

# Excited-State (Anti)Aromaticity Explains Why Azulene Disobeys Kasha's Rule

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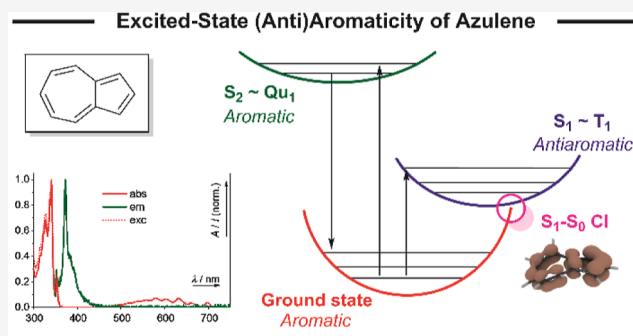
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**ABSTRACT:** Fluorescence exclusively occurs from the lowest excited state of a given multiplicity according to Kasha's rule. However, this rule is not obeyed by a handful of anti-Kasha fluorophores whose underlying mechanism is still understood merely on a phenomenological basis. This lack of understanding prevents the rational design and property-tuning of anti-Kasha fluorophores. Here, we propose a model explaining the photophysical properties of an archetypal anti-Kasha fluorophore, azulene, based on its ground- and excited-state (anti)aromaticity. We derived our model from a detailed analysis of the electronic structure of the ground singlet, first excited triplet, and quintet states and of the first and second excited singlet states using the perturbational molecular orbital theory and quantum-chemical aromaticity indices. Our model reveals that the anti-Kasha properties of azulene and its derivatives result from (i) the contrasting (anti)aromaticity of its first and second singlet excited states ( $S_1$  and  $S_2$ , respectively) and (ii) an easily accessible antiaromaticity relief pathway of the  $S_1$  state. This explanation of the fundamental cause of anti-Kasha behavior may pave the way for new classes of anti-Kasha fluorophores and materials with long-lived, high-energy excited states.



## 1. INTRODUCTION

In 1959, Michael Kasha postulated that, in single molecules, “the emitting level of a given multiplicity is the lowest excited level of that multiplicity”.<sup>1</sup> Since then, however, Kasha's rule has been broken by a number of molecules known as anti-Kasha (also non-Kasha) fluorophores.<sup>2–4</sup> Among them, one fluorophore stands out for exclusively emitting from the second singlet excited state ( $S_2$ ) as the archetype of anti-Kasha fluorophores, azulene.<sup>5</sup>

Azulene's anti-Kasha behavior is particularly robust under structural perturbations. Binsch et al. tried to quell the anti-Kasha properties of azulene through multiple synthetic strategies, including annellation, symmetry lowering, substitution by heavy atoms, and addition of a “loose bolt” substituent (Figure 1A), albeit to no avail.<sup>6</sup> All approaches failed to induce the first singlet excited state ( $S_1$ ) emission of the azulene derivatives.

Based on Longuet-Higgins and Beer's hypothesis according to which the anomalous emission of azulene results from its large  $S_2$ – $S_1$  gap ( $\sim 14,000$   $\text{cm}^{-1}$ ),<sup>5</sup> Murata et al. followed a more systematic approach to reduce the  $S_2$ – $S_1$  gap by extensive substitution of the azulene scaffold (Figure 1B).<sup>7</sup> They were able to increase the rate of  $S_2$ – $S_1$  internal conversion, thereby reducing the quantum yield of the  $S_2$  emission. Yet, even in later studies, despite the increased IC rate, no  $S_1$  emission was observed in any azulene derivative at room temperature.<sup>8–15</sup>

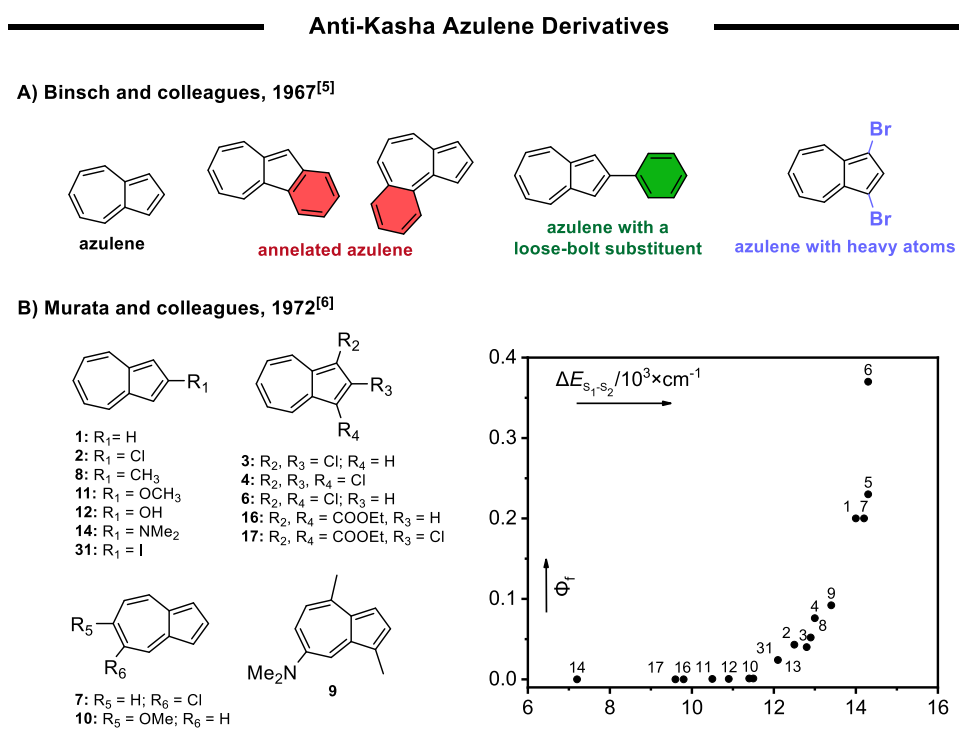
The anomalous photophysical properties of azulene and its derivatives prompted further research efforts to uncover their underlying mechanism, leading to the following, now well-established explanations: (i) the large  $S_2$ – $S_1$  gap of azulene results in a low rate of IC from  $S_2$ , which in turn leads to a high yield of  $S_2$  emission,<sup>5,7,10</sup> and (ii) the  $S_1$  of azulene rapidly decays by a  $S_1$ – $S_0$  conical intersection,<sup>18</sup> located near the  $S_1$  minimum energy geometry, thereby accounting for the absence of  $S_1$  emission. Notwithstanding these efforts, no structure–property relationship was provided to explain the anti-Kasha behavior of azulene. In fact, the description of azulene's anti-Kasha behavior has long remained insufficient to guide any attempt at rational molecular design and anti-Kasha property tuning, a shortcoming that we shall overcome herein.

Azulene is a  $10\pi$ -aromatic fused bicyclic hydrocarbon with no substituents or heteroatoms; therefore, its photophysical phenomena must be a manifestation of its  $\pi$ -electron configuration. Cyclic,  $\pi$ -conjugated molecules can be described as aromatic or antiaromatic in their ground and excited

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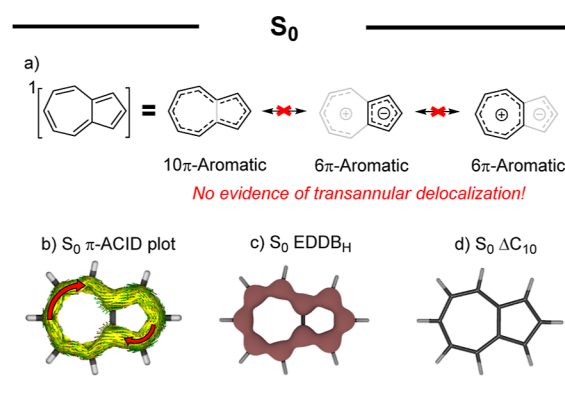
**Figure 1.** Examples of anti-Kasha azulene derivatives: (A) substituent effects explored by Binsch et al.,<sup>6</sup> (B) derivatives (numbered as in the original publication) explored by Murata et al. (left) and a plot of fluorescence quantum yields as a function of  $S_1-S_2$  gap (right).<sup>7</sup>

states.<sup>19–24</sup> Among other characteristics, these descriptors indicate whether their  $\pi$ -electron configuration in a given electronic state is stabilizing or destabilizing, respectively. Accordingly, we hypothesized that the anti-Kasha behavior of azulene could be related to the (anti)aromatic character of  $S_1$  and  $S_2$ . Such a relationship between excited-state (anti)aromaticity and anti-Kasha behavior may explain how the electronic structure of azulene leads to its anti-Kasha behavior, thus providing key mechanistic insights into anti-Kasha fluorophores.

## 2. RESULTS AND DISCUSSION

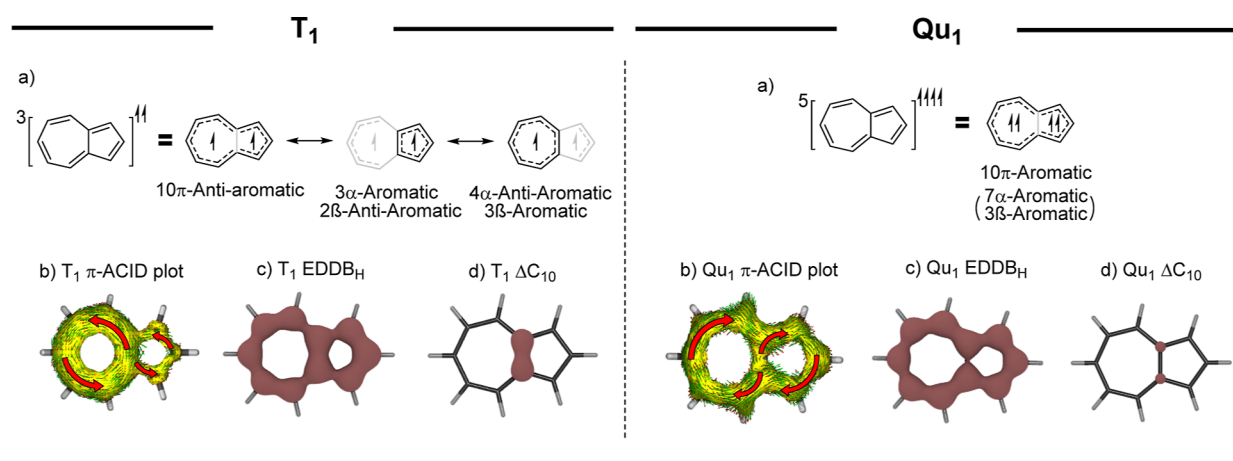
To understand how the electronic structure of azulene leads to its anti-Kasha behavior, we analyzed its ground- and excited-state (anti)aromaticity in increasing order of complexity. The ground singlet state ( $S_0$ ) and first-excited triplet state ( $T_1$ ) of small conjugated cyclic hydrocarbons typically show contrasting aromaticity/antiaromaticity, as per Hückel's and Baird's rules.<sup>20</sup> Moreover, the aromaticity of the first excited quintet state ( $Q_{U1}$ ) of azulene has been previously reported.<sup>25,26</sup> Hence, we computationally investigated the  $S_0$ ,  $T_1$ , and  $Q_{U1}$  to model the (anti)aromatic character of azulene in the lowest states of each multiplicity. Subsequently, we compared their electronic structures and various aromaticity indices (Section S5) with those of  $S_1$  and  $S_2$ , which account for the anti-Kasha behavior of azulene. This approach enabled us to establish the relationship between the anti-Kasha behavior of azulene and its excited-state (anti)aromaticity.

Ground state azulene is a Hückel  $10\pi$ -aromatic molecule, as shown by all calculated aromaticity indices (Figure 2 and Chapter S5.1). Yet, only when comparing the calculated aromaticity indices of all possible delocalization circuits within its molecular geometry (Figure S6) do we find that the aromaticity of azulene originates from the delocalization along



**Figure 2.** Summary of the results of  $S_0$  azulene; (a) important resonance structures, (b)  $S_0$   $\pi$ -ACID plot (Figure S35), (c)  $S_0$  EDDB<sub>H</sub>, and (d) density of delocalized  $\pi$ -electrons in the transannular bond ( $\Delta C_{10}$ ), which corresponds to the density of 0.02 electrons (amounting to virtually no delocalization through the transannular bond).

its perimeter. The calculated delocalization indices [aromatic fluctuation (FLU), multicenter delocalization (MCI), and electron density of delocalized bonds (EDDB)] indicate (Table S1) that most of the delocalized  $10\pi$ -electron density is situated along the perimeter of azulene (cyclodecapentaenyl circuit). Conversely, delocalization circuits involving the transannular bond (cyclopentadienyl and cycloheptatrienyl) exhibit poor  $\pi$ -electron delocalization (Figure 2 and Table S1). By calculating EDDB<sub>p</sub> electron counts (Table S2), we quantified the electron delocalization within the transannular bond of azulene ( $\Delta C_{10}$ ). This bond exhibited only a negligible contribution, 0.02 electrons, to the global delocalized electron density of azulene (Figure 2). The virtual absence of ground-



**Figure 3.** Summary of the results of  $T_1$  and  $Qu_1$  azulene; (a) most prevalent resonance structures, (b)  $\pi$ -ACID plots (Figures S36 and S37), (c) EDDB<sub>H</sub>, and (d) density of delocalized  $\pi$ -electrons in the transannular bond ( $\Delta C_{10}$ ).

state transannular delocalization in azulene corresponds to its unusually long transannular bond of approximately 1.5 Å.<sup>27</sup>

The  $10\pi$ -aromaticity of azulene was predicted in previous studies.<sup>26,28</sup> However, the relevance of this finding has been largely overlooked. For example, the permanent dipole moment of azulene is usually explained by resonance structures that invoke delocalization through the transannular bond,<sup>29</sup> but these resonance structures do not significantly contribute to the net electronic structure of azulene (Figure 2a), as evidenced by the negligible  $\Delta C_{10}$  value. As a case in point, we found that homoazulene,<sup>30</sup> the homoannulated counterpart of azulene without a conjugated transannular bond, has a similar permanent dipole moment (Chapter S13.1). Furthermore, in contrast to many other polycyclic aromatic hydrocarbons (PAH), such as the isoelectronic naphthalene (Chapter S13.2), which is known to favor the formation of multiple,  $6\pi$ -aromatic rings,<sup>31,32</sup> azulene's  $S_0$  electronic structure resembles a single  $10\pi$ -aromatic ring. Therefore, in the ground state, the bicyclic molecular geometry of azulene should be treated as a single  $10\pi$ -aromatic hydrocarbon rather than a PAH.

In the first triplet excited state, azulene follows Baird's rules<sup>19</sup> and is antiaromatic (Figure 3). This antiaromaticity is partly alleviated by transannular bond contraction. As a result, the delocalization decreases in the perimeter but increases in the cyclopentadienyl and cycloheptatrienyl circuits of azulene, as shown by our calculations (Table S5), and these circuits adopt the electronic structures of their corresponding cyclic radicals, as demonstrated by the EDDB (Chapter S12). The consequences of this enhanced geometric relaxation and the associated changes in the electronic structure of azulene can also be observed in the calculated isomerization stabilization energies (ISE) (Table S30), which are close to zero, or negative, for methylated isomers of  $T_1$  azulene. Despite the extensive reorganization and significant loss of antiaromaticity,  $T_1$  azulene remains, nevertheless, moderately antiaromatic.

The  $Qu_1$  of azulene has never been observed experimentally. However, previous theoretical studies have indicated that  $Qu_1$  azulene is aromatic.<sup>25,26</sup> Furthermore, our results showed that the aromaticity of  $Qu_1$  originates primarily from the delocalization along its perimeter (Figure 3 and Table S9). The contrasting preferred electronic structures of  $T_1$  and  $Qu_1$  azulene are supported by both the perturbational molecular orbital (PMO) theory<sup>28</sup> (Chapter S3.1.1) and Mandado's rules<sup>33</sup> (Chapter S3.1.2).

The concepts developed based on the  $S_0$ ,  $T_1$ , and  $Qu_1$  azulene enabled us to evaluate the aromaticity of azulene in  $S_1$  and  $S_2$  (Figure 4). The complete active space self-consistent field (CASSCF) aromaticity indices (Table S13) indicated that the  $S_1$  azulene is antiaromatic, whereas its  $S_2$  is aromatic.

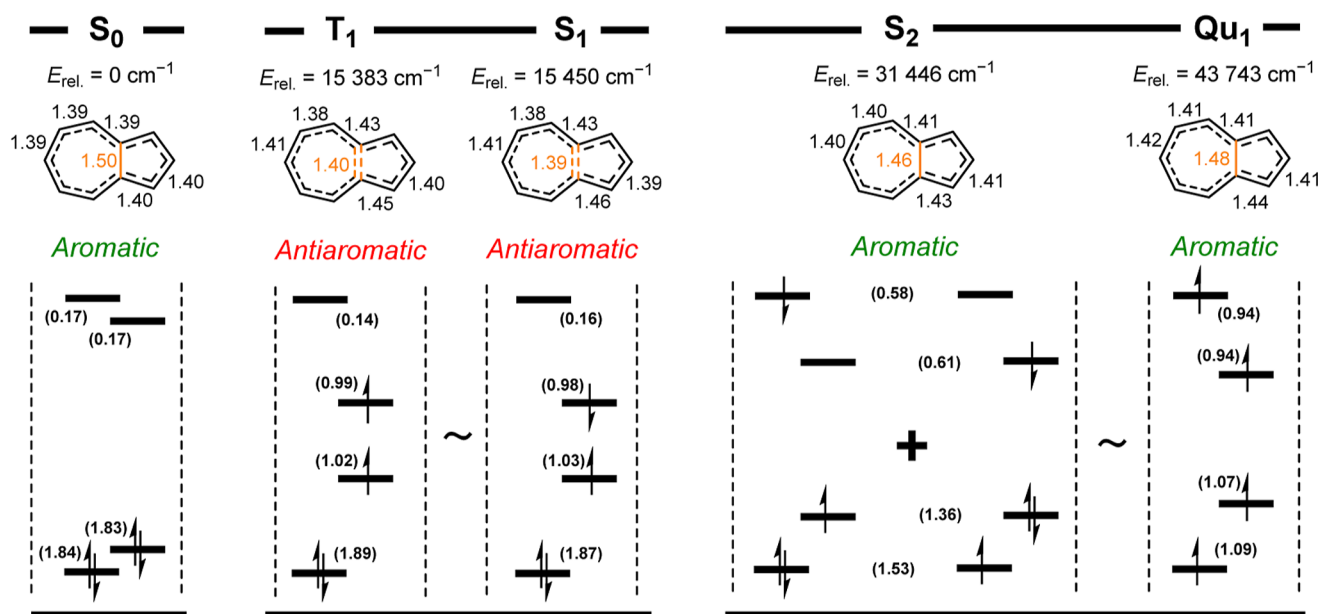
We investigated the (anti)aromaticity of  $S_1$  and  $S_2$  azulene further by calculating the magnetically induced current density (MICD) at the CASSCF(10,10) level.<sup>34,35</sup> We found that azulene in  $S_2$ , similarly to  $S_0$ , exhibited a diatropic ring current along its perimeter. Conversely, azulene in  $S_1$  exhibited a paratropic ring current, localized primarily within the cyclopentadienyl and cycloheptatrienyl circuits (Figure 4B). The polarity of the MICD confirmed the antiaromaticity of azulene in  $S_1$  and the aromaticity in  $S_2$ .

The  $S_1$  antiaromaticity of azulene followed Baird's rules. Although Baird's rules were originally formulated only for molecules in  $T_1$ ,<sup>19</sup> in many molecules, the rules can be applied to  $S_1$  as well.<sup>20</sup> The similarity between the  $S_1$  and  $T_1$  azulene is indicated by the calculated energies, minimum energy molecular geometries, aromaticity indices, and EDDB values (Figure 4 and Chapter S5.4).

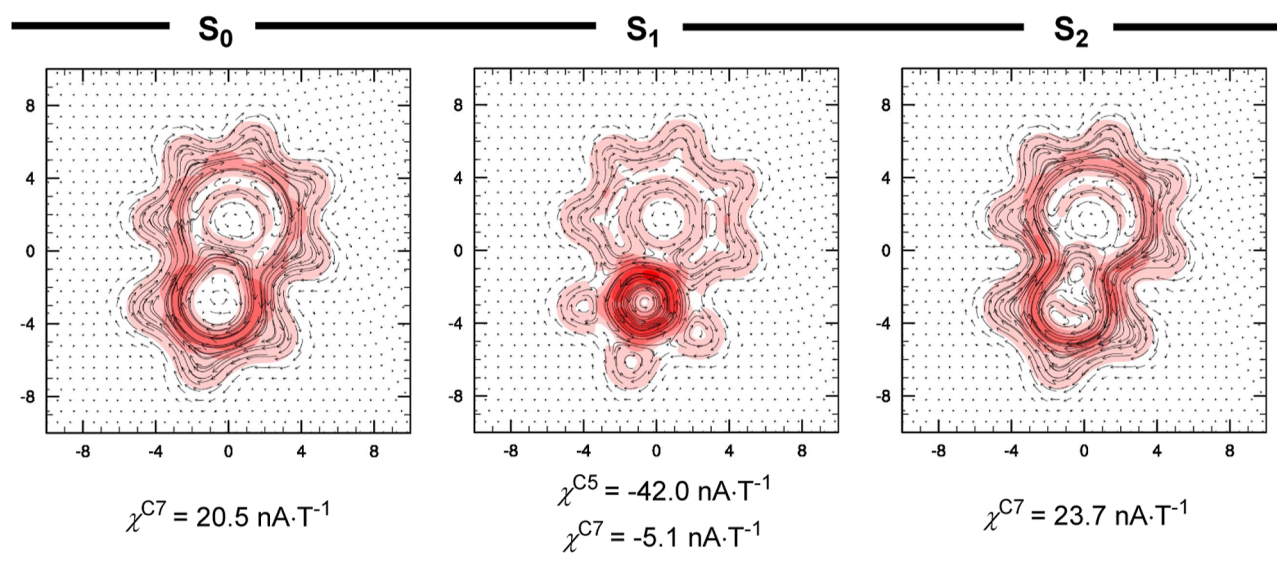
Our findings also explain the aromaticity of  $S_2$  azulene. The root-optimized CASSCF(10,10) wave function of  $S_2$  azulene has a significant multireference character (Figure 4 and Tables S18 and S19). The wave function attributed near-degenerate occupancy by unpaired electrons to HOMO - 1 and LUMO and to HOMO and LUMO + 1. This factor plays a key role in the  $S_2$  aromaticity of azulene. The multireference character of  $S_2$  azulene mimics the  $Qu_1$  state by adopting a similar normalized  $\pi$ -orbital occupancy, in a relationship not unlike  $S_1$ - $T_1$ . Consequently, the  $S_2$  and  $Qu_1$  states of azulene share a similar aromatic character.

In summary,  $S_1$  azulene is antiaromatic, and its geometry relaxes significantly to alleviate its antiaromaticity, whereas  $S_2$  azulene is aromatic, and its geometry does not relax significantly, thus preserving the energy gained upon excitation. Moreover, in antiaromatic  $S_1$ , azulene adopts a biradical electronic structure. The biradical electronic structure of  $S_1$  azulene leads to spatial segregation of its two unpaired electrons into  $\pi$  and  $\pi^*$  orbitals. Thus, in  $S_1$ , azulene's unpaired electrons exhibit low interelectron repulsion, which contributes to its low  $S_1$  energy (previously also described by Michl and Thulstrup).<sup>36</sup> In the aromatic  $S_2$ , conversely, the two unpaired electrons are delocalized within the azulene's perimeter circuit.

## A) Summary of CASSCF(10,10) results



## B) CASSCF(10,10) Magnetically induced current density

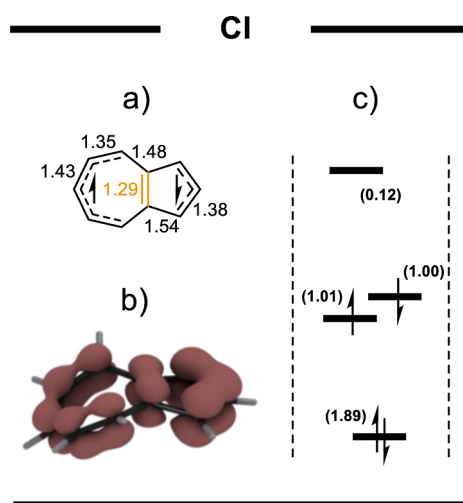


**Figure 4.** (A) Summary of calculated properties of the CASSCF(10,10) wave functions of the  $S_0$ ,  $S_1$ ,  $S_2$ ,  $T_1$ , and  $Qu_1$  of azulene, grouped by their shared aromaticity ( $S_1 \sim T_1$ ,  $S_2 \sim Qu_1$ ), including their (from top): relative energies in reference to the  $S_0$  ( $E_{rel.}$ ) which in case of  $S_1$  (318 nm) and  $S_2$  (647 nm) directly relate to the UV–vis absorption bands of azulene (see Figure 6B), bond lengths ( $C_{2v}$  symmetry), assigned aromatic character, canonicalized active-space natural MOs [reduced to (4,4) for clarity], their normalized occupancy (in brackets), and scheme of the dominant configuration(s). (B) CASSCF(10,10) MICD plot of azulene in  $S_0$ ,  $S_1$ , and  $S_2$ , constructed 1 au above the molecular plane (for full resolution plots, see Figures S38–S40), and the numerically integrated ring current susceptibilities of the cyclopentadienyl ( $\chi^{C5}$ ) and cycloheptatrienyl ( $\chi^{C7}$ ) rings (for integration planes, see Figure S7).

Accordingly, in  $S_2$  azulene, the unpaired electrons share a higher orbital overlap, resulting in higher interelectron repulsion. This contrast between the extent of geometric relaxation of azulene in  $S_1$  and  $S_2$  and the resulting difference in interelectron repulsion explains the large  $S_2$ – $S_1$  energy separation and, consequently, leads to a low rate of  $S_2$ – $S_1$  internal conversion (IC).

At this point, the absence of  $S_1$  emission caused by the depletion of  $S_1$  states via a  $S_1$ – $S_0$  conical intersection<sup>18</sup> remained unaddressed though. To account for this key feature of the anti-Kasha behavior of azulene, we optimized the  $S_1$ – $S_0$  conical intersection geometry and calculated the CASSCF aromaticity indices (Section S5.5), as previously performed for  $S_1$  and  $S_2$ . In the optimized conical intersection geometry,  $S_1$

azulene adopts the electronic structure of two acyclic radicals separated by a double bond (Figure 5), in turn increasing the



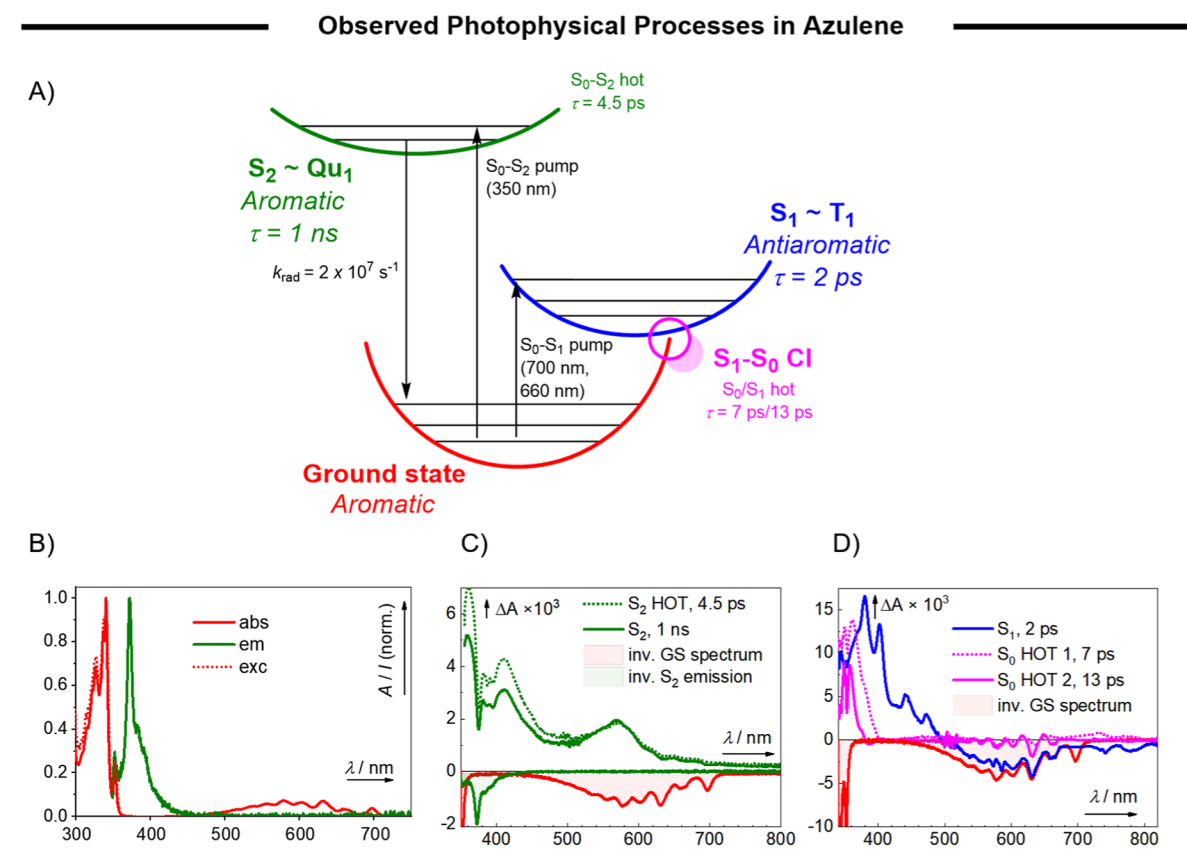
**Figure 5.** Summary of properties of the  $S_1$  CASSCF(10,10) wave functions of the  $S_1$ – $S_0$  conical intersection of azulene, calculated in the  $S_1$  state; (a) scheme of the proposed electronic structure and the bond lengths of CI azulene, (b)  $EDDB_H$  plot, (c) canonicalized active-space natural MOs [reduced to (4,4) for clarity], their normalized occupancy (in brackets), and scheme of the dominant configuration.

overall energy. This increase is offset by subsequent non-radiative transition to the aromatic ground state (Table S1). As suggested by canonicalized active-space natural MO's (Figure 5c), at the CI geometry, azulene exhibits low HOMO–LUMO separation. This low separation favors the pairing of its two unpaired electrons (in  $S_1$ ), thus providing a nonradiative pathway to  $S_0$ . Therefore, the conical intersection enables  $S_1$  antiaromaticity relief.

### 3. CONCLUSIONS

In conclusion, the (anti)aromaticity of the lowest three singlet states of azulene ( $S_0$ ,  $S_1$ , and  $S_2$ ) explains its anti-Kasha behavior. Azulene is aromatic in its ground state, antiaromatic in its  $S_1$ , and aromatic in the  $S_2$ . The (anti)aromaticity of each state matches its lifetime, as experimentally determined by transient absorption spectroscopy (Figure 6 and Chapter S11). Moreover, the  $S_1$  azulene's geometry relaxes significantly to alleviate its antiaromaticity. Consequently, the  $S_1$  minimum-energy geometry of azulene is found near a conical intersection.

In the antiaromatic,  $S_1$  minimum-energy geometry, azulene readily undergoes a favorable, nonradiative transition to its aromatic ground state through a conical intersection (Figure 6A). The depletion of  $S_1$  through the conical intersection provides unimolecular antiaromaticity relief. By contrast, the aromatic  $S_2$  is stabilized, does not undergo significant geometric relaxation, and maintains at high energy, which



**Figure 6.** (Anti)aromaticity of the lowest three singlet states of azulene ( $S_0$ ,  $S_1$ , and  $S_2$ ) explains its anti-Kasha behavior. (A) Jablonski diagram of the experimentally observed photophysical phenomena, (B) UV–vis absorption, emission ( $\lambda_{exc} = 338$  nm), and excitation spectra ( $\lambda_{em} = 372$  nm) of azulene, (C) species associated spectra (SAS) of azulene excited at 350 nm ( $E = 600$  nJ), and (D) SAS of azulene excited at 700 nm ( $E = 2$   $\mu$ J). All spectra were recorded in cyclohexane.

causes a low rate of  $S_2$ – $S_1$  IC. For this reason, the  $S_2$  state of azulene is long-lived and emitting, breaking Kasha's rule.

## 4. METHODS

Both PMO analysis<sup>28</sup> and Mandado's rules,<sup>33</sup> wherein  $\pi$ -electrons are separated by their spin ( $m$ ), were extensively used in this study and supported by quantum chemical calculations of delocalization and aromaticity indices. We calculated HOMA,<sup>37,38</sup> MCI,<sup>39</sup> and FLU<sup>40</sup> and  $I_{\text{ring}}^{\text{41}}$  indices for the  $C_5$ ,  $C_7$ , and  $C_{10}$  circuits (Figure S6); in both "net" and "spin-separated" formulations, for all above states. We used the EDDB scheme, which represents electron delocalization that cannot be assigned to atoms or bonds due to its (multicenter) delocalized nature, to integrate the number of globally (EDDB<sub>G</sub> and EDDB<sub>H</sub>) and locally (EDDB<sub>F</sub>, EDDB<sub>E</sub>, and EDDB<sub>P</sub>) delocalized  $\pi$ -electrons<sup>42,43</sup> and, in particular, the density of delocalized  $\pi$ -electrons in the transannular bond of azulene ( $\Delta C_{10}$ ). Note that the spin-separated values of each index can be interpreted in line with Mandado's rules in open-shell systems. We also calculated the NICS<sup>44</sup> at the centroid of  $C_5$  and  $C_7$  fragments and constructed ACID<sup>45</sup> plots of  $S_0$ ,  $T_1$ , and  $Q_{u1}$  azulene and MRSCF MICD at CASSCF(10,10) level for  $S_0$ ,  $S_1$ , and  $S_2$ .<sup>34,35</sup> ISE of methylated derivatives of  $S_0$  and  $T_1$  azulene were also calculated.<sup>46</sup> Full details on the computational methods and theoretical approach and the measured stationary absorption and emission and transient absorption spectra are provided in the Supporting Information.

## ■ ASSOCIATED CONTENT

### SI Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/jacs.3c07625>.

PMO theory and Mandado's rules, computational methods, ground and excited state aromaticity calculations,  $S_1$ – $S_0$  conical intersection, NICS, dipole moment, ISE, ACID, MICD calculations, absorption and emission spectroscopy, time-resolved spectroscopy, and azulene versus naphthalene and homoazulene (PDF) Optimized geometries (ZIP)

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## Author Contributions

All authors have given approval to the final version of the manuscript.

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## Notes

The authors declare no competing financial interest.

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