ion battery applications.

## Introduction

Due to environmental pollution and the finite reserve of fossil fuels, the world's demand for green and clean energy is becoming more and more urgent. With the rapid development of society, the clean electric energy accounts for an increasing proportion in human energy use. In the current era, the lithium battery is playing an important role in electricity storage. However, due to the uneven distribution and relative shortage of lithium resources, the large-scale industry urgently seeks for lower-cost and more abundant resources for energy storage [1–3]. The sodium element which is in the same main group with lithium owns some similar physicochemical properties [4]. Geological surveys show that the abundance of sodium (2.75%) is significantly higher than that of lithium (0.002%) in the Earth crust and the sodium is widely distributed and readily available in the world [5]. Therefore, sodium-ion batteries (SIBs) are usually regarded as one of the most outstanding candidates especially for large-scale industrial system applications [6,7]. While, since the sodium-ion has a larger radius than lithium, most of the electrode materials for lithium batteries are not suitable for sodium storage

such as the commercial graphite anode materials [8,9]. Oumellal et al. propounded a new notion of using metal hydride as the negative electrode of battery, which provided great inspiration to get beyond the delamination/intercalation mechanism [10,11]. Their ability to undergo conversion reactions with lithium to function as capacitive anodes or to transport Li ions to perform as competent super-ionic conductors has been demonstrated [12–18]. While at present, the exploration of metal hydride materials' utilization in sodium ion batteries (SIBs) is very scarce. Attentions have been paid to electrode materials with appropriate redox potentials and high specific capacities with excellent electrochemical properties [19–21]. According to previous reports, metal hydrides showed the lowest polarization for conversion reaction materials. Compared with sulfides, phosphides, oxides, nitrides, and fluorides, using metal hydrides as the negative electrode of sodium-ion battery will have far-reaching significance to the promotion of sodium-ion battery and utilization of clean energy [22,23]. In 2002, Chen et al. proposed that the MNH (metal nitrogen hydrides) could release and absorb hydrogen reversibly in large quantity, which aroused people's attention to the research of metal nitrogen hydrides for hydrogen

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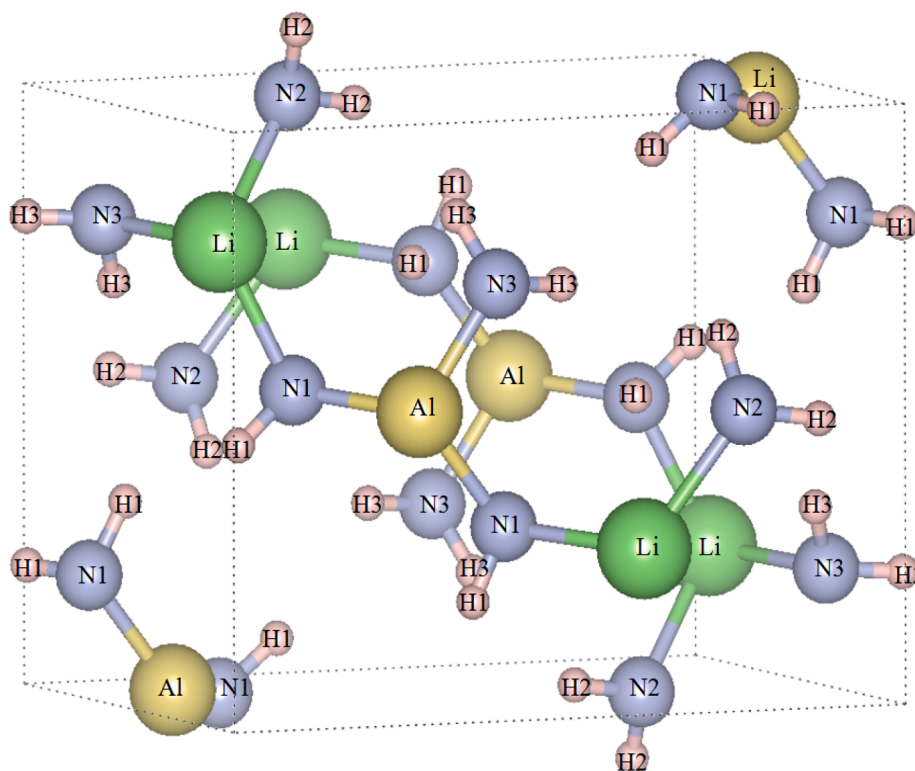
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**Fig. 1.** The complex structure of  $\text{LiAl}(\text{NH}_2)_4$  (56 atoms each unit cell) after structural optimizations. The green, gold, blue, and pink balls represent Li, Al, N, and H atoms, respectively. The atomic sites are distinguished by Arabic numbers. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

storage materials [24]. In the application of thermal-chemical hydrogen storage, people pay more attention to whether the material has excellent reversible property of hydrogen absorption and release. While for the electrochemical energy storage applications, the physical understanding of electrode reaction is the key to utilizing metal hydrides [25–28].

One of the powerful tools to understand many properties of materials is first-principles calculations [29–31]. The first-principles method is also of significance in dissecting the electrochemical performance of electrode materials and designing high performance sodium-ion battery materials [32–34]. Theoretical screening of electrode materials can lay important foundation for the selection of promising material(s) for battery applications, avoid a large number of blind experiments and help the development of excellent electrode materials more efficiently [35–42]. In this work, our investigation aims at exploring the potential properties of  $\text{LiAl}(\text{NH}_2)_4$  and its derivative materials for sodium-ion battery applications. The structural, electronic, electrochemical and diffusion-related kinetic properties are taken into consideration. We have chosen the two elements K (in the same main group as Li) and B (in the same main group as Al) for modifying the pristine compound. The different concentrations of B and K are also considered for modification to achieve better electrochemical properties and the diffusion kinetics of sodium-ions in these systems are also investigated. This quantum-mechanical study is proposed to help to understand the energy storage properties of the materials [43–45]. Furthermore, our findings have important implications for advancing the atomic-scale understanding of MNH (metal nitrogen hydrides) as potential conversion electrode materials in sodium-ion batteries (SIBs) and make important contribution and guide to the experimental development of the related materials for energy storage.

## Methods

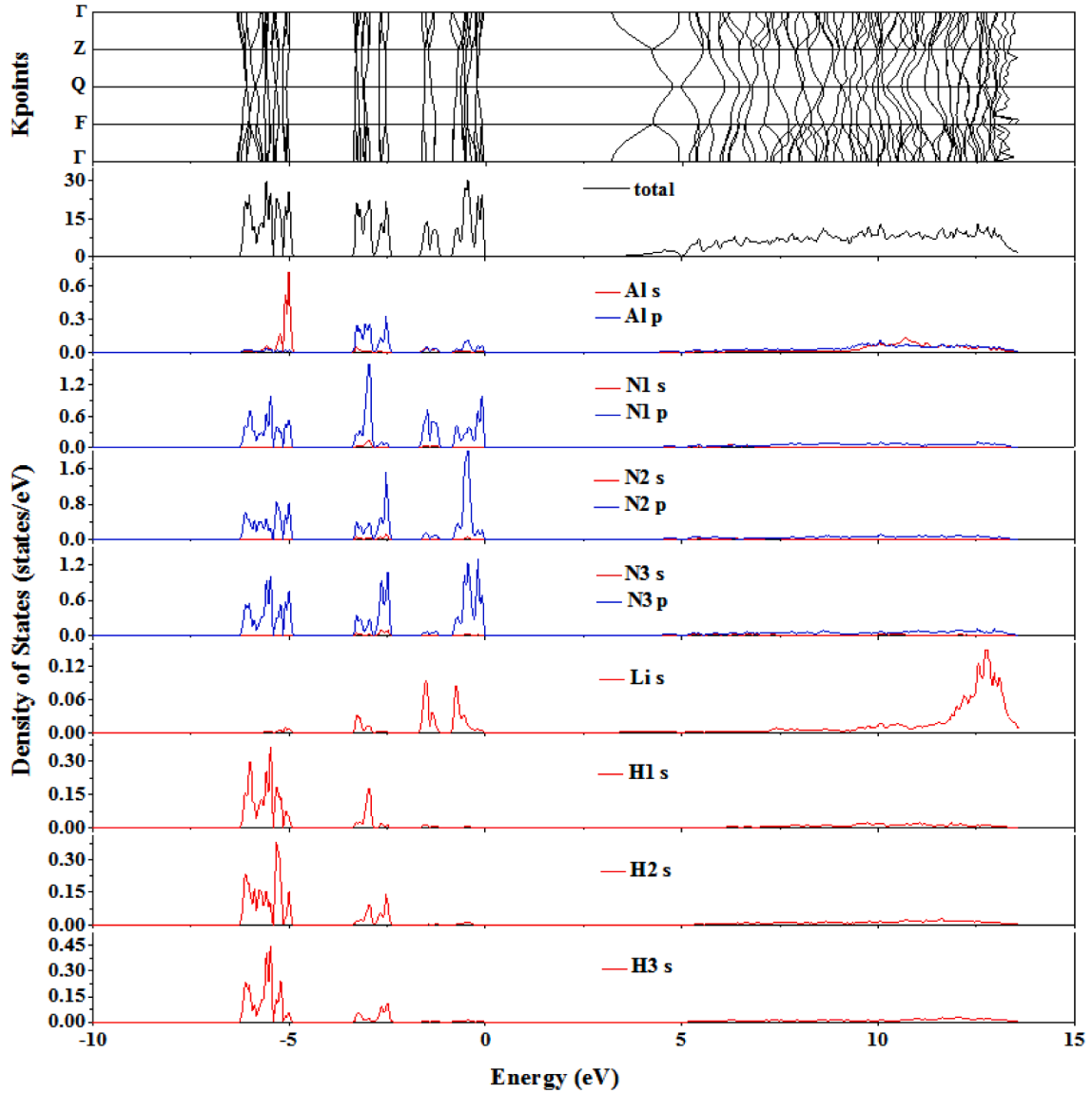
All the computational sections were carried out by Density

Functional Theory (DFT) method as implemented in Vienna Ab initio Simulation Package [46–48]. The inner electrons were represented by projector augmented wave (PAW) pseudopotentials [49,50]. The exchange correlation energy was treated by the Perdew-Burke-Ernzerhof (PBE) functional within the generalized gradient approximation (GGA) [51,52]. The crystal structures were optimized by the conjugate gradient algorithm. The Brillouin zone was sampled by  $5 \times 5 \times 7$  k-points using Monkhorst-Pack scheme in structural relaxations and the k-point of  $1 \times 1 \times 1$  was employed in time-consuming ab initio molecular dynamics (AIMD) calculations. We adopted the plane wave basis set with an energy cutoff of 520 eV. The force and energy convergence thresholds for structural optimizations were set to 0.02 eV/Å and  $10^{-4}$  eV, respectively. The calculation cell was enlarged to a supercell of  $2 \times 2 \times 1$  during the computations of mean squared displacement and diffusion coefficient. The Bader charge analysis was used to unveil the charge transfer inside the electrode materials.

During the investigations of Na-ion diffusion behavior in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ , some images were constructed using the linear interpolation method in CI-NEB [53,54]. The transition state in minimum energy pathway (MEP) was computed to obtain the diffusion barrier. The optimization thresholds were  $10^{-4}$  eV and 0.05 eV/Å for electronic and ionic relaxation, respectively. The spin-polarized calculations were performed throughout the work.

## Results and discussion

The low-temperature phase of  $\text{LiAl}(\text{NH}_2)_4$  is illustrated in Fig. 1. The geometrically optimized lattice parameters of the structure are:  $a = 9.499$  Å,  $b = 7.373$  Å,  $c = 7.476$  Å and  $\alpha = \gamma = 90^\circ$ ,  $\beta = 90.11^\circ$  with a monoclinic structure (space group of P21/n). There are 4 Al atoms, 4 Li atoms, 16 N atoms and 32 H atoms ( $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ ) in each unit cell. The calculated lattice parameters are consistent with the results obtained in experiments or other related computational works [55–57]. In the



**Fig. 2.** The electronic band structure, the total and partial density of states (DOS) for pristine  $\text{LiAl}(\text{NH}_2)_4$ . The s and p states are represented by red and blue colors respectively. The Fermi energy level is set at zero. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

structure, the 4 Al atoms are equivalent in site occupancy and 4 Li atoms as well. While, the 32 H atoms are classified into three different kinds of sites that are marked as H1, H2 and H3. Each unit cell has three different N sites that are designated as N1, N2 and N3 site respectively. The pristine  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  lattice has an ordered structure to potentially accommodate sodium-ions and facilitate the sodium-ion's diffusion through atomic gaps or interstitial spaces.

It is important to analyze the electronic density of states when exploring the chemical bonding in materials. As shown in Fig. 2, the total and partial DOS of the pristine  $\text{LiAl}(\text{NH}_2)_4$  solid are given. The total DOS of  $\text{LiAl}(\text{NH}_2)_4$  consists of three parts: the part below  $-2.417$  eV corresponds to the lower energy region of valence band; the part from  $-1.662$  eV to  $0$  eV corresponds to the higher valence band; and the part above  $3.302$  eV corresponds to the conduction band. From the partial DOS, there emerges distinct energy overlapping regions of N1 p-states and H1 s-states. Analogical cases are applied to N2 p-states and H2 s-states as well as N3 p-states and H3 s-states. This sp hybridization between N and H in valence band results in the strong bonding between N1 and H1, N2 and H2, N3 and H3 respectively. The bonding electrons are mainly those whose energy is between  $-1.662$  eV and Fermi level.

In view of the strategy that modification is a valid approach to improving the electrochemical properties of materials, we have used different concentrations of B or K elements (as mentioned in the introduction) to modify the pristine material in this study. Their designation can be expressed as  $\text{Li}_4\text{Al}_3\text{B}(\text{N}_4\text{H}_8)_4$ ,  $\text{Li}_4\text{Al}_2\text{B}_2(\text{N}_4\text{H}_8)_4$ ,  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ ,  $\text{Li}_3\text{KAl}_4(\text{N}_4\text{H}_8)_4$ ,  $\text{Li}_2\text{K}_2\text{Al}_4(\text{N}_4\text{H}_8)_4$ , and  $\text{LiK}_3\text{Al}_4(\text{N}_4\text{H}_8)_4$  respectively. We have substituted Al atoms or Li atoms in the 56-atom unit cell by B atoms or K atoms, which correspond to the modifying concentration of 1.79 at.%, 3.57 at.% and 5.36 at.%. In order to find the most reasonable modified structure, we have completely relaxed the crystal structures and determined the most stable site by referring to the value of formation energy after geometry optimizations. The formation energy can be calculated as follows:

$$E_f = E_T(\text{M}) + \mu_h - \mu_m - E_T(\text{P}) \quad (1)$$

where  $E_T(\text{M})$  and  $E_T(\text{P})$  represent the total energy of the modified and pristine structure respectively,  $\mu_h$  and  $\mu_m$  mean the atomic potential of the host and modifying atoms [58]. When one B or K atom substitutes a single Al or Li atom at the concentration of 1.79 at.%, the calculated

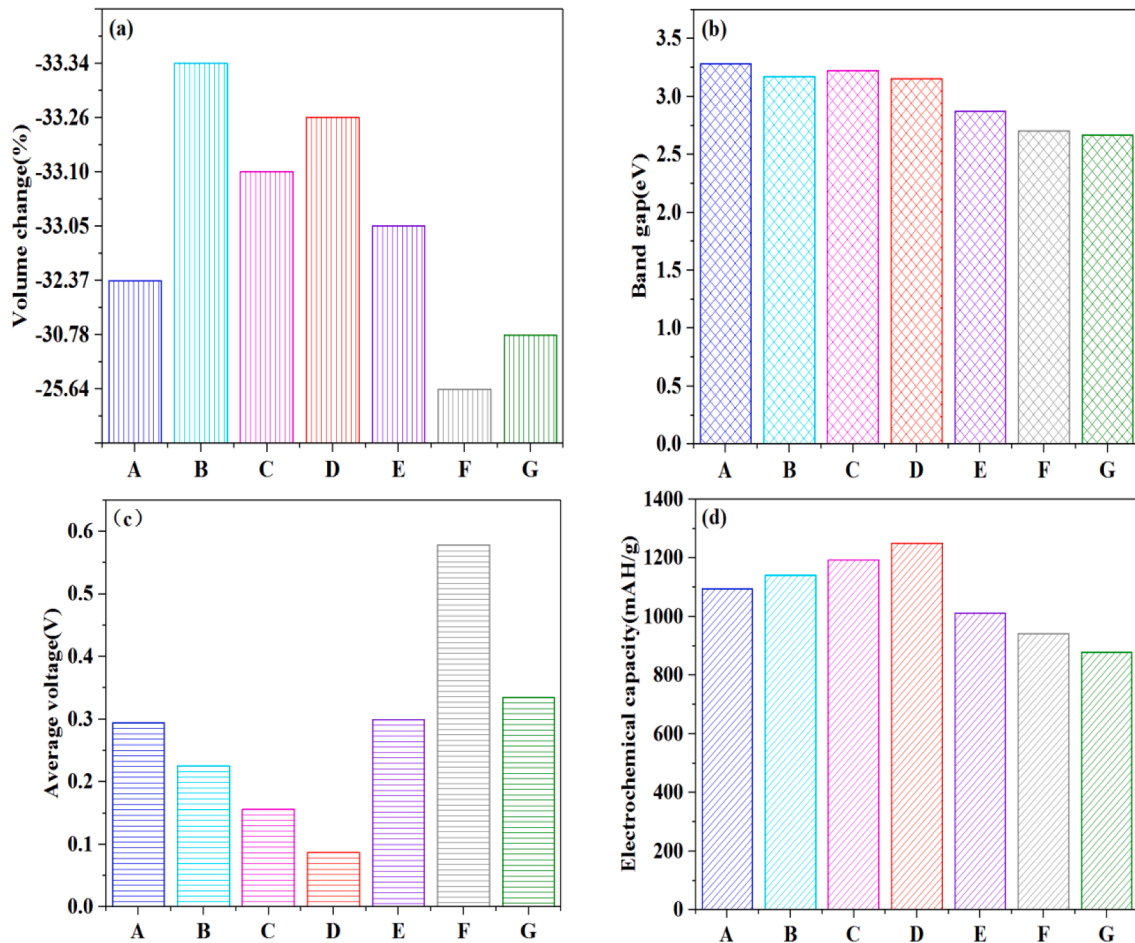
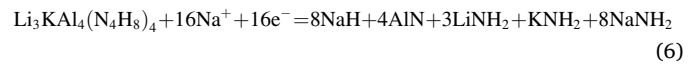
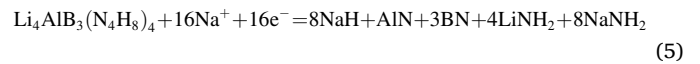
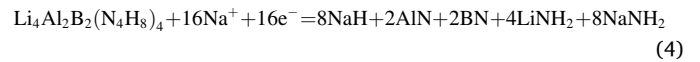
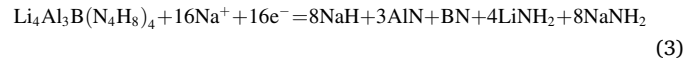
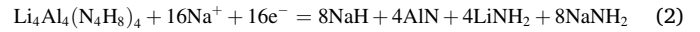
**Table 1**The calculated formation energies (eV/f.u.) for B- or K-modified LiAl(NH<sub>2</sub>)<sub>4</sub>.

Site	Element	
	B	K
Al site	-2.740	9.142
Li site	-1.003	1.930

formation energies are given in Table 1. It is clear that when the B element is utilized, the formation energy is lower when occupying the Al position. This indicates that the Al site is more thermodynamically favorable for the modification by the B atom. The formation energy is lower when the K atom occupies the Li atom instead of the Al site. We can conclude that the Li site is more thermodynamically favorable for the modification by K.

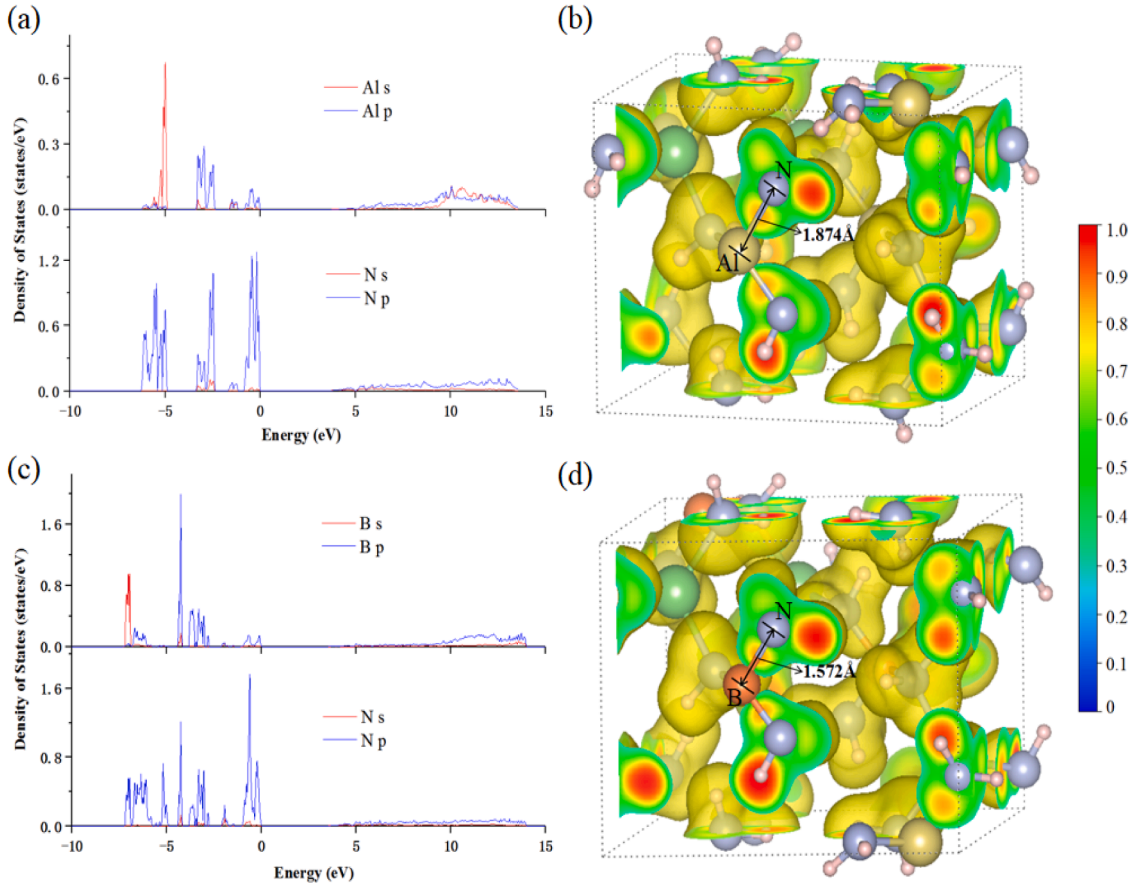
The charging and discharging conversion reactions of various LiAl(NH<sub>2</sub>)<sub>4</sub> derivative electrode materials are then investigated, described by the following half-cell reactions versus Na<sup>+</sup>/Na<sup>0</sup> in (2)–(8). The volume changes of various systems before and after conversion reactions are illustrated in Fig. 3(a). Most of the modifications increase the volume change. While, compared with the pristine system, the band gaps of all the modified systems are decreased in Fig. 3(b). The average voltage (versus Na<sup>+</sup>/Na<sup>0</sup>) of various derivative materials for sodium-storage electrodes is obtained by the formula (9) [59] where  $\Delta G$  is the Gibbs free energy variation of the reactions from (2)–(8) respectively and  $F$  is the Faraday constant. All the average voltage values versus Na<sup>+</sup>/Na<sup>0</sup> are below 0.6 V, i.e. 0.294 V for Li<sub>4</sub>Al<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, 0.225 V for Li<sub>4</sub>Al<sub>3</sub>B(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>,

0.156 V for Li<sub>4</sub>Al<sub>2</sub>B<sub>2</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, 0.087 V for Li<sub>4</sub>AlB<sub>3</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, 0.299 V for Li<sub>3</sub>KAl<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, 0.578 V for Li<sub>2</sub>K<sub>2</sub>Al<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub> and 0.335 V for LiK<sub>3</sub>Al<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub> respectively as described in Fig. 3(c). In addition, the theoretical specific capacities of various electrode materials can be calculated according to the formula (10), in which  $M$  stands for the molar mass of the anode material and  $n$  means the quantity of electrons involved in the electrode reactions. Li<sub>4</sub>AlB<sub>3</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub> has the highest specific capacity and the lowest average voltage as shown in Fig. 3(d).

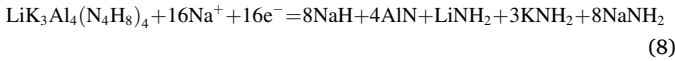
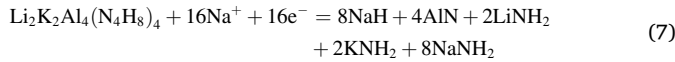


**Fig. 3.** Comparison of sodium-storage properties of Li<sub>4</sub>Al<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub> and its derivative materials: (a) volume change; (b) band gap; (c) average voltage versus Na<sup>+</sup>/Na<sup>0</sup>; (d) electrochemical specific capacity for sodium-storage. A: Li<sub>4</sub>Al<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, B: Li<sub>4</sub>Al<sub>3</sub>B(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, C: Li<sub>4</sub>Al<sub>2</sub>B<sub>2</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, D: Li<sub>4</sub>AlB<sub>3</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, E: Li<sub>3</sub>KAl<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, F: Li<sub>2</sub>K<sub>2</sub>Al<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>, G: LiK<sub>3</sub>Al<sub>4</sub>(N<sub>4</sub>H<sub>8</sub>)<sub>4</sub>.





**Fig. 4.** The calculated partial density of states and electron localization function for  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . (a) The partial DOS of the Al atom and N atom of  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ ; (b) the ELF of  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ ; (c) the partial DOS of the B atom and N atom of  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ ; (d) the ELF of  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . Al is shown in yellow sphere, N is in light blue and B is in orange. The Fermi level is set at zero. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



$$V \approx -\Delta G/F \quad (9)$$

$$\text{the specific capacity} = F \cdot n / 3600M \quad (10)$$

To further analyze the electronic structures of  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ , the partial electronic density of states of the two materials are described in Fig. 4. As shown in Fig. 4(a), the p-state of Al and the p-state of N have overlapping in the vicinity of Fermi level. And in Fig. 4(c), the p-state of B and the p-state of N have overlapping around the Fermi level, indicating that B and N are chemically bonded. The electron localization functions of two materials are described in Fig. 4(b) and (d), respectively. The ELF value between Al and N atoms is close to 1, indicating that there is a distinct covalent bond between Al and N atoms. The ELF value between B and N atoms is also close to 1 in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . The charge between Al-N bonds is more dense than that between Al-N bonds and the local bond length decreases to  $d_{\text{B-N}} = 1.572 \text{ \AA}$  from the pristine  $d_{\text{Al-N}} = 1.874 \text{ \AA}$ . In terms of their atomic structures, both B atoms and Al atoms have four coordination numbers and each atom forms a tetrahedral structure with four surrounding  $\text{NH}_2^-$  groups. The geometrically optimized lattice parameters of  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  are:  $a = 9.250 \text{ \AA}$ ,  $b = 7.297 \text{ \AA}$ ,  $c = 7.288 \text{ \AA}$  and  $\alpha = 90^\circ$ ,  $\beta = 91.90^\circ$ ,  $\gamma = 89.33^\circ$

**Table 2**

Comparison of energy, unit-cell volume and charge state of Na when one Na-ion migrates to different sites of  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ .

The migration sites	Energy (eV)	Volume ( $\text{\AA}^3$ )	Charge state ( $e^-$ )
Li site	-295.314	579.170	+0.801
Al site	-295.338	592.494	+0.799
Interstitial site	-295.247	599.794	+0.792

**Table 3**

Comparison of energy, unit-cell volume and charge state of Na when one Na-ion migrates to different sites of  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ .

The migration sites	Energy (eV)	Volume ( $\text{\AA}^3$ )	Charge state ( $e^-$ )
Li site	-302.691	561.122	+0.788
Al site	-302.650	554.581	+0.783
Interstitial site	-302.604	554.971	+0.797

with a triclinic structure (space group of P1).

The diffusion behavior of sodium ions in the electrode material is crucial for the kinetic performance during charging and discharging, thus it is indispensable to investigate the diffusion property of sodium-ions in electrode materials. Firstly, we considered a sodium ion in various sites of  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  lattice as well as  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  and further calculated the thermodynamically most stable site to accommodate the sodium ion. The calculated results are given in Tables 2 and 3. The results suggest that the Na-ion tends to move to the Al-site in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  lattice. While the Li-site is the most appropriate site to

**Table 4**

The diffusion coefficient of Na-ion in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  at 300 K and 400 K.

$\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ at 300 K	$\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ at 400 K	$\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ at 300 K	$\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ at 400 K
$9.167 \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$	$1.500 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$	$3.250 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$	$3.667 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$

which the Na-ion tends to move in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . With respect to the charge circumstance inside the materials, the Bader charge analysis has been done to unveil the charge states of each atom in two materials (the full information can be found in [Supplementary materials](#)). Na has the charge state of  $+0.799 \text{ e}^-$  when it migrates to the Al site in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and has the charge state of  $+0.788 \text{ e}^-$  when it migrates to the Li site of  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . [Table 4](#).

After determining the most stable initial site(s), the *ab initio* molecular dynamics (AIMD) calculations have been conducted to analyze the diffusion coefficient of the Na-ion in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  as well as  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . The mean squared displacement (MSD) both at 300 K (room temperature) and at 400 K is calculated as described in [Fig. 5](#). It is found that the Na-ion in the  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  electrode diffuses faster than in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  whether at 300 K or at 400 K.

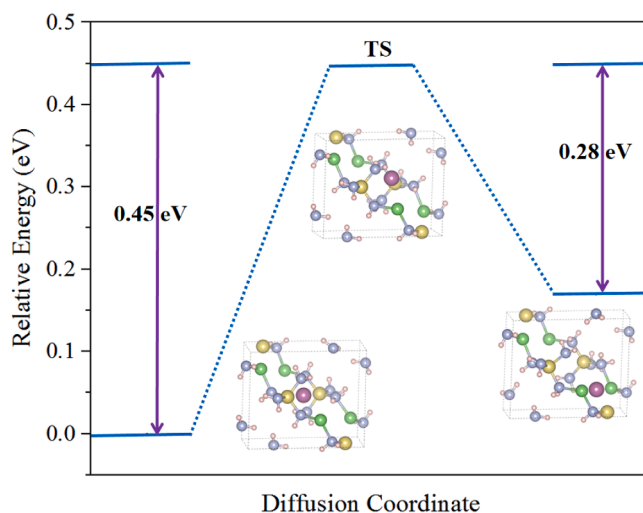
The quantitative diffusion coefficients of Na-ion in both  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  at 300 K and 400 K were further calculated through the Einstein equation:

$$\text{Diffusion coefficient } D = \text{MSD}/6N \cdot t \quad (11)$$

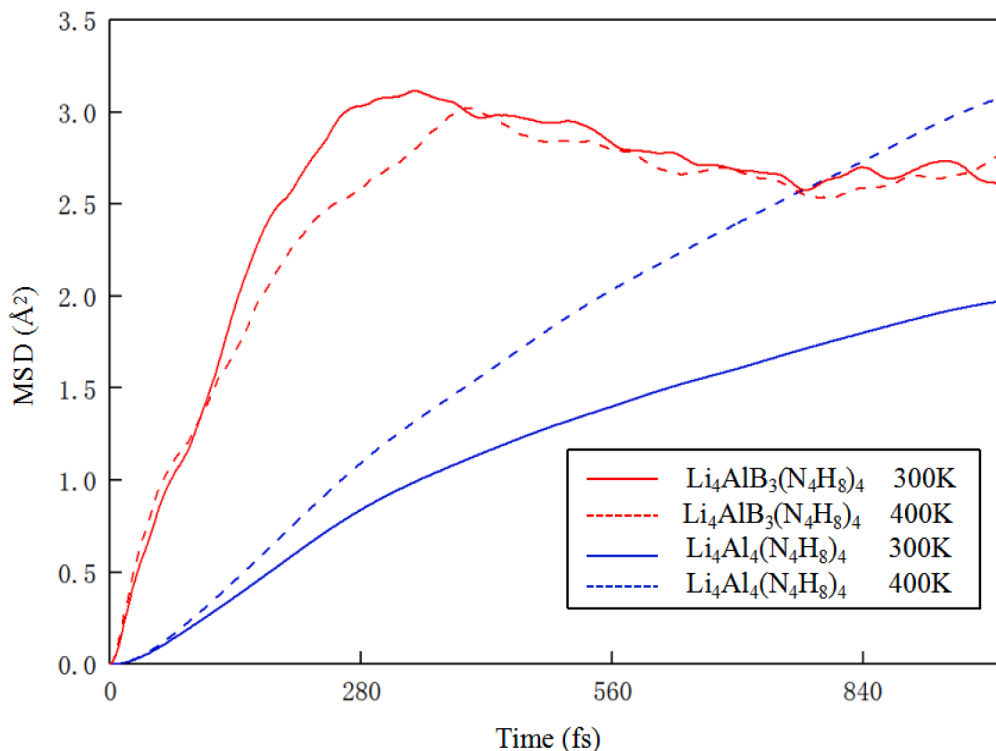
where  $N$  means the number of ions in the calculation model. The diffusion coefficient value of Na-ion in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  electrode is obviously increased to  $3.250 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ . The results indicate that the modification with B element is very beneficial to the diffusion and migration of Na-ion, thereby greatly improving the electrochemical performance of pristine hydride for SIBs.

The diffusion route and energy barriers of Na-ion in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$

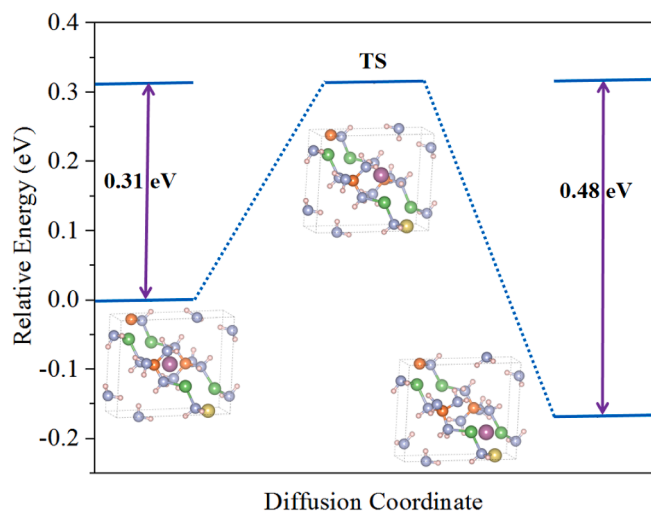
and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  have also been explored as shown in [Figs. 6 and 7](#). We explored the diffusion of Na-ion from the middle of two Al atoms to the middle of two Li atoms in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and from the middle of two B atoms to the middle of two Li atoms in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . When the Na-ion diffuses in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ , the energy barrier is calculated to be 0.45 eV. Interestingly, the Na-ion only needs to surmount a small energy barrier of 0.31 eV in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ , suggesting that the Na-ion is extremely easy to diffuse in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . In addition, compared with  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ , the energy of the final state in the whole diffusion process is lower than that of the initial state in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ , indicating that the diffusion process tends to more stable. These results suggest that the doping by B element will be highly beneficial to increase the potential



**Fig. 6.** Diffusion diagram of Na-ion (in purple color) in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$ . TS refers to the transition state. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)



**Fig. 5.** The calculated mean squared displacement of Na-ion in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  through *ab initio* molecular dynamics (AIMD) technique at 300 K and 400 K.



**Fig. 7.** Diffusion diagram of Na-ion (in purple color) in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$ . TS refers to the transition state. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

discharging/charging rates of the pristine electrode material.

### Summary and outlook

In conclusion, the atomic and electronic structures as well as the electrochemical properties of light-metal based  $\text{LiAl}(\text{NH}_2)_4$  and its modified compounds as conversion electrode materials for sodium-ion batteries have been detailedly investigated through DFT calculations. It is found that this material system (especially the derivative  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  compound) has proper potential for conversion-type electrode applications for sodium storage, which possesses a theoretical specific capacity of  $1249.57 \text{ mAh g}^{-1}$  and a low average voltage of  $0.087 \text{ V}$ . The diffusion of Na-ion can be evidently enhanced in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  compared with the pristine  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  whether at  $300 \text{ K}$  ( $9.167 \times 10^{-10} \text{ m}^2 \text{ s}^{-1}$  to  $3.250 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ ) or at  $400 \text{ K}$  ( $1.500 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$  to  $3.667 \times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ ), which implies the potential rate capability of electrode materials at room temperature as well as high temperature when  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  is modified by the boron element. Besides, the diffusion coefficients of Na-ion in  $\text{Li}_4\text{Al}_4(\text{N}_4\text{H}_8)_4$  and  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  have also been unveiled through *ab initio* molecular dynamics (AIMD). The lower kinetic barrier of  $0.31 \text{ eV}$  in  $\text{Li}_4\text{AlB}_3(\text{N}_4\text{H}_8)_4$  is very favorable for the migration of Na-ion. This quantum-mechanical based theoretical research will provide important clues for the new application of light-metal hydrides as conversion electrode materials in Na-ion batteries.

### CRediT authorship contribution statement

**Yingying Ren:** Methodology, Writing - original draft. **Xiaohan Ren:** Data curation. **Rajeev Ahuja:** Writing - review & editing. **Zhao Qian:** Conceptualization, Methodology, Writing - review & editing, Project administration, Funding acquisition, Conceptualization, Methodology, Writing - review & editing, Project administration, Funding acquisition.

### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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### Appendix A. Supplementary data

Supplementary data to this article can be found online at <https://doi.org/10.1016/j.rinp.2020.103408>.

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