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A fermionic portal to a non-abelian dark sector

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We introduce a new class of renormalizable models for dark matter with a minimal particle content, consisting of a dark $SU(2)_D$ gauge sector connected to the standard model through a vector-like fermion mediator, not requiring a Higgs portal, in which a massive vector boson is the dark matter candidate. These models are labeled fermion portal vector dark matter (FPVDM). Multiple realizations are possible, depending on the properties of the vector-like partner and scalar potential. One example is discussed in detail. Fermion portal vector dark matter models have a large number of applications in collider and non-collider experiments, with their phenomenology depending on the mediator sector.

KEYWORDS

dark matter, large Hadron collider, vector-like fermions, dark gauge group, relic density, direct dark matter detection

The nature of DM, whose existence has been established beyond any reasonable doubt by several independent cosmological observations, is one of the greatest puzzles of contemporary particle physics. Models with a vector DM, especially in the non-abelian case, are the least explored but well-motivated, as the gauge principle offers guidance and constraints limiting the possible theoretical constructions (see, e.g., [1–26], for a discussion of non-abelian DM in different setups, in particular using non-renormalizable kinetic mixing terms or Higgs portal scenarios). In this article, we develop a new minimal framework that extends the gauge sector of the standard model (SM) by a new non-abelian gauge group for which no renormalizable kinetic mixing terms are allowed¹ and under which all SM particles are singlets. The full model structure, Lagrangian, and particle content are presented in the following sections, along with the main results and immediate prospects for experimental testing, while more technical details can be found in [27].

The simplest non-abelian group is $SU(2)$, which in the following will be labeled $SU(2)_D$ as it connects the SM to the dark sector. The gauge bosons associated with $SU(2)_D$ are labeled as $V_\mu^D = (V_{D+\mu}^0, V_{D0\mu}^0, V_{D-\mu}^0)$, where, here and in the following, the electric charge is specified in the field superscripts, while the isospin under $SU(2)_D$ (D-isospin) is specified in the field subscripts. The covariant derivative associated with $SU(2)_D$ is

¹ Contributions to gauge kinetic mixing may arise at the loop level, depending on the structure of the Higgs sector, but they correspond to suppressed higher operator terms.

$$D_\mu = \partial_\mu - \left(i \frac{g_D}{\sqrt{2}} V_{D\pm\mu}^0 T_D^\pm + i g_D V_{D0\mu}^0 T_{3D} \right), \quad (1)$$

where g_D is the $SU(2)_D$ coupling constant and T_{3D} is the D-isospin.

The fields responsible for breaking the gauge symmetries are two scalar doublets:

$$\begin{aligned} \Phi_H &= (\phi^+ \phi^0)^T \rightsquigarrow \langle \Phi_H \rangle = \frac{1}{\sqrt{2}} (0 \ v)^T, \\ \Phi_D &= (\varphi_{D+\frac{1}{2}}^0 \ \varphi_{D-\frac{1}{2}}^0)^T \rightsquigarrow \langle \Phi_D \rangle = \frac{1}{\sqrt{2}} (0 \ v_D)^T, \end{aligned} \quad (2)$$

where the first is breaking $SU(2)_L \times U(1)_Y$, while the second is breaking $SU(2)_D$ via their respective vacuum expectation values (VEVs) v and v_D .

The scalar potential for Φ_H and Φ_D reads

$$V(\Phi_H, \Phi_D) = -\mu^2 \Phi_H^\dagger \Phi_H - \mu_D^2 \Phi_D^\dagger \Phi_D + \lambda (\Phi_H^\dagger \Phi_H)^2 + \lambda_D (\Phi_D^\dagger \Phi_D)^2 + \lambda_{\Phi_H \Phi_D} \Phi_H^\dagger \Phi_H \Phi_D^\dagger \Phi_D, \quad (3)$$

which was introduced in [2] and ensures that the gauge bosons of $SU(2)_D$ are degenerate and stable because of the custodial symmetry of the scalar Lagrangian. Although the operator $\Phi_H^\dagger \Phi_H \Phi_D^\dagger \Phi_D$ is not protected by any symmetry and cannot thus be removed from the potential, coupling $\lambda_{\Phi_H \Phi_D}$ can have any value. If it is small enough, the dark sector would be effectively decoupled from the SM and only observable through gravitational effects. Moreover, the Higgs portal induces scalar mixing, which modifies Higgs–SM couplings and generates Higgs–DM interactions, all of which are strongly constrained [28]. Here, we suggest a different mechanism of communication between the dark and visible sectors via a fermion doublet $\Psi = (\psi_D \ \psi)$, vector-like (VL) under $SU(2)_D$, and both elements of which are singlets under $SU(2)_L$, sharing the same hypercharge as one of the SM right-handed fermions². The mass and Yukawa interaction terms of Ψ read

$$-\mathcal{L}_f = M_\Psi \bar{\Psi} \Psi + (y' \bar{\Psi}_L \Phi_D f_R^{\text{SM}} + h.c.), \quad (4)$$

where f_R^{SM} generically denotes an SM right-handed singlet and y' is a new Yukawa coupling connecting the SM fermion with $\Psi_L = \frac{(1-\gamma_5)}{2} \Psi$ through the Φ_D doublet. At this point, it would be possible to write an additional Yukawa term $y'' \bar{\Psi}_L \Phi_D^c f_R^{\text{SM}}$, which would violate the stability of DM due to the simultaneous mixing of ψ_D and ψ with SM fermions and would induce a direct coupling $V_{D\pm}^0 \bar{f}^{\text{SM}} f^{\text{SM}}$. The appearance of such y'' term and the respective stability of DM can be avoided by imposing an unbroken continuous global symmetry $U(1)_D \equiv e^{i\Lambda Y_D}$, unrelated to local $SU(2)_D$.

Without this symmetry, such a term would be compulsory since the scalar doublet, Φ_D , is in the pseudo-real representation. The symmetry-breaking pattern is $SU(2)_D \times U(1)_D \rightarrow U(1)_D^d$. With $U(1)_D$ phase assignments $Y_D = \frac{1}{2}$ for dark doublets and $Y_D = 0$ for triplets, there is still an invariance under the subgroup

TABLE 1 Quantum numbers of the new particles under the electro-weak (EW) and $SU(2)_D$ gauge groups.

	$SU(2)_L$	$U(1)_Y$	$SU(2)_D$	\mathbb{Z}_2
$\Phi_D = \begin{pmatrix} \varphi_{D+\frac{1}{2}}^0 \\ \varphi_{D-\frac{1}{2}}^0 \end{pmatrix}$	1	0	2	– +
$\Psi = \begin{pmatrix} \psi_D \\ \psi \end{pmatrix}$	1	Q	2	– +
$V_\mu^D = \begin{pmatrix} V_{D+\mu}^0 \\ V_{D0\mu}^0 \\ V_{D-\mu}^0 \end{pmatrix}$	1	0	3	– + –

The bold numbers correspond to the representation of the multiplets under SU_2 .

$\mathbb{Z}_2 \equiv (-1)^{Q_D}$, where $Q_D = T_D^3 + Y_D$. The new particles are summarized in Table 1.

The lightest \mathbb{Z}_2 -odd particle is stable and could be either $V_{D\pm}^0$ or ψ_D , with very different consequences from a cosmological point of view [27]. We consider the case where the lightest \mathbb{Z}_2 -odd particle is $V_{D\pm}^0$, which we label fermion portal vector dark matter (FPVDM). The theory contains six massive gauge bosons (Z , W^\pm , V_{D0}^0 , and $V_{D\pm}^0$), and therefore, six Goldstone bosons correspond to their longitudinal components. The remaining two degrees of freedom correspond to physical scalars, which include the SM Higgs boson and another CP-even scalar. By denoting the neutral scalars in terms of their components in the unitary gauge as $\phi^0 = \frac{1}{\sqrt{2}} (v + h_1)$ and $\varphi_{D-1/2}^0 = \frac{1}{\sqrt{2}} (v_D + \varphi_1)$, the mass terms of the scalar Lagrangian reads

$$\mathcal{L}_m^S = (h_1 \ \varphi_1) \begin{pmatrix} \lambda v^2 & \frac{\lambda_{\Phi_H \Phi_D}}{2} v v_D \\ \frac{\lambda_{\Phi_H \Phi_D}}{2} v v_D & \lambda_D v_D^2 \end{pmatrix} \begin{pmatrix} h_1 \\ \varphi_1 \end{pmatrix}. \quad (5)$$

Upon diagonalization, the mass eigenvalues read

$$m_{h,H}^2 = \lambda v^2 + \lambda_D v_D^2 \mp \sqrt{(\lambda_D v_D^2 - \lambda v^2)^2 + \lambda_{\Phi_H \Phi_D}^2 v^2 v_D^2}, \quad (6)$$

with the mixing angle $\sin \theta_S = \sqrt{2 \frac{m_H^2 v^2 \lambda - m_h^2 v_D^2 \lambda_D}{m_H^4 - m_h^4}}$.

In the fermion sector, the component with $T_{3D} = +1/2$ gets only a VL mass; therefore, $m_{\psi_D} = M_\Psi$. However, the other fermion masses are generated after both scalars acquire a VEV. The fermionic mass Lagrangian reads

$$\mathcal{L}_m^f = (\bar{f}_L^{\text{SM}} \ \bar{\Psi}_L) \begin{pmatrix} y \frac{v}{\sqrt{2}} & 0 \\ y' \frac{v_D}{\sqrt{2}} & M_\Psi \end{pmatrix} \begin{pmatrix} f_R^{\text{SM}} \\ \Psi_R \end{pmatrix}. \quad (7)$$

The mass eigenvalues are

$$m_{f,F}^2 = \frac{1}{4} \left[\Delta \mp \sqrt{\Delta^2 - 8 y^2 v^2 M_\Psi^2} \right], \quad (8)$$

where $\Delta = y^2 v^2 + y'^2 v_D^2 + 2M_\Psi^2$, f identifies the SM fermion, and F identifies its heavier partner. The mass hierarchy is $m_f < m_{\psi_D} \leq m_F$.

The Yukawa couplings and mixings can be expressed in terms of the masses of the physical fermions. The new fermion sector is completely decoupled in the limit $m_F = m_{\psi_D}$, for which $y = y_{\text{SM}}$ and $y' = 0$. When the full flavor structure of the SM is taken into consideration, different possibilities can be considered. A VL fermion can interact with one or more SM flavors, and there can

² VL portals have also been explored in [29, 30], but for scalar DM candidates, and in [26, 31] for vector dark matter, but with either the simplifying assumptions of setting the new Yukawa coupling to zero [31] or with a much larger, hence non-minimal, particle content [26].

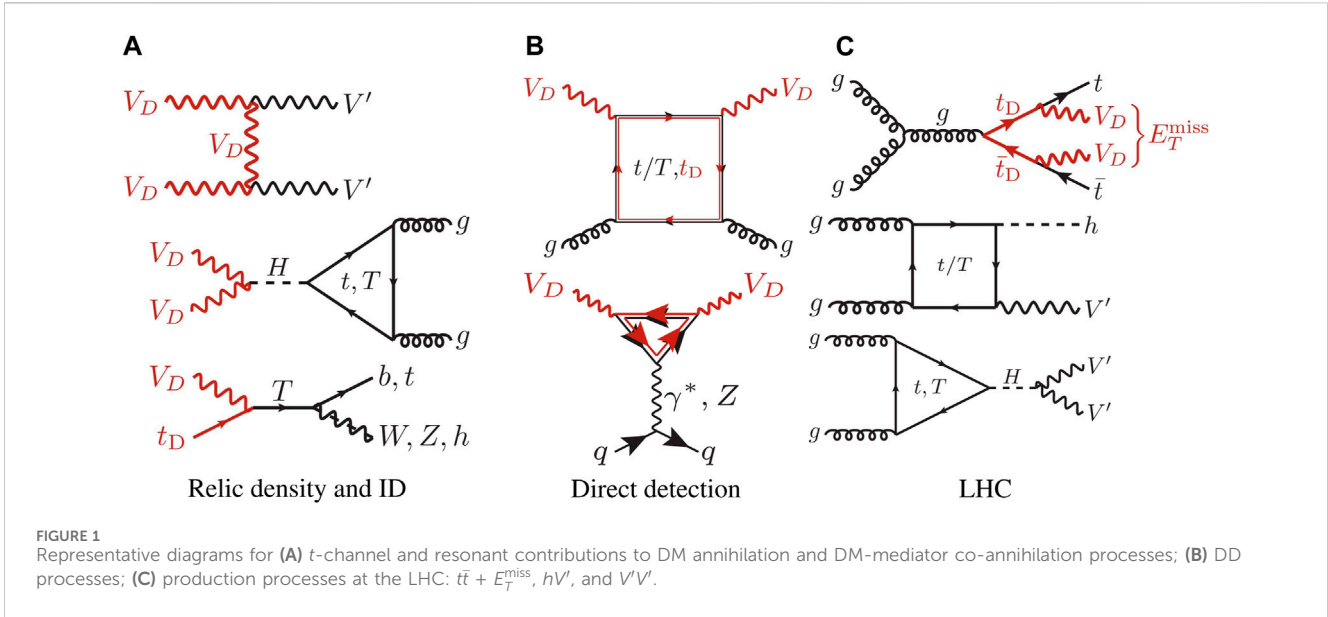


FIGURE 1 Representative diagrams for (A) t -channel and resonant contributions to DM annihilation and DM-mediator co-annihilation processes; (B) DD processes; (C) production processes at the LHC: $t\bar{t} + E_T^{\text{miss}}$, hV' , and $V'V'$.

be multiple VL fermions. The Cabibbo–Kobayashi–Maskawa (CKM) matrix of the SM might also receive contributions from new physics induced by the mixing of SM and VL quarks.

The masses of the SM gauge bosons are not altered by the presence of Φ_D . The gauge bosons of $SU(2)_D$ are all degenerate in mass at the tree level: $m_{V_D} \equiv m_{V_{D\pm}} = m_{V_{D0}} = \frac{g_D}{2} v_D$. This degeneracy is broken by kinetic mixing in the broken EW and dark gauge symmetry phases and by the different fermionic loop corrections associated with the opposite \mathbb{Z}_2 parities of the $SU(2)_D$ gauge bosons. Such different contributions might also affect loop corrections to Z and W masses, addressing the CDF anomaly [32]. In the following, to simplify notation, we will label $V_D \equiv V_{D\pm}^0$, with mass m_{V_D} , and $V' \equiv V_{D0}^0$, with mass $m_{V'}$. The leading contribution to the radiative mass split of V' and V_D bosons, $\Delta m_V = m_{V_D} - m_{V'}$, is determined by F and ψ_D loops and reads

$$\Delta m_V = \frac{\epsilon^2 g_D^2 m_F^2}{32\pi^2 m_{V_D}} + o(\epsilon^2), \quad \text{where } \epsilon = \frac{m_F^2 - m_{\psi_D}^2}{m_F^2}. \quad (9)$$

In the following, we assume that new VL fermions interact only with one flavor of the SM. Six independent input parameters are thus necessary to describe the new physics sector of the model, namely, $g_D, m_{V_D}, m_H, m_F = m_T$, and $m_{\psi_D} = m_{t_D}$.

Let us now discuss a specific realization of the model, assuming only one VL partner interacting exclusively with the SM top quark and no mixing between h and H , i.e., $\theta_S = 0$. This choice significantly simplifies the Lagrangian: the Higgs sector of the SM is not affected by the new physics at the tree level, and the potential of Φ_D has the very same structure as the Higgs potential. A mixing between h and H is induced only by fermionic loops and will be neglected in the following. Therefore, in this case, the model is described by the following five parameters: $g_D, m_{V_D}, m_H, m_F = m_T$, and $m_{\psi_D} = m_{t_D}$.

The hierarchy between the masses in the fermion sector is $m_t < m_{t_D} \leq m_T$, while H can have any mass allowed by experimental bounds, even being lighter than the SM Higgs boson.

In our study, we tested this realization of the model against multiple observables from cosmology, DM direct, and indirect

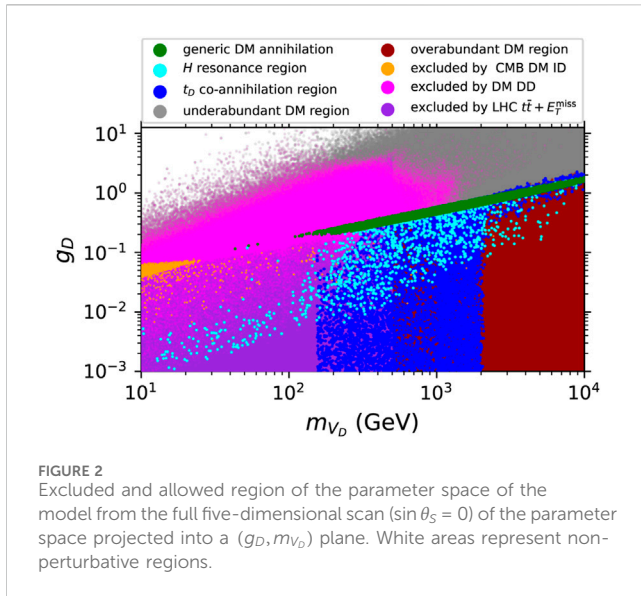
detection (DD and ID) experiments and LHC searches. For this purpose, the Lagrangian has been implemented in LanHEP [33] and FeynRules [34], while model files have been generated in CalcHEP [35], UFO [36], as well as FeynArts [37] formats and are available on the HEPMDB [38]. This implementation has been used in micrOMEGAS v5.2.7 [39] for the evaluation of various DM observables and for extracting the respective limits. The model implementation in UFO format has been used in MG5_AMC [40] for the determination of the LHC constraints. Collider simulations have been performed at LO using the NNPDF3.0 LO set [41] through the LHAPDF6 library [42] (LHA index 262400). A simplified version of the model has been implemented to calculate cross-sections at one loop in MG5_AMC and FORMCALC9.8 [43].

The amount of relic density is determined by the interplay of annihilation and co-annihilation processes, a subset of which is shown in Figure 1A. ID constraints are associated with DM annihilation rates at CMB time, excluding regions of parameter space where the injection into SM-plasma in the early universe is too large to be consistent with CMB data. Both the relic density and ID processes are tested against PLANCK data [44]. DD processes arise from diagrams such as those shown in Figure 1B and are tested against limits from XENON 1T [45].

The LHC bound has been obtained via testing of t_D pair production with subsequent decay into V_D and top quarks against CMS searches for top squark pair production decaying into DM [46]. The relevant limit from $T\bar{T}$ of even partners of the SM top quark from the respective ATLAS and CMS searches is approximately 1.5 TeV for m_T [47, 48]. Single T production is less constrained, as it is driven by the small $T - t$ mixing.

We also estimated the relevance of V' pair production and associate production of V' with the Higgs boson, occurring at LO via fermion loops. Representative topologies for the tested processes are shown in Figure 1C.

The complementarity of cosmological and collider constraints has been studied by performing a comprehensive scan over the parameter space (excluding the fixed parameter $\sin \theta_S = 0$) projected onto the (g_D, m_{V_D}) plane, as shown in Figure 2. The allowed



parameter space is indicated by the green, cyan, and blue regions, presenting generic DM annihilation, dominated by the t-channel diagram of Figure 1A, resonance (H) and DM- t_D co-annihilation regions, respectively, which satisfy the relic density constraint from PLANCK within 5%. The allowed regions of the parameter space are superimposed on top of the forbidden ones to provide their best visualization in this projection of the five-dimensional scan into the two-dimensional plane.

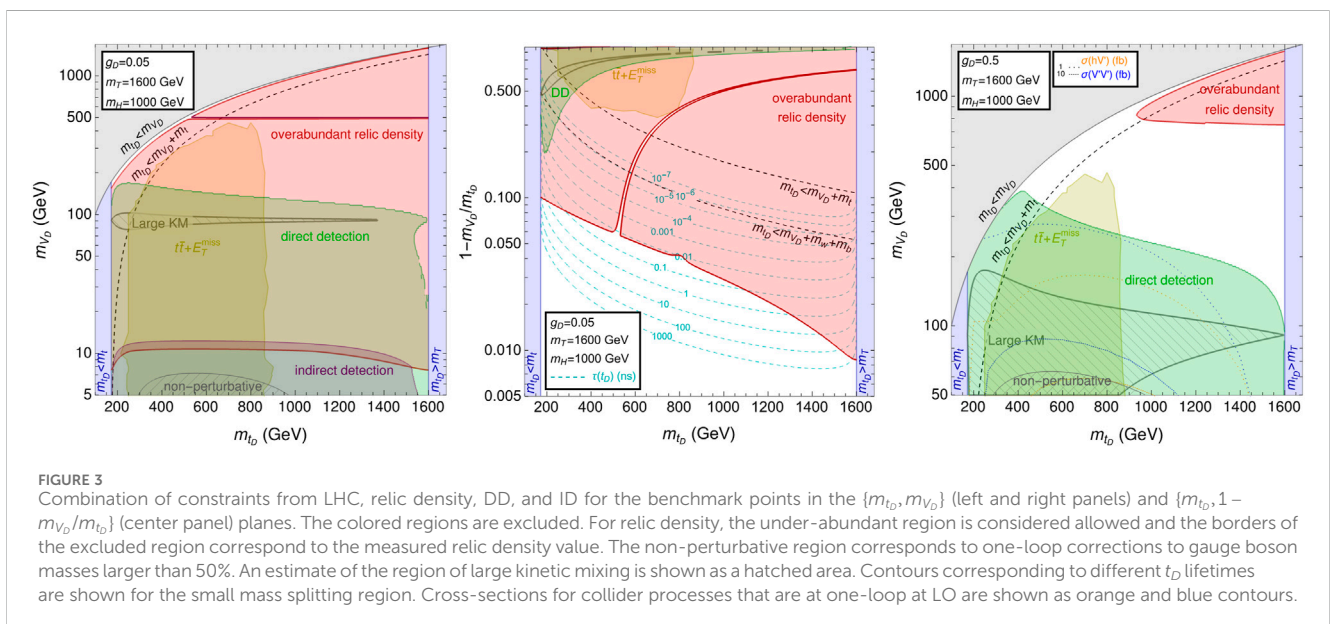
The generic DM annihilation determines a lower limit on g_D as a function of m_{V_D} . At the same time, the H -resonant region allows for the reduction of g_D values by up to two orders of magnitude, while the strong DM- t_D co-annihilation channel allows for even lower values of g_D for not-so-heavy DM. For m_{V_D} above 2 TeV, however, the co-annihilation mechanism saturates, while H -resonant annihilation requires larger g_D coupling for higher DM mass to

provide the right amount of relic density. Therefore, the region with $m_{V_D} \geq 1$ TeV has an over-abundant relic density, as indicated by the dark red color, except the space with large values of g_D couplings, corresponding to the bulk $V_D V_D \rightarrow V' V'$ annihilation and H -resonant annihilation presented in Figure 2 by green and light-blue colors, respectively. Notice also that the regions with $m_{V_D} \leq 1$ TeV values are partly excluded by DD and/or ID experiments, as indicated by magenta and orange points, respectively. The region of DM masses that can be tested and excluded by the LHC is $m_{V_D} \leq 400$ GeV, represented by the violet region.

To assess the relative role of the different constraints, we identify representative benchmarks characterized by different gauge couplings, $g_D = 0.05$ and $g_D = 0.5$, and fixed values for the masses, $m_T = 1,600$ GeV and $m_H = 1,000$ GeV. For these points, gauge coupling is small enough to allow a perturbative treatment in a region of parameter space, which can be tested by both collider and cosmological observables.

We show in Figure 3 the exclusion regions in the $\{m_{t_D}, m_{V_D}\}$ and $\{m_{t_D}, 1 - m_{V_D}/m_{t_D}\}$ planes to highlight the low m_{V_D} or low $m_{t_D} - m_{V_D}$ regions, respectively. The masses of the DM candidate V_D and mediator t_D are left as free parameters.

The predicted relic density is consistent with PLANCK results only in specific regions: for $g_D = 0.05$ (left and central panels of Figure 3), most of the parameter space predicts an over-abundant relic density, except for an area where the mass difference between t_D and DM is less than $\sim 10\%$ of the mediator mass (where t_D - t_D and DM- t_D co-annihilation processes dominate), a small area around $m_{V_D} = m_H/2$ (DM annihilation via resonant H), and $m_{V_D} \leq 10$ GeV. For larger values of g_D (right panel of Figure 3), annihilation processes become more effective, reducing the size of the excluded area in the lower m_{V_D} region and eventually extending the under-abundant relic density region. The enhancement of the $V_D V_D \rightarrow V' V'$ process, due to $\Delta m_V > 0$, affects the relic density and ID signals. The complementarity of various constraints is especially evident for small values of g_D in the low m_{V_D} region. The region excluded by ID corresponds to small values of m_{V_D} for $g_D = 0.05$,



largely overlapping with the region excluded by relic density, and rapidly vanishes as g_D increases. The large region excluded by DD is mainly determined by processes (see Figure 1B) with sizable kinetic mixing or DM multipole moment contributions, taking place in the regions with low m_{V_D} values (i.e., below few hundreds GeV).

The LHC bound is almost independent of the mass of t_D until its mass difference with the DM reaches the top-quark threshold: in that region, E_T^{miss} decreases and the sensitivity of the CMS search reduces, allowing a small mass-gap region. As the process is QCD-initiated, the bound is also almost independent of other parameters of the model. Processes of V' pair production and associated production of V' with the Higgs boson would only be potentially testable in a region already excluded by DD constraints (see orange and blue contours in the right panel of Figure 3). The model has an important feature, especially for small values of g_D in the small DM- t_D mass-gap region where the correct relic density is reproduced. In this region, t_D is long-lived (its lifetime in the small mass-gap region is shown in the central panel, Figure 3³) and can be probed by dedicated searches at the LHC or future colliders. Different T or H masses would not modify this qualitative picture.

The FPVDM scenario introduced in this paper connects a vectorial DM candidate from a non-abelian $SU(2)_D$ gauge group to the fermionic sector of the SM without the necessity of a Higgs portal at the tree level, and the mechanism is realized in the most economical way, with a minimal set of new parameters and new particles. Even the simplest realization of FPVDM, involving interactions of the dark sector with only one SM fermion, has great potential to explain DM phenomena and has several important implications for collider and non-collider DM searches. Minimal FPVDM realizations involving other SM fermions can be used to explain outstandingly observed anomalies. For example, if the VL fermion interacts with the leptonic sector of the SM, new contributions might explain $(g - 2)_\mu$ [49] and, at the same time, provide novel physics cases for future e^+e^- colliders [50–53]. Non-minimal realizations, including mixing in the scalar sector, further VL partners, or additional interactions of the same VL representation, would open up a vast range of possibilities for future studies, both phenomenological and experimental, and would allow one to explore the complementarity between collider and non-collider observables in multiple scenarios.

Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

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Author contributions

AB: writing–original draft and investigation. LP: writing–original draft and investigation. AD: writing–original draft and investigation. SM: writing–original draft and investigation. DR: writing–original draft and investigation. NT: investigation and writing–original draft.

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Conflict of interest

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