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Persistent half-metallic ferromagnetism in a (111)-oriented manganite superlattice

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We employ electronic structure calculations to show that a (111)-oriented $(LaMnO_3)_{12}|(SrMnO_3)_6$ superlattice retains a half-metallic ferromagnetic character despite its large thickness. We link this behaviour to the strain and the octahedral connectivity between the layers. This also gives rise to breathing modes, which are coupled to charge and spin oscillations, whose components have a pure e_g character. Most interestingly, the magnetisation reaches its maximum value inside the LaMnO₃ region and not at the interface, which is fundamentally different from what observed for the (001) orientation. The inter-atomic exchange coupling shows that the magnetic order arises from the double-exchange mechanism, despite competing interactions inside the $SrMnO_3$ region. Finally, the van Vleck distortions and the spin oscillations are crucially affected by the variation of Hund's exchange and charge doping, which allows us to speculate that our system behaves as a Hund's metal, creating an interesting connection between manganites and nickelates.

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INTRODUCTION

Due to continuous advances in molecular beam epitaxy^{1,2} and pulsed laser deposition²⁻⁸, perovskites (and the more general Ruddlesden-Popper family, $A_{n+1}B_nO_{3n+1}$, where $n=\infty$ for perovskites) have been objects of undying attention in the scientific community⁹⁻¹¹. In the last years, this trend has been further accelerated by advances in defect engineering, which has improved the perspective of practical applications^{8,12}. Despite their apparent simplicity, bulk materials exhibit a variety of ground states, driven by the strong interplay of different degrees of freedom^{13–17}. The symmetry breaking at interfaces^{18–21} leads to even more exciting phenomena, such as flat bands²², anisotropic conductivity²³, magnetic anisotropy^{24,25}, exchange bias²⁶, spinglass²⁷, electronic quantum confinement^{28–30}, unconventional superconductivity³¹, topologically protected edge states^{32,33}, unexpected metallicity^{34–38} and tunable quantum phase transitions^{38–40}.

Much research on interfaces and surfaces has been focused on mixed-valence manganites. Bulk materials are primarily known for their colossal magnetoresistance⁴¹, which is favoured by a disordered solid mixture of Mn⁺³ and Mn⁺⁴ ions^{42–44}. In superlattices, however, non trivial phenomena may be observed and ordered hetero-valent ions do not prevent the emergence of a large magnetoresistance⁴⁵. Particularly studied are (LaM nO_3 _n|(SrMnO₃)_m superlattices, where various magnetic and electronic ground states across the metal-insulator transition can be tuned $^{10,46-50}$. This is achieved by varying their period (n+m) or component ratio $(n/m)^{47,48,51}$, which is a way to modulate the tunnelling of e_q electrons across the interface⁴⁸; orbital⁵² and charge⁵³ order were also reported. More exotic phenomena, including correlated topological states, may be expected when passing from the (001) orientation to the (111) orientation, because of the large polarity and a peculiar symmetry-driven epitaxial strain^{54,55}. This is the reason why (111)-oriented superlattices remain under intense scrutiny, despite of the scarcity of suitable substrates and unfavourable thermodynamics^{55–57}.

In this context, the current article presents an ab-initio study on the structural, electronic and magnetic properties of a (111)-oriented (LaMnO₃)₁₂|(SrMnO₃)₆ superlattice as illustrated in Fig. 1(a), which is isostochiometric to the colossal magnetoresistive La_{2/3}Sr_{1/3}MnO₃. Our calculations will show that this superlattice has a half-metallic ferromagnetic (FM) ground state, whose character persists inside the innermost layers of the component regions. This behaviour is profoundly different from what reported for other orientations and is traced back to the cooperation of charge transfer across the interface, strain, structural distortions and electronic correlations. Magnetism will be shown to originate from a double-exchange interaction between the Mn atoms and to be pinned inside the LaMnO₃ region and not at the interface. Finally, the Mott-Hund character of the electronic correlations will also be analysed.

RESULTS AND DISCUSSION

Ground-state structure and spectral properties

The $(LaMnO_3)_{12}|(SrMnO_3)_6$ superlattice is investigated via density functional theory (DFT) plus Hubbard U approach, labelled as sDFT+U. While tilting systems and angles are known for many perovskites in the bulk, their determination at surfaces and interfaces is not trivial. A previous ab-initio study⁵⁴ predicted that (111)-oriented manganite superlattices should adopt the $a^-a^-a^-$ tilting system instead of the native $a^-a^-c^+$ tilting system, as expressed in Glazer notation⁵⁸, used throughout this paper. The energy difference between these two structures depends on the lattice parameters. With a lattice constant of 3.860 Å (hereby denoted as equilibrium or 0% strain), the $a^-a^-c^+$ tilting system is favoured by 7.6 meV per formula unit (f.u., i.e., a AMnO₃ unit, where A may be La or Sr) with respect to the $a^-a^-a^-$ tilting system. A reasonably small compressive strain may change this structural order, as recently

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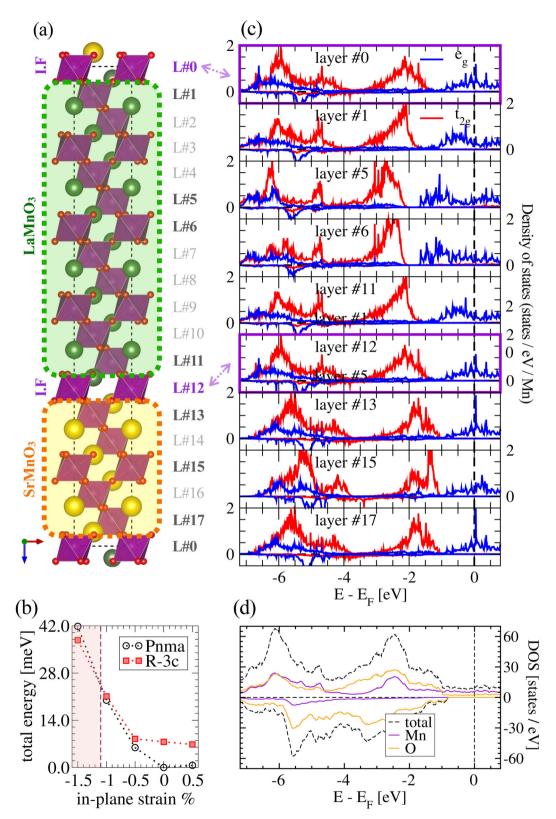


Fig. 1 Overview of the superlattice and its properties. a Crystal structure of the superlattice. The interfacial layers are #0 and #12. **b** Curve total energy vs strain for FM solutions with $a^-a^-c^+$ (black) and $a^-a^-a^-$ (red); `zero' strain means that the pseudo-cubic lattice constant is 3.860 Å. **c** Projected DOS for Mn- t_{2g} and Mn- e_g states for selected layers; additional information, covering all Mn and O layers, is provided in the Supplemental Material. **d** Total, Mn-d projected and O-p projected DOS for the FM solution.

Table 1. Energy difference per formula unit relative to the ground state structure – i.e., the FM phase with the $a^-a^-c^+$ tilting system – of various magnetic orders and tilting systems. The energies are computed for the same in-plane lattice parameters, corresponding to 0% strain.

| | $a^-a^-c^+$ | a ⁻ a ⁻ a |
|--|-------------|---------------------------------|
| FM | G. S. | 7.6 |
| A-type AFM | 26.5 | 37.5 |
| C-type AFM | 43.7 | 53.8 |
| A-type AFM C-type AFM G-type AFM | 71.8 | 95.6 |
| | | |

reported for nickelates⁵⁹. As shown in Fig. 1(b), we predict a transition to the $a^-a^-a^-$ tilting system for a compressive strain of ~ 1.5 %, corresponding to epitaxial growth on SrMnO₃ (on LaAlO₃ the strain is~2%). The energy difference between the two tilting systems remains below 7 meV (~80 K) at all simulated strain values, whereas that between the ground state FM and anti-ferromagnetic (AFM) orders are larger than 25 meV (~290 K), see Table 1. Therefore, phase transitions and coexistence are more likely to occur in the structure than in the magnetic order.

The two tilting systems do not lead to qualitatively different results in terms of distribution of charges and magnetic moments, but the $a^-a^-c^+$ requires a large supercell, which may hinder a thorough analysis of the layer-resolved properties. Therefore, we focus on the $a^-a^-a^-$ tilting system at the equilibrium lattice constant, for simplicity.

The superlattice analysed has a half-metallic character, as inferred by the total density of electronic states (DOS) in Fig. 1(d), with a band-gap in the minority-spin channel between Mn-d and O-p of ~2.0 eV. The site-projected DOS in Fig. 1(c) reveals that the half-metallicity persists across all the layers. The curves show that the deeper the Mn inside the LaMnO3 region, the lower the onset of the e_g bands, because of the larger electronegativity of La with respect to Sr. The smooth variation of these onsets across the superlattice is a further signature of metallicity. Moreover, the e_g states are well separated from the t_{2g} states in the LaMnO3 region (see layers 5 and 6), whereas they are much closer in the SrMnO3 region. Their separation is small also at the interface, note the larger upshift of the t_{2g} states with respect to the e_g states in Fig. 1(b).

The features just outlined are unusual for manganite superlattices with this large thickness. For the (001) orientation, the superlattice becomes insulating if LaMnO₃ is thicker than 2 layers 48,53,60 , whereas it is 12-layers thick in the present case. To understand the difference between the two orientations we should first understand what drives the formation of a half-metallic FM state. We recall that bulk LaMnO₃ (characterised by the $a^-a^-c^+$ tilting system) becomes half-metallic FM under a small compressive strain 61,62 . As discussed above, SrMnO₃ causes a small compressive strain on LaMnO₃, and this should be sufficient to induce the transition. Interestingly, this situation is even more favourable in the $a^-a^-a^-$ tilting system, which is predicted by our calculations to be a FM half-metal for all in-plane lattice parameters hereby considered.

Once established that strain is the driving factor in determining the half-metallic FM state in the $LaMnO_3$ region, we need to understand why this state is more likely to survive in the (111)-oriented superlattice than in its (001)-oriented counterpart. Clarifying this issue requires a deeper analysis of the structural features and the magnetic properties, presented in the next sections.

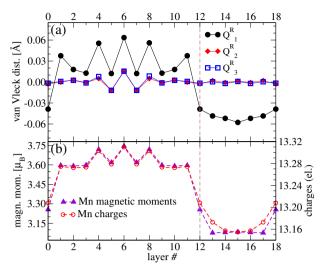


Fig. 2 Correlation between distortions and charge. a Layer-resolved van Vleck distortions. **b** Mn-projected Bader charges and magnetic moments. The dashed vertical line indicates the interfacial layer. The charge transfer across the interface is visible in having Bader charges larger (lower) than for the nominal oxidation state, i.e., 13 (14) in the SrMnO3 (LaMnO3) region. A more direct visualisation of the structure with respect to the layers numbering is provided in Fig. 1.

Breathing distortions and spin-charge oscillations

As for most perovskites, the structural features are linked to the electronic and magnetic properties. In agreement with leading literature^{63,64}, we introduce the Jahn-Teller distortions and breathing distortions in terms of the variations of the octahedral lengths x,y,z (with respect to their average values). Breathing distortions are defined as $Q_1^R = (\Delta x + \Delta y + \Delta z)/\sqrt{3}$, whereas the are $Q_2^R = (\Delta x - \Delta y)/\sqrt{2}$ Jahn-Teller distortions $Q_3^R = (-\Delta x - \Delta y + 2\Delta z)/\sqrt{6}$. Breathing distortions are seldom found in manganites, which host orbital order and Jahn-Teller distortions (also defined in the Methods) instead. A recent study highlighted that Jahn-Teller modes arise from a steric effect that affects the electron-lattice coupling and are therefore dependent on the tilting system^{65,66}. In the bulk, the constraint imposed by the $R\overline{3}c$ phase should lead to a total quenching of these (pseudo) Jahn-Teller modes. The Jahn-Teller distortions are shown in Fig. 2 (a) and are quenched in agreement with the aforementioned literature. The guenching is not full because the relaxation of the superlattice modifies the pristine $a^-a^-a^-$ tilting pattern.

The quenching of the Jahn-Teller modes is accompanied by the presence of the breathing modes. The latter are lessened by a factor 4 in the structure without tilts (data not shown). A similar relation between octahedral tilts and breathing distortions was recently found in rare-earth nickelates, where it leads to a structurally triggered metal-insulator transition⁶⁷. In addition, LaMnO₃ is mentioned as a case where a close competition between charge and orbital order is driven by a similar mechanism (in line with refs. 63 and 68). In the superlattice under investigation, this mechanism has to compete with the high stability of the FM half-metallic phase, associated to the strained structure, and with the uniform shift of the band-edge, induced by the charge transfer - see again Fig. 1(b). Therefore, it becomes unfavourable to induce a transition to an AFM insulator with orbital order. The site-projected charge and magnetic moment distributions, as computed à la Bader^{69–73}, is presented in Fig. 2(b) and shows a hint of charge order, leading to oscillations in the LaMnO₃ region and a smooth behaviour in the SrMnO₃ region.

The smooth variation of the Mn-O-Mn angles across the superlattice (which take approximately the same values for all

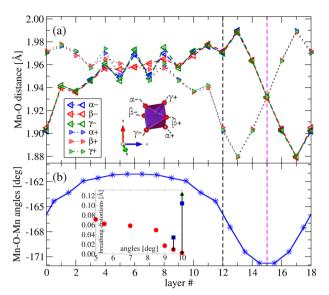


Fig. 3 Correlation between angles and distances/distortions. a Mn-O distance for the 3 inequivalent nearest neighbours, as illustrated in the inset; + and - denote increasing and decreasing c_i respectively. **b** Opposite of the Mn-O-Mn angles (MnOMn) averaged over the three directions; inset: correlation between the angles (π MnOMn)/2 and the breathing distortions. In the main panels, the vertical dashed black line denotes the laver at the interface, while the dashed magenta line denotes the center of the SrMnO₃ region. Note that layers #0 and #18 are also at the interface. In the inset of panel (b), the vertical lines denote the range of breathing distortions for one corresponding value of the angle.

layers in the central LaMnO₃ region) mirrors the uniform shift of the band-edge, compare Figs. 3(b) and 1(b), whereas the Mn-O distances appear with oscillations in the inner LaMnO₃ region, see Fig. 3(a). Where the Mn-O-Mn bond are closer to a flat angle (the SrMnO₃ region) the structure presents larger splitting in the Mn-O distances between increasing \hat{z} and decreasing \hat{z} , and where the Mn-O-Mn bonds are more bent (the LaMnO₃ region) the structure presents oscillating Mn-O distances and breathing modes, see Figs. 2, 3. In fact, the connection between breathing distortions and angles is even more apparent in the inset of Fig. 3(b), where flat angles correspond to single values for the MnO₆ volumes (breathing distortion) and bent angles - in the LaMnO₃ region correspond to large variance of the MnO₆ volumes distribution, in line with the above mentioned literature⁶⁷. The large Mn-O distance splitting, occurring in the SrMnO₃ region, reveals a typical tendency for SrMnO₃ to ferroelasticity⁷⁴, avoided by the symmetry with respect to the interface.

Exchange couplings and ferromagnetic order

As we argued that the magnetism is a consequence of structure and strain, we do not expect it to be interfacially driven. This is clearly visible in Fig. 2(b), where the largest magnetisation is found in the innermost layers of the LaMnO₃ region. For a better insight into the magnetic properties, we analyse the inter-atomic exchange coupling, computed for a lattice constant of 3.892 Å (which corresponds to a tensile strain below 1%). The largest contributions in the Mn sublattice are those connecting a Mn atom to its first nearest neighbours or fourth-nearest neighbours. The latter correspond to the second-nearest neighbours along Mn-O-Mn-··· lines, consistently with the double-exchange mechanism^{48,60}. The relevant exchange couplings across the superlattice are illustrated in Fig. 4. In the LaMnO₃ region, the magnetic order is driven by the FM nearest neighbour coupling, which in the innermost layer takes the value of 17.7 meV

and sharply decreases at the interface, exhibiting oscillations in phase with the magnetic moments. Interestingly, the maximum value is not reached at the innermost layer, but at intermediate layers, and amounts to 18.4 meV, which is 30% smaller than in the isostochiometric La_{2/3}Sr_{1/3}MnO₃⁷⁵. This behaviour reflects a competition between the trend of the magnetisation - see Fig. 2(b) – and the potential induced by the charge transfer across the interface – see Fig. 1(b). Such relatively strong ferromagnetism is even more surprising if compared to the behaviour of (001)oriented supercells, whose nearest neighbour exchange becomes bulk-like AFM for LaMnO₃ regions thicker than 2 unit cells^{48,60}. A smaller contribution to the magnetic order is given by the fourthnearest neighbour exchange, whose values are noticeable at the interface (1.36 meV), but are totally guenched in the innermost layers of the LaMnO₃ region.

The situation is more complicated in the SrMnO₃ region. In the innermost layers, the nearest neighbour exchange is AFM, as in the bulk⁷⁶. However, The strength of the coupling is much weaker than in the bulk, i.e., -1.6 meV versus -7.5 meV⁷⁷, due to the combined effect of charge transfer and epitaxial strain (about 1%). Strain alone was shown to induce an AFM-FM transition at about 3% in bulk cubic SrMnO₃⁷⁷ – while here the strain is virtually null on SrMnO₃. Interestingly, the FM order inside the SrMnO₃ region is stabilised by the fourth-nearest neighbour coupling, which becomes even larger (1.8 meV) than the nearest neighbour one. This frustration due to competing FM and AFM interactions is likely to lead to a more complex magnetic structure, probably accompanied by non-collinearity. Exploring the magnetic phase diagram may be an interesting project, but outside the scope of the present work. We prefer, instead, to focus on the origin of the oscillations of charge, magnetic moments, exchange couplings and breathing distortions.

We can summarise what leads to the half-metallic FM state with the help of Fig. 5. In the bulk, LaMnO₃ and SrMnO₃ behave as an AFM Mott insulator with Mn3+ ions and an AFM band insulator with Mn⁺⁴ ions, respectively. In the superlattice, the local strain in the LaMnO₃ region induces the delocalisation of the Mn-3d states, which in turn suppresses the AFM super-exchange and favours the FM double-exchange^{60,61}. This effect is further enhanced by the charge transfer across the interface, which penalises the ionic picture and promotes the hopping between Mn sites. In (001)oriented superlattices, the local strain is imposed in-plane - hence along two crystallographic directions - and allows different relaxations in different regions: SrMnO₃ recovers its G-type AFM order, blocking the tunnelling of e_q electrons from LaMnO₃ and imposing a strong penalty on the double-exchange mechanism. For the (111) orientation, the strain acts on the same footing for all octahedral axes, and therefore the aforementioned phase separation is forbidden, the e_a tunnelling survives and the FM coupling prevails. In summary, geometrical degrees of freedom affect the electronic ones, governing the magnetic and metallic properties of the superlattice. Further information can be inferred by the analysis of the bond angles, shown in Fig. 3. In the LaMnO₃ region, the Mn-O-Mn angles vary from 160° to 165°. These values are higher than the bulk LaMnO₃⁷⁸ value of 155° and close to the La_{2/} ₃Sr_{1/3}MnO₃ value⁷⁹ of 165°. The analysis of the Mn-O bond lengths, see Fig. 3, is in line with the presence of breathing modes in the LaMnO₃, but also with a tendency to ferroelasticity in SrMnO₃, avoided by the equivalence of the interfaces. Such behaviour is typical of SrMnO₃⁷⁴. Charge doping and metallicity would anyway prevent the transition to a ferroelectric phase.

Role of Hund's coupling

The suppression of Jahn-Teller order in favour of breathing distortions was predicted a decade ago in nickelates as a consequence of Hund's coupling and was pointed out to be persistent well into the metallic side of the Mott transition⁸⁰.

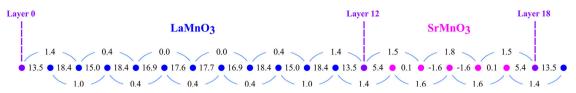


Fig. 4 Magnetic coupling constants as computed and shown along the (001) – or any of the equivalent (010) and (100) – crystallographic directions of the superlattice. The Mn are shown as circles, and the values of the coupling constants are reported in meV. Straight segments denote first nearest neighbours, whereas semicircles denote fourth-nearest neighbours, namely Mn two layers away but along the same Mn-O-Mn direction (whereas they vanish for all other Mn couples).

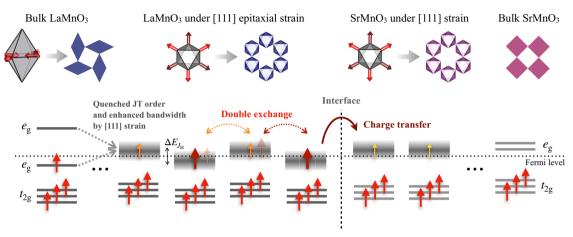


Fig. 5 Sketch of the physical mechanisms driving the interface behaviour in the superlattice. Bulk LaMnO₃ (left side) is an AFM Mott insulator with Jahn-Teller distortion and orbital order, in a d^4 ionic configuration. Bulk SrMnO₃ (right side) is an AFM band insulator in a d^3 configuration. Across the interface, charge transfer and epitaxial strain lead to partially filled bands and breathing distortions, while the Jahn-Teller order is quenched. Metallicity favours the FM order driven by the double-exchange mechanism, and in turn accompanied by spin and charge oscillations.

Later studies⁶⁷ pointed to structural distortions as the driving mechanism. In the present case, we observe an intermediate situation. On one hand, the structure has a primary importance, forbidding certain distortions, such as Jahn-Teller, and preserving metallicity. On the other hand, the breathing distortions are not large enough to induce a metal-insulator transition, but we still observe signs of charge order. The dependence of our results on the strength of Hund's exchange J is investigated via charge density functional plus U scheme (denoted as cDFT+U|J hereafter)81,82 for a lattice constant of 3.892 Å. It suggests to what extent Hund's coupling affects the properties of our system. The oscillations of the magnetic moments across the superlattice depend crucially on the value of Hund's coupling, see Fig. 6(b). When J becomes as small as 0.6 eV, the magnetism is no longer pinned at the innermost layers of the LaMnO₃ region. Instead, it becomes pinned at the interface, similarly to what happens in (001)-oriented superlattices. The change in the trend of the magnetic moments across the superlattice is accompanied by an analogous change of the breathing distortions, emphasising that the former drives the latter, to a large extent. Furthermore, electron/hole doping may lead to the disappearance of the breathing distortions as well as the magnetic moments oscillations (data not shown). Such a drastic change is surprising, considering the shape of the density of states in the corresponding doping range (\pm 0.1 eV), and suggests that strong electronic correlations play an important role. Overall, the metallic character with spin and charge oscillations, the presence of strong correlation effects, and the key role of the Hund's exchange J suggest that our superlattice behaves as a Hund's metal^{83,84}. Using our parameters U and J, as well as the effective bandwidth extracted from the DOS, we can obtain some information from existing phase diagrams of the Hubbard model^{85–87}. The most accurate comparison is offered by ref. 87, where Merkel et al. investigated

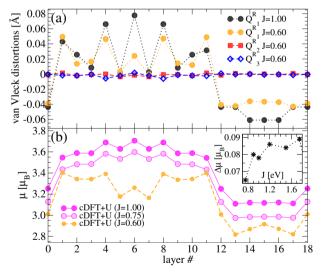


Fig. 6 Dependence of the distortions and charge/spin distribution on the correlation. a Layer-resolved van Vleck distortions and (b) Mn-projected Bader magnetic moments for different values of Hund's exchange J (in eV). See the Methods section for details on cDFT+U|J and sDFT+U|J. Inset: difference $\Delta\mu$ between the magnetic moments at layers #5 and #6, which provides a measure of the amplitude of the moment oscillations.

a 5 orbital system with a d^4 occupation, including the level splittings associated to the presence of breathing modes (representative of CaFeO₃). Using their phase diagram, we can confirm the regime of (homogeneous) Hund's metallicity, with an



estimated quasiparticle weight between 0.4 and 0.6. By increasing *J*, we expect to get closer to a valence skipping metal phase, which finds correspondence in an increasing amplitude of charge and spin oscillations (see inset of Fig. 6(b)). A further increase of *J* would lead to a charge disproportionated insulator, which in ref. ⁸⁷ is predicted to happen for values larger than 2.3 eV. Despite signs of "Hundness" have been found in a variety of systems during the last decade^{83,84}, they had never been reported for a manganite superlattice. For a more quantitative analysis allowing for more precise conclusions, one would need to perform calculations beyond DFT, e.g., in combination with the dynamical mean-field theory (DMFT), including the structural response. Considering the size of the system as well as the very high number of degrees of freedom, such an analysis would be beyond the scope of the present study.

Outlook

In summary, we have investigated the electronic and magnetic properties of the (111)-oriented (LaMnO₃)₁₂|(SrMnO₃)₆ superlattice using DFT+U|J. A half-metallic FM state is supported by the cooperation of charge, spin, orbital and lattice degrees of freedom, and is favoured with respect to an AFM state. The halfmetallic FM character is found to persist across the entire superlattice, while the innermost layers of its (001)-oriented counterpart become AFM insulators for a thickness larger than 3 layers. The atomic volumes, charges and magnetic moments are correlated across the superlattice, in particular in the LaMnO₃ region, where adjacent sites display charge, spin, and volume oscillations. Breathing distortions arise and may be accompanied by the quenching of Jahn-Teller distortions in the presence of $a^-a^-a^-$ tilting of MnO₆ octahedra while may coexist with the Jahn-Teller distortions in other tilting systems such as $a^-a^-c^+$. Overall, the present results suggest that the [111] epitaxial strain associated to the superlattice formation is a viable pathway to engineer a system analogous to La_{2/3}Sr_{1/3}MnO₃ without introducing doping-induced disorder. This is not only an advantage for avoiding alloy-related problems, as e.g. cation disorder, but does also widen the potential of interfacial engineering in oxide heterostructures. Finally, we also speculate that the fascinating physics exhibited by this superlattice may arise from Hundness, alongside with structural aspects, similarly to what happens in nickelates. Therefore, the system addressed here can provide further theoretical ground for the development of heterostructures hosting exotic magnetic phases and topological states.

METHODS

Framework and parameters

The superlattice is fully relaxed with an optimised lattice constant of $3.860\,\mathrm{\AA}$ (denoted as equilibrium or $0\,\%$ strain). Calculations are performed in density functional theory (DFT) using the projector-augmented wave method as implemented in the Vienna Ab-initio Simulation Package (VASP)88,89. The exchange-correlation functional is treated in the generalised gradient approximation (GGA) by Perdew-Burke-Ernzerhof 90,91. To improve the description of the Mn-3d states⁹², we make use of on-site corrections for static correlation effects in the rotational invariant DFT+U approach by Liechtenstein et al.93, denoted as sDFT+U|J. Further calculations to analyse Hund's coupling are performed by following the approach discussed in ref. 94, which we label as cDFT+U|J. The Coulomb interaction parameters are chosen as U = 3.8 eV and J = 1.0 eV, in accordance with works on similar systems^{95,96}. A deeper analysis of the magnetic properties is then performed via the full-potential linear muffintin orbital (FP-LMTO) method as implemented in the RSPt code⁹⁷⁻ used also the SCAN parameter-free functional 100: results (shown in the Supplemental Material) confirm the core results obtained with DFT+U|J.

The inter-atomic exchange interactions J_{ij} are calculated by mapping the magnetic excitations onto an effective Heisenberg Hamiltonian $\hat{H} = -\sum_{i \neq j} J_{ij} \cdot (\overrightarrow{e_i} \cdot \overrightarrow{e_j})$, where i, j are atomic sites and $\overrightarrow{e_i}$, $\overrightarrow{e_j}$ are unit vectors along the local magnetisation direction. This calculation is performed

via the magnetic force theorem, using the implementation of ref. ¹⁰¹, which was also successfully applied to CaMnO3²¹. Due to the better accuracy of all-electron methods¹⁰², these calculations also serve to confirm the validity of VASP results.

General considerations on the modelled system

The supercells used for the calculations consist of two types: the $R\overline{3}c$ cell was used for the results presented throughout this work, whereas an orthorhombic cell was used for calculations to compare total energies and results on the charge and spin distributions. The two interfaces have the same stacking sequence (i.e., LaO₃|Mn|SrO₃ or SrO₃|Mn|LaO₃), thus they are equivalent; furthermore, the superlattice possess inversion symmetry with respect to the Mn atom at the interface and therefore there is no built-in electric field generated. Further details on the cells and the sampling of the Brillouin zones are given in the Supplemental Material.

The analysis on the on-site charges and magnetic moments is carried on by in agreement with state-of-the-art methods^{69–73}. The analysis of the electronic properties is performed with the aid of the post-processing code VASPKIT¹⁰³. Finally, images of structures and charge/spin distributions are produced with VESTA JP-Minerals¹⁰⁴. Further details on the calculations are given in the Supplemental Material.

DATA AVAILABILITY

The datasets generated during and/or analysed during the current study are available from the first author on reasonable request.

CODE AVAILABILITY

The calculations for this work have been performed with VASP and RSPt. The former is a licence product from the University of Vienna; the licence can be obtained upon submitting an application through the vasp portal (http://www.vasp.at). The latter is a free software distributed under GPL license after registration to a mailing list. More information about RSPt can be found at http://fplmto-rspt.org/⁹⁸.

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AUTHOR CONTRIBUTIONS

F. C. planned the project and performed all the VASP calculations. I. D. M. performed all the RSPt calculations. F. C. and I. D. M. wrote the initial paper. All authors contributed to analysing the data, revising the paper and drawing the conclusions

COMPETING INTERESTS

The authors declare no competing interests.

ADDITIONAL INFORMATION

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