



















# 1. Introduction

We live in a world that is ruled by particles and their interactions. There are electrons, quarks, neutrinos and all other particles that together form the plethora of particles described by the standard model. For our everyday life however, the most important particles are the electrons. Together with the protons and neutrons, the electrons form the foundation of all elements of the Periodic Table. It is the electrons and their interactions that determine how molecules are formed from atoms and how atoms are combined to form solids. Within the field of materials physics the aim is to be able to understand the properties of various kinds of materials, from the atomic level to the condensed forms of the crystalline solids and the liquid state.

This thesis deals with a theoretical description based on first principles theory of issues regarding chemical bonding, structure and stability of materials that are of great interest, both from a scientific point of view and from an industrial perspective. To a great extent this thesis is concerned with the properties of transition metal carbides. For a long time these materials have been the focus of extensive research due to their many interesting physical properties and they are nowadays used in many technological applications. One example of such an application is as hard metal coatings on various components. Coatings are regularly used to protect surfaces in order to prolong different components life time. A bad or not well adapted coating material can severely shorten the life time, whereby a lot of attention has been given to investigations on how to design new coating materials with better functionality. As a part of this thesis an approach on how it is possible to design coating materials based on the transition metal carbides will be presented.

A traditional crystalline solid is an arrangement of atoms in some sort of lattice. This is in principle a homogeneous ordering with identical lattice positions where atoms occupy the different lattice sites. Nowadays, experimenters are able to manufacture superstructures in various forms. One example of such a structure is a multilayered material where different types of materials are grown on top of each other in a layered manner. These types of materials possess new properties and functionality, an example of which are the giant magneto resistance (GMR) effect for which Albert Fert and Peter Grünberg were awarded the Nobel Prize in Physics in 2007.

Theoretical investigations have always played a crucial role in the understanding of the physical world. The aim is here to obtain a description of all particles and how they interact by knowing only the number of particles and by

basing the description on fundamental laws of nature, i.e. from first principles or *ab initio*. For a solid or a liquid system it is very complicated to theoretically model and calculate different physical properties in such a way. This is due to the vast number of particles which constitute these many body systems. In order to obtain some useful information it is necessary to make a series of approximations and to setup elaborate models. In this work the density functional theory[1, 2] developed by Walter Kohn and co-workers has been used to calculate various materials properties. In essence the density functional theory converts the problem of many interacting particles and transforms it into a one particle problem which is much easier to solve. Various implementations of density functional theory are today among the most commonly used methods to perform calculations of the electronic structure of materials.

This thesis is divided into two parts. Part I is devoted to the theories of matter that have been used extensively in the research that is contained within this thesis. This part is not material specific and the discussion can be applied to any material of interest. In Part II there is a summary of the results presented in the attached papers which form the basis of this thesis, along with additional discussions concerning the properties of transition metal carbides and multilayered structures. Much of the work presented in this thesis has been performed in parallel with experimental investigations and this will be reflected when it comes to the discussion of the obtained results. However, the experimental techniques that have been used will not be described in any detail. For further details regarding the results the reader is directed to the original papers which are attached at the end of the thesis.

Part I:

Theory of the solid state



## 2. Introduction to the many body problem

In the solid state there are atoms which have condensed to form crystals out of free atoms. In free atoms the electrons move about the nucleus in atomic-like electron orbitals. In the condensed state these electrons begin to interact in between different atoms to form energy bands. The electronic structure in materials, which is the result of bringing atoms together, is what determines all materials properties. In this chapter we will discuss some of the theories and approximations that underlie the theoretical treatment of solid state systems.

The many body problem in condensed matter systems is of great importance, both when it comes to a complete understanding of the fundamental properties of these systems and to the understanding of materials for applications. Furthermore, it is one of the hardest problems to deal with, since the number of interacting particles is very large ( $\sim 10^{23}$ ). To solve the problem as it is presented is analytically impossible and numerically intractable even when using top-of-the-line algorithms and computers. It is therefore imperative to make approximations in order to solve the problem at hand within a reasonable time.

The fundamental problem in condensed matter physics is the solution of the time-independent Schrödinger equation

$$\hat{H}\Psi = E\Psi, \quad (2.1)$$

where  $\Psi$  is the many particle wave function,  $E$  is the energy of the system, and  $\hat{H}$  is the Hamiltonian given by

$$\hat{H} = -\frac{\hbar^2}{2M_N} \sum_{I=1}^{N_N} \nabla_I^2 - \frac{\hbar^2}{2m_e} \sum_{i=1}^{N_e} \nabla_i^2 + V(\{\mathbf{R}_I\}, \{\mathbf{r}_i\}),^1 \quad (2.2)$$

where  $M_N$  is the mass of the nuclei,  $m_e$  the electron mass,  $N_N$  the number of nuclei,  $N_e$  the number of electrons, and  $V(\{\mathbf{R}_I\}, \{\mathbf{r}_i\})$  is the potential describing all interactions between electrons and nuclei, and  $\hbar$  is Planck's constant. The potential is given by the sum of three different contributions:

$$V(\{\mathbf{R}_I\}, \{\mathbf{r}_i\}) = V_{NN}(\{\mathbf{R}_I\}) + V_{ee}(\{\mathbf{r}_i\}) + V_{Ne}(\{\mathbf{R}_I\}, \{\mathbf{r}_i\}), \quad (2.3)$$

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<sup>1</sup>  $\{\mathbf{R}_I\}$  and  $\{\mathbf{r}_i\}$  are the positions of all nuclei and electrons respectively.

where

$$V_{NN}(\{\mathbf{R}_I\}) = \frac{e^2}{8\pi\epsilon_0} \sum_{I \neq J} \frac{Z_I Z_J}{|\mathbf{R}_I - \mathbf{R}_J|} \quad (2.4)$$

is the interaction between different nuclei,<sup>2</sup>

$$V_{ee}(\{\mathbf{r}_i\}) = \frac{e^2}{8\pi\epsilon_0} \sum_{i \neq j} \frac{1}{|\mathbf{r}_i - \mathbf{r}_j|} \quad (2.5)$$

is the electron-electron interaction, and

$$V_{Ne}(\{\mathbf{R}_I\}, \{\mathbf{r}_i\}) = -\frac{e^2}{4\pi\epsilon_0} \sum_{I,j} \frac{Z_I}{|\mathbf{R}_I - \mathbf{r}_j|} \quad (2.6)$$

is the electron-nuclei interaction.

To solve the problem presented in Eq. (2.1) for all particles in a solid is a very difficult task and one has to resort to approximations in order to manage it (the only problem that is solvable without approximations is in fact the hydrogen atom which can be solved analytically). In what follows a number of approximations will be given that are commonly used in the theory of the solid state.

## 2.1 The Born-Oppenheimer approximation

The Born-Oppenheimer or adiabatic approximation [3] is based on the fact that when considering the electronic structure, it is possible to neglect the kinetic energy of the nuclei in Eq. (2.2), since this term can be considered as small in relation to the other terms. This approximation relies on the fact that the mass of the nuclei is much larger than the mass of the electrons,  $M_N \gg m_e$ . It may therefore be assumed, since the nuclei move so slowly compared to the electrons, that the electrons will move in an external potential from a static configuration of nuclei. It is therefore possible to formulate a Hamiltonian describing the electronic system as

$$\hat{H}_{el} = \hat{T} + \hat{V}_{ext} + \hat{V}_{int}, \quad (2.7)$$

where

$$\hat{T} = -\frac{\hbar^2}{2m_e} \sum_{i=1}^{N_e} \nabla_i^2 \quad (2.8)$$

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<sup>2</sup> $e$  is the elementary charge,  $Z_I$  is the atomic number, and  $\epsilon_0$  is the electric constant.

is the kinetic energy operator for the electrons,

$$\hat{V}_{ext} = V_{Ne} = \sum_{I,j} V_I(|\mathbf{R}_I - \mathbf{r}_j|) \quad (2.9)$$

is the external potential acting on the electrons due to the nuclei, and

$$\hat{V}_{int} = V_{ee} \quad (2.10)$$

is the internal potential describing the interaction between the electrons in the system. The electronic problem can now be solved via

$$\hat{H}_{el}\Psi_{el} = E_{el}\Psi_{el}.^3 \quad (2.11)$$

The total energy of the system (electrons and nuclei),  $E_{tot}$ , can then be found as

$$E_{tot} = E_{el} + E_{II}, \quad (2.12)$$

where  $E_{II}$  is the energy contribution from a static configuration of nuclei that can be solved once and for all for a specific structure. We note that the interaction energy between the nuclei comes into the electronic problem as an additional constant energy shift. This shift does not change the form of the electronic wave function; the only contribution is a shift of the total energy of the system according to Eq. (2.12). The Born-Oppenheimer approximation effectively separates the electronic motion from the motion of the nuclei, and by doing so limits the complexity of the problem.

## 2.2 Bloch electrons

In a perfect crystal the ions are positioned in a periodic crystal lattice. The potential  $V(\mathbf{r})$  then has the periodicity of the lattice

$$V(\mathbf{r} + \mathbf{R}) = V(\mathbf{r}), \quad (2.13)$$

for all translational lattice vectors  $\mathbf{R}$ . Assume for the moment that the electrons in the system are non-interacting and moving in a potential in the form of Eq. (2.13). Bloch's theorem then states that the wave function  $\psi$  of the one-electron Hamiltonian  $H = -\hbar^2 \nabla^2 / 2m + V(\mathbf{r})$  can be chosen to have the form of a plane wave times a function with the periodicity of the crystal [4]:

$$\psi_{n\mathbf{k}}(\mathbf{r}) = e^{i\mathbf{k}\cdot\mathbf{r}} u_{n\mathbf{k}}(\mathbf{r}), \quad (2.14)$$

where

$$u_{n\mathbf{k}}(\mathbf{r} + \mathbf{R}) = u_{n\mathbf{k}}(\mathbf{r}). \quad (2.15)$$

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<sup>3</sup>In what follows, the subscripts in Eq. (2.11) will be neglected if there is no possibility of confusion.

The periodic functions  $u_{n\mathbf{k}}(\mathbf{r})$  can be expanded using a basis set of plane waves whose wave vectors are reciprocal lattice vectors of the crystal:

$$u_{n\mathbf{k}}(\mathbf{r}) = \sum_{\mathbf{G}} c_{n\mathbf{k},\mathbf{G}} e^{i\mathbf{G}\cdot\mathbf{r}}, \quad (2.16)$$

where the  $\mathbf{G}$ 's are defined by  $\mathbf{G} \cdot \mathbf{R} = 2\pi m$ , where  $m$  is an integer. Each electronic wave function can then be written as a sum of plane waves:

$$\psi_{n\mathbf{k}}(\mathbf{r}) = \sum_{\mathbf{G}} c_{n,\mathbf{k}+\mathbf{G}} e^{i(\mathbf{k}+\mathbf{G})\cdot\mathbf{r}}. \quad (2.17)$$

The Bloch theorem with the periodicity of  $H$  and  $V(\mathbf{r})$  greatly reduces the number of particles that have to be included in the evaluation of the wave function since it is now only necessary to solve the Schrödinger equation within the primitive unit cell.

## 2.3 Chemical bonding and forces between atoms

In solid state systems there are essentially four different types of chemical bonds: ionic, metallic, covalent and van der Waals (vdW) bonds, each with different characteristics. The ionic bond is characterized by an electron transfer from one atomic species to another, as in the case of salts, while the metallic bond is characterized by a more or less homogeneous distribution of electrons in space. The covalent bond in turn is characterized as the sharing of electrons between atoms. Most materials display a bonding character that is a mixture of all these different bonding types, to a varying degree. The bonding of the transition metal carbides as an example, which will be further discussed in Part II, shows a combination of covalent, ionic and metallic bonding, which is the reason for their interesting physical properties. The vdW bond, on the other hand, is much weaker than the other three types and in many system it is completely negligible, however, there are some famous cases where it is extremely important. One example of such a system is graphite where the vdW bond is solely responsible for the interlayer bonding between the graphite planes.

In order to find the most stable atomic configuration for a specific combination of atoms, it is necessary to calculate how much energy that can be gained by forming the crystal or molecule from individual atoms. This energy is the cohesive energy or the energy of formation. The stable ground state situation is found for the arrangement of atoms that gives the lowest energy of formation.

From a knowledge of the energy of a system for a specific atomic configuration it is possible to calculate the forces acting between all of the atoms by using the Hellmann-Feynman theorem [5, 6]. This theorem states that the





















homogeneous electron gas with the same density, i.e.

$$E_{xc}[n^\uparrow, n^\downarrow] = \int n(\mathbf{r}) \varepsilon_{xc}^{hom}(n^\uparrow(\mathbf{r}), n^\downarrow(\mathbf{r})) d\mathbf{r}, \quad (3.17)$$

where  $\varepsilon_{xc}^{hom}(n^\uparrow(\mathbf{r}), n^\downarrow(\mathbf{r}))$  is the exchange-correlation energy per particle in a homogeneous electron gas with density  $n^\sigma(\mathbf{r})$ . The LDA works very well for being such a simple approximation. The reason for this is that many solids may be considered close to the limit of the homogeneous electron gas. When the electron density no longer may be considered to be homogeneous the LDA is expected to be less useful and it is necessary to use more advanced functionals.

In the so called generalized-gradient approximations (GGAs) the LDA is taken a step further and functionals are introduced that not only depend on the density at a point but also the magnitude of the gradient of the density at a point  $|\nabla n^\sigma|$ . The exchange-correlation energy functional can in this case be written as

$$E_{xc}^{GGA}[n^\uparrow, n^\downarrow] = \int n(\mathbf{r}) \varepsilon_{xc}(n^\uparrow(\mathbf{r}), n^\downarrow(\mathbf{r}), |\nabla n^\uparrow(\mathbf{r})|, |\nabla n^\downarrow(\mathbf{r})|) d\mathbf{r}. \quad (3.18)$$

There are many varieties of the GGA, among the most commonly used in actual calculations are the ones created by Becke (B88) [27], Perdew and Wang (PW91) [28], and by Perdew, Burke and Enzerhof (PBE) [29]. For many properties the GGA is an improvement over the LDA, bonds in molecules are more accurately described by the GGA than with the LDA for example.

There are also other improvements to the exchange-correlation functional that can be made [21] to improve on the accuracy of the Kohn-Sham method, however in the calculations performed in this thesis only the LDA and the GGA approaches have been used.



## 4. Plane waves, pseudopotentials and PAW's

The Kohn-Sham equation, Eq. (3.11), presented in the previous chapter is a Schrödinger-like equation, describing a single electron moving in an effective potential:

$$\left[ -\frac{\hbar^2}{2m_e} \nabla^2 + V_{eff}(\mathbf{r}) \right] \phi_i(\mathbf{r}) = \varepsilon_i \phi_i(\mathbf{r}). \quad (4.1)$$

In solid state physics there are mainly two different approaches towards solving the above equation; Hamiltonian methods that rely on a direct diagonalization of the Hamiltonian and Green's function based methods. The Hamiltonian methods utilize an expansion of the orbitals  $\phi_i$  into some kind of basis functions according to

$$\phi_i = \sum_k c_k^{(i)} \xi_k, \quad (4.2)$$

where  $\xi_k$  is some type of basis function and the  $c_k^{(i)}$  are expansion coefficients. The expansion can be performed in many different ways, for example it is possible to use plane waves as a basis in all of space, or one can use augmented methods where space is divided into regions and different kinds of functions are used as basis in the various regions. The difference in the way the expansion is performed has given rise to many different methods that are used regularly in electronic structure calculations, such as plane wave pseudopotential methods, augmented plane wave methods, as well as the muffin-tin based methods. The Green's function based methods on the other hand rely on single-particle Green's functions which describe the propagation of electrons from different points in space. The different methods have their advantages and disadvantages. In this chapter the focus is on the way Eq. (4.1) is solved when the expansion in Eq. (4.2) is in terms of plane waves.

If the system of interest is a crystal it is known from the Bloch theorem discussed in Chapter 2 that the wave functions may be described by a plane wave multiplied by a function with the periodicity of the lattice. Plane waves of the form  $e^{i\mathbf{q}\cdot\mathbf{r}}$  may be used to effectively describe the periodic function and the Kohn-Sham orbitals may then be expanded in the form

$$\phi_{n\mathbf{k}}(\mathbf{r}) = \sum_{\mathbf{G}} c_{n,\mathbf{k}+\mathbf{G}} e^{i(\mathbf{k}+\mathbf{G})\cdot\mathbf{r}}, \quad (4.3)$$

where  $\mathbf{G}$  is a reciprocal lattice vector and the  $c_{n,\mathbf{k}}$ 's are plane wave coefficients that remain to be determined. The Kohn-Sham equation expressed in terms of a plane wave basis then has the form

$$\sum_{\mathbf{G}'} \left[ \frac{\hbar^2}{2m_e} |\mathbf{k} + \mathbf{G}|^2 \delta_{\mathbf{G}\mathbf{G}'} + V_{eff}(\mathbf{G} - \mathbf{G}') \right] c_{n,\mathbf{k}+\mathbf{G}'} = \epsilon_n c_{n,\mathbf{k}+\mathbf{G}}. \quad (4.4)$$

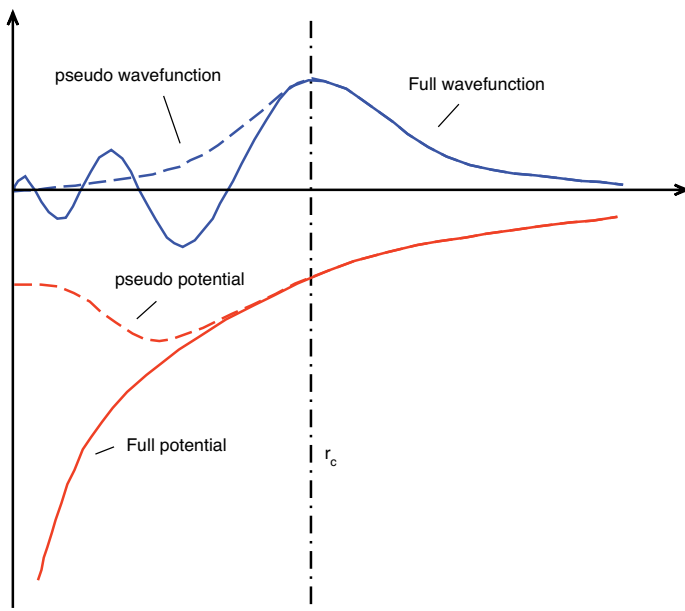
In principle, an infinite number of plane waves need to be involved in the solution of the above equation. However, the plane wave coefficients  $c_{n,\mathbf{k}+\mathbf{G}}$  with small kinetic energy,  $(\hbar^2/2m_e)|\mathbf{k} + \mathbf{G}|^2$ , are more important than those with high kinetic energy. It is therefore possible to expand the wave functions in a finite basis by only considering those plane waves with a kinetic energy below a specified cut-off energy. This cut-off introduces an error in the calculation, but this error can be controlled by checking the convergence of the total energy with respect to increased basis size [10].

The expansion of the wave function in terms of plane waves has a number of advantages, e.g. a plane wave expansion is a conceptually easy basis set, it is relatively easy to implement in a computer code, fast Fourier transforms between real and reciprocal space may be used and the kinetic energy operator has a nice diagonal form. However, there is a serious problem when trying to describe the wave functions in the core region of atoms, since the wave functions in this region is rapidly varying. It is therefore necessary to include a large number of plane waves in the basis to accurately describe the wave function in this region.

## 4.1 Pseudopotentials

A fact of nature is that most physical properties of solids, bonding for example, depend on the valence electrons to a much greater extent than on the electrons in the core. The pseudopotential approximation makes use of this fact by replacing the strong ionic potential by a weaker pseudopotential that acts on pseudo wave functions instead of on the true wave functions. The concept behind the pseudopotential is illustrated in Fig. 4.1. The valence wave functions oscillate rapidly in the region close to the core. These oscillations occur since the valence wave functions must be orthogonal to the core wave functions, because of the exclusion principle. The pseudo wave functions are then constructed in such a way that they have identical scattering properties off the ions and core electrons as the valence wave functions, but also so that they have no radial nodes in the core region [21, 10], see Fig. 4.1.

Pseudopotentials have been used for a long time in electronic structure calculations. In order to have a good pseudopotential it is necessary for the potential to be transferable, so that the same potential may be applied to different problems. Norm-conserving pseudopotentials are examples of potentials that



*Figure 4.1:* Illustration of the concept behind the pseudopotential. The pseudo wave function coincides with the true or full valence wave function at the cut-off radius  $r_c$  and beyond. Similarly, for the pseudopotential.

not only have the property that the all-electron and pseudo wave function coincide beyond the cut-off radius but also that the integrated charge inside  $r_c$  is identical. These norm-conserving potentials are both accurate and transferable.

One aim when constructing pseudopotentials is to make the potential as smooth as possible, meaning that the potential is constructed so that the plane wave basis set that has to be used is as small as possible. The norm-conserving potentials are accurate but the size of the basis set is still required to be large leading to large computational costs. By using so-called ultrasoft (US) pseudopotentials [30, 31] it is possible to perform accurate calculations while having a smooth potential. The concept behind this approach is to divide the problem into two parts; one smooth function and another auxiliary function around each ion core that represents the rapidly varying part of the density. In the next section another method will be described that can be adapted into the pseudopotential concept which increases the accuracy beyond both the norm-conserving and US pseudopotentials, namely the projector augmented wave method.

## 4.2 Projector augmented waves

The projector augmented wave (PAW) method, due to Blöchl [32], is another general method to solve the electronic structure problem. By combining the properties of the augmented plane wave (APW) method and the pseudopotential method it is possible to have access to the full wave functions, which is impossible in the pseudopotential method, while maintaining a limited size of the basis set.

The strategy of APW methods is to divide the wave functions into two parts: a partial wave expansion within an atom centered sphere and envelope functions outside the spheres. The envelope functions are then expanded into plane waves or some other basis set. Partial wave expansion and envelope functions are then matched at the sphere radius. The PAW method, however, utilizes a transformation of the valence wave functions onto fictitious pseudo wave functions according to

$$|\phi\rangle = \mathcal{T}|\tilde{\phi}\rangle, \quad (4.5)$$

where  $|\phi\rangle$  is the true all-electron (AE) valence wave function and  $|\tilde{\phi}\rangle$  the pseudo (PS) wave function. By knowing the transformation from the PS wave functions to the AE wave functions, it is possible to evaluate expectation values  $\langle\hat{A}\rangle$  for an operator  $\hat{A}$  in terms of the PS wave functions instead of the AE wave functions. Especially, it is possible to evaluate the total energy as a function of the PS wave functions and end up with a Kohn-Sham equation for the PS wave functions according to

$$\mathcal{T}^\dagger \hat{H} \mathcal{T} |\tilde{\phi}\rangle = \varepsilon \mathcal{T}^\dagger \mathcal{T} |\tilde{\phi}\rangle. \quad (4.6)$$

The transformation  $\mathcal{T}$  is defined to differ from identity only by a sum of local atom-centered contributions:

$$\mathcal{T} = \mathbf{1} + \sum_{\mathbf{R}} \hat{\mathcal{T}}_{\mathbf{R}}, \quad (4.7)$$

where each local contribution  $\hat{\mathcal{T}}_{\mathbf{R}}$  acts only within an augmentation region  $\Omega_{\mathbf{R}}$  enclosing the atom at  $\mathbf{R}$ . This implies that the PS and AE wave functions coincide outside the augmentation region. The local operators  $\hat{\mathcal{T}}_{\mathbf{R}}$  are defined for each augmentation region by specifying a set of target functions  $|\phi_i\rangle$  for the transformation  $\mathcal{T}$  for a set of initial functions  $|\tilde{\phi}_i\rangle$  that are orthogonal to the core states and complete within the augmentation region. We call these functions, following Blöchl's terminology [32], AE and PS partial waves respectively. The relation between them is

$$|\phi_i\rangle = (\mathbf{1} + \hat{\mathcal{T}}_{\mathbf{R}}) |\tilde{\phi}_i\rangle \quad (4.8)$$

within  $\Omega_{\mathbf{R}}$ . The next step is to express the PS wave function as

$$|\tilde{\phi}\rangle = \sum_i |\tilde{\phi}_i\rangle c_i \quad (4.9)$$

within  $\Omega_{\mathbf{R}}$ . So the PS wave function inside the augmentation region is a sum of PS partial waves multiplying constants  $c_i$ . The corresponding AE wave functions can also be expressed, within  $\Omega_{\mathbf{R}}$ , as

$$|\phi\rangle = \mathcal{T}|\tilde{\phi}\rangle = \sum_i |\phi_i\rangle c_i. \quad (4.10)$$

The coefficients  $c_i$  are scalar products and can be written as

$$c_i = \langle \tilde{p}_i | \tilde{\phi} \rangle, \quad (4.11)$$

with  $\langle \tilde{p}_i |$  being projector functions, one for each partial wave and fulfilling the condition  $\sum_i |\tilde{\phi}_i\rangle \langle \tilde{p}_i| = 1$  within  $\Omega_{\mathbf{R}}$ . This implies that the expansion  $\sum_i |\tilde{\phi}_i\rangle \langle \tilde{p}_i| \tilde{\phi}\rangle$  is identical to  $|\tilde{\phi}\rangle$  itself and in turn that  $\langle \tilde{p}_i | \tilde{\phi}_j \rangle = \delta_{ij}$  within the same augmentation region. The linear transformation  $\mathcal{T}$  may therefore be written as

$$\mathcal{T} = \mathbf{1} + \sum_i (|\phi_i\rangle - |\tilde{\phi}_i\rangle) \langle \tilde{p}_i|, \quad (4.12)$$

and accordingly the AE wave functions is expressed as

$$|\phi\rangle = |\tilde{\phi}\rangle + \sum_i (|\phi_i\rangle - |\tilde{\phi}_i\rangle) \langle \tilde{p}_i | \tilde{\phi} \rangle. \quad (4.13)$$

Any operator  $\hat{A}$  can now be transformed to act on the smooth PS wave functions according to

$$\tilde{A} = \mathcal{T}^\dagger \hat{A} \mathcal{T} = \hat{A} + \sum_{i,j} |\tilde{p}_i\rangle (\langle \phi_i | \hat{A} | \phi_j \rangle - \langle \tilde{\phi}_i | \hat{A} | \tilde{\phi}_j \rangle) \langle \tilde{p}_j|. \quad (4.14)$$

By using Eq. (4.14) it is possible to write the the total density at a point  $\mathbf{r}$  as

$$n(\mathbf{r}) = \tilde{n}(\mathbf{r}) + n_1(\mathbf{r}) + \tilde{n}_1(\mathbf{r}), \quad (4.15)$$

where the first term is a smooth part arising from the density of PS wave functions, while the last two terms are one-center terms that depend on the AE and PS partial waves respectively, within each augmentation region. A similar decomposition can also be done for the total energy. By effectively separating the problem into different parts, the PAW method allows for an efficient treatment of separated problems, while at the same time it offers the possibility for implementation of the PAW method in plane wave pseudopotential codes. By using plane waves for a basis the PAW method has become a very useful method, with the ability of performing accurate calculations with a limited basis set size [33].





Part II:

Transition metal carbides and multilayers

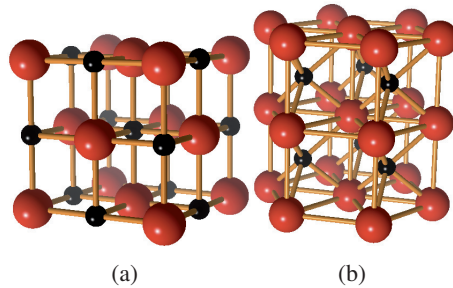


## 5. Transition metal carbides

The transition metal carbides (TMC) are materials that have attracted large interest, due to their combination of many interesting physical properties. This combination of physical properties has given these materials many different forms of industrial applications, for example as hard metal coatings on various machine components. In this chapter some general properties of TMC will be presented along with a summary of the results presented in Papers I to VII.

### 5.1 General properties of transition metal carbides

The TMC that will be the focus of this chapter are known as interstitial carbides, meaning that the crystal structure is built up by a metallic lattice, where the carbon atoms occupy the interstitial positions of the lattice. Since there are many different types of crystal structures that metal atoms can form, there are naturally many different forms of carbide structures. In Figure 5.1 there are illustrations of TMC in the B1 (or NaCl) and B<sub>h</sub> (or WC) structures. These



*Figure 5.1:* Illustration of the crystal structure of metal carbides in the B1 (a) and B<sub>h</sub> (b) structures. Metal atoms is represented by the red spheres and carbon atoms by black spheres.

materials are known for their many interesting physical properties, such as high hardness and high melting temperatures. In fact, some of the melting temperatures are among the highest ever measured [34]. The TMC also possess high electrical and thermal conductivities. A striking feature of these carbides is their defect structure. Ideal stoichiometry is almost never found and

|   |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    |  |  |  |  |  |  |  |  |  |  |  |
|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|--|--|--|--|--|--|--|--|--|--|--|
|   | 1  |    |    |    |    |    |    |    |    |    |    |    |    |    |    |    | 18 |    |    |    |    |  |  |  |  |  |  |  |  |  |  |  |
| 1 | H  |    | 2  |    |    |    |    |    |    |    |    |    |    |    | 13 |    | 14 | 15 | 16 | 17 | He |  |  |  |  |  |  |  |  |  |  |  |
| 2 | Li | Be |    |    |    |    |    |    |    |    |    |    |    |    | B  | C  | N  | O  | F  | Ne |    |  |  |  |  |  |  |  |  |  |  |  |
| 3 | Na | Mg | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | Al | Si | P  | S  | Cl | Ar |    |    |    |  |  |  |  |  |  |  |  |  |  |  |
| 4 | K  | Ca | Sc | Ti | V  | Cr | Mn | Fe | Co | Ni | Cu | Zn | Ga | Ge | As | Se | Br | Kr |    |    |    |  |  |  |  |  |  |  |  |  |  |  |
| 5 | Rb | Sr | Y  | Zr | Nb | Mo | Tc | Ru | Rh | Pd | Ag | Cd | In | Sn | Sb | Te | I  | Xe |    |    |    |  |  |  |  |  |  |  |  |  |  |  |
| 6 | Cs | Ba | La | Hf | Ta | W  | Re | Os | Ir | Pt | Au | Hg | Tl | Pb | Bi | Po | At | Rn |    |    |    |  |  |  |  |  |  |  |  |  |  |  |

Figure 5.2: Illustration of the Periodic Table with the transition metal elements that are involved in carbide formation is highlighted. The elements with orange coloring are strong carbide formers, while the elements with yellow coloring form metastable carbides [38, 39, 40].

the carbide phases exist over a broad range of compositions,  $\text{TiC}_{1-y}$  for example is stable for carbon vacancy concentrations,  $y$ , ranging from about 0.05 to 0.45. The reason for the combination of different properties is closely related to the chemical bonding in the carbides, which display a combination of covalent, metallic and ionic flavors to a varying degree [34, 35, 36, 37]. The most prominent bonding in these systems is however, the covalent bonds that are formed between metal d- and carbon p-electrons.

Carbide formation is quite common among the transition metal elements, which is illustrated in Fig. 5.2. The early transition metals in group 3 to 6 of the Periodic Table are strong carbide formers and form thermodynamically stable carbides with various crystal structure and stoichiometry. The late transition metals in group 8 to 10 form metastable carbides and are therefore known to be weak carbide formers [34, 38, 39, 40].

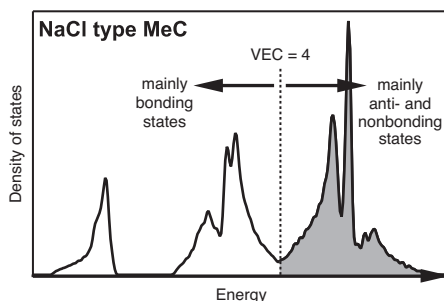


Figure 5.3: Illustration of the density of states of TMC in the B1 or NaCl crystal structure. The Fermi level of  $\text{TiC}$  is given by the vertical dotted line. The valence electron concentration (VEC) is here given per atom.

Since the structure of TMC consist of binary lattices, the formation of a carbide involves an expansion of the metal lattice in order to make room for the carbon atoms. Fortunately, when the carbon atoms are in place bonds between metal and carbon atoms are created that make up for the loss in energy due to the expansion of the metal lattice [41, 42, 43, 44, 45]. By restricting the discussion to TMC in the B1 or rock salt crystal structure, the stability of the TMC varies throughout the transition metal (TM) series. The most stable carbides are found for TM in group 4; Ti, Zr and Hf. The reason for this is illustrated in Fig. 5.3 for the case of the 3d TM. Generally, the electronic structure of these carbides display a rigid band behavior when varying the TM in the carbide. The density of states (DOS) shown in Fig. 5.3 has been calculated for TiC. With 4 valence electrons per atom contributing to the bonding, the Fermi level of TiC is positioned in a valley in the DOS that separates bonding states from anti- and non-bonding states [42, 45, 46]. The TMC in this group are therefore maximally bonded and by increasing or decreasing the number of electrons the carbide will become less stable due to the occupation of anti-bonding states or because of the lower occupation of bonding states. Another interesting fact concerning the bonding in the TMC is that carbides in the rock salt structure become dynamically unstable if the valence electron concentration is larger than 9, whereupon a phase transition should occur [47, 48]. In what follows, the fact that the TM have a varying tendency for carbide formation will be used to see how the stability changes when stable monocarbides are alloyed with elements that have a weak carbide forming ability.

## 5.2 Alloying of carbides and carbon release

As mentioned in the previous section, the TMC are known to be chemically stable compounds. However, the ability to form stable carbides varies throughout the Periodic Table. While some elements are good carbide formers, such as Ti and W, other elements such as Ni, Cu or Al do not form any stable forms of carbides, at least not when considering the traditional carbide compounds. In Figure 5.4 the calculated formation energy of  $Ti_{1-x}M_xC$  in the rock salt structure is shown, where M is any of the 3d transition metal atoms. The energy of formation has been calculated according to

$$E_{Form} = E(Ti_{1-x}M_xC) - (1-x) \cdot E(Ti) - x \cdot E(M) - E(C).^1 \quad (5.1)$$

It is clear that the formation energy increases as a function of the alloying. A negative formation energy signifies a stable ternary solution while a positive value in this case means that the alloyed carbides will decompose into more stable phases. Also shown in Fig. 5.4 is the calculated energy for carbon to be

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<sup>1</sup>Here and throughout the remaining parts of the thesis  $E(X)$  means the total energy of the compound or element X.

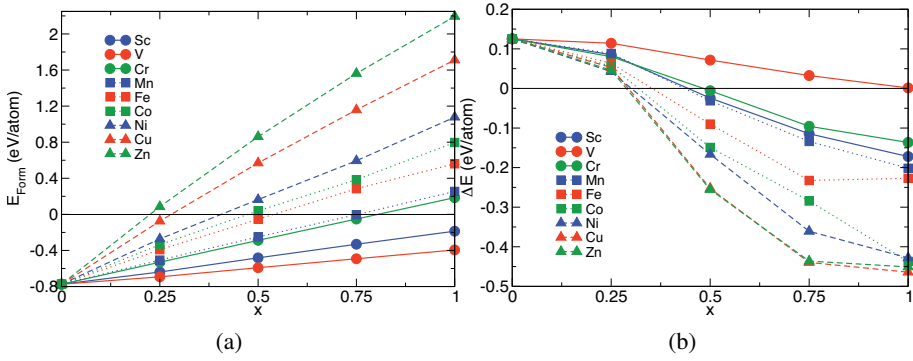


Figure 5.4: The calculated formation energy of alloyed  $\text{Ti}_{1-x}\text{M}_x\text{C}$  for alloying TiC with other metals from the 3d transition metal series as a function of the alloying component  $x$  (a) and the calculated energy difference for carbon segregation defined by Eq. (5.2) (b). From Paper I.

released from the carbide, calculated according to

$$\Delta E = E(\text{Ti}_{1-x}\text{M}_x\text{C}_{1-y}) + y \cdot E(\text{C}) - E(\text{Ti}_{1-x}\text{M}_x\text{C}), \quad (5.2)$$

where the reference state for carbon is graphite. Negative values mean that carbon will be released from the carbide and it is clear that carbon release correlates with the increased formation energy of  $\text{Ti}_{1-x}\text{M}_x\text{C}$ .

In Figure 5.5 experimental results obtained by X-ray diffraction (XRD) and X-ray photoelectron spectroscopy (XPS) is given for the case of TiC alloyed with Ni. The XRD results show that Ni is dissolved in the carbide on the Ti lattice and that no segregation of Ni is apparent. Furthermore, results from the XPS show that as a response of the alloying there is an increased amount of C-C bonds in the alloyed samples, suggesting that carbon has been released. This is visible for both as deposited samples and as a response to annealing. For further discussions on this see Paper I.

The results presented here and in Paper I show that there is a driving force for the release of carbon from alloyed  $\text{Ti}_{1-x}\text{M}_x\text{C}$ , the strength of which depends on the composition and which element has been used as the alloying component. This release of carbon may be utilized to obtain new functionality of the TMC. This was investigated in Paper VII. Here the alloying component was Al and it was found from both theoretical calculations and from experimental measurements that carbon was released from the carbide. It was also shown that the friction coefficient of these systems is lowered in the alloyed samples than when compared to samples which contained no Al. These materials may therefore be used as hard and durable coating materials, which also possess an inherent drive for self-lubrication upon external pressures and

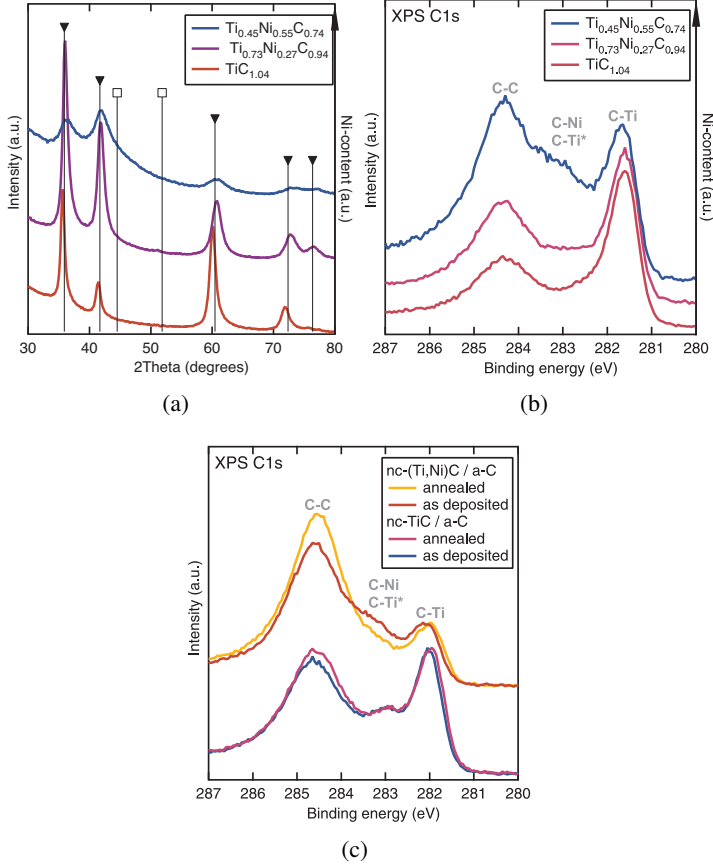
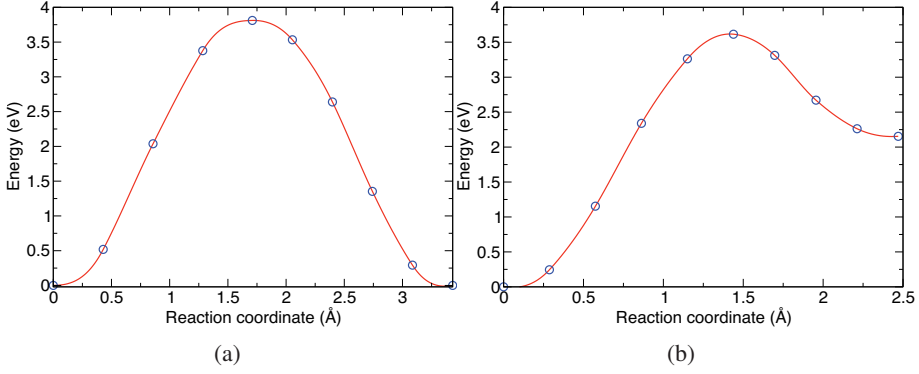


Figure 5.5: X-ray diffraction data (a), and X-ray photoelectron spectra of as-deposited (b) and annealed (c) samples of  $\text{Ti}_{1-x}\text{Ni}_x\text{C}_{1-y}$ . From Paper I.

elevated temperatures. A general review of the experimental and theoretical situation of ternary thin films of TMC is given in Paper V.

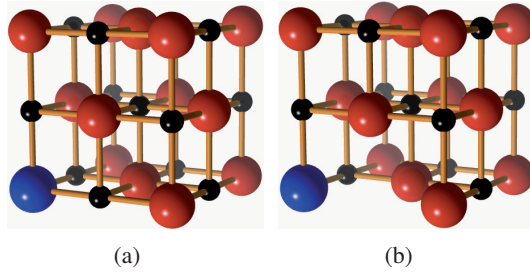
### 5.3 Stability and mobility of defects

The ability for TMC to release carbon is not solely depending on the driving force for carbon release. The carbon atoms must also be mobile, which means that it must be possible for them to move. In Figure 5.6 the activation energy barriers for C vacancy mediated diffusion and for a C atom to move from a octahedral to a tetrahedral site is given for a supercell of TiC. These barriers have been calculated using the nudged elastic band technique [49, 50, 51, 52], which is ideal for calculations of energy barriers since the method maps out



*Figure 5.6:* Calculated activation energy barrier for carbon vacancy mediated diffusion (a) and the energy required to move a C atom from an octahedral to a tetrahedral position (b) in TiC.

the minimum energy path between an initial and a final geometry. The barriers in Fig. 5.6 are in good agreement with experimental findings [38]. However, the experimental situation is complex due to the varying stoichiometry of TiC. What can be concluded is however, that the energy required for C diffusion to be activated is high, which means that the carbides must be heated to high temperatures in order for carbon to diffuse in the crystal. It is therefore interesting to see how the carbon diffusion processes changes when a smaller or larger amount of foreign elements are introduced in a binary carbide, especially when regarding carbon release from alloyed TMC which was discussed in the previous section.



*Figure 5.7:* TiC in the B1 crystal structure with the defects considered in Paper II. Figure (a) shows the case of a single substitutional 3d TM impurity (blue) while Figure (b) depicts the situation when a C vacancy is present at the nearest neighbor C position to the TM impurity. Ti and C are illustrated by the red and black spheres respectively.



Table 5.1: *Calculated defect formation energies obtained using Eqs. (5.3) and (5.4) for single metal substitutions and carbon vacancies in TiC. Note that there is no substitutional defect in the case of Ti. The activation energy,  $E_A$  is given for C vacancy driven diffusion. Also shown are the lattice parameters of the binary 3d TM carbides in the B1 structure,  $a_{B1}$ .*

| Element | $a_{B1}$ (Å) | $E_s$ (eV) | $E_v$ (eV) | $E_A$ (eV) |
|---------|--------------|------------|------------|------------|
| Sc      | 4.68         | 1.08       | 0.33       | 4.71       |
| Ti      | 4.34         | n.a.       | 0.61       | 3.81       |
| V       | 4.15         | 0.74       | 0.46       | 3.01       |
| Cr      | 4.07         | 2.25       | 0.04       | 2.47       |
| Fe      | 3.99         | 3.76       | -0.38      | 2.05       |
| Co      | 4.01         | 4.10       | -0.40      | 2.20       |
| Ni      | 4.08         | 4.65       | -0.54      | 2.45       |
| Cu      | 4.24         | 5.95       | -0.71      | 2.68       |
| Zn      | 4.40         | 7.08       | -0.83      | 2.98       |

In Paper II we report on the stability of substitutional 3d transition metal (TM) defects and their effect on the local surrounding in TiC, especially when regarding bonding to carbon. Furthermore, activation energy barriers for C diffusion was investigated. The main results are summarized in Table 5.1, where the energy of formation of a single 3d TM substitutional impurity,

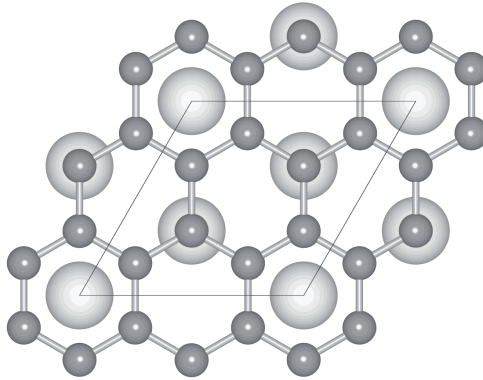
$$E_s = E(\text{TiC};\text{M}_s) - E(\text{TiC}) - (E(\text{M}) - E(\text{Ti})), \quad (5.3)$$

as well as the formation energy of carbon vacancies, in the vicinity of TM defects,

$$E_v = E(\text{TiC};\text{C}_v) - E(\text{TiC}) + E(\text{C}), \quad (5.4)$$

are shown, together with calculated lattice parameters of the different TMC in the B1 structure. Activation energy barriers for vacancy driven carbon diffusion in TiC is also shown in Table 5.1. These barriers are for the case of C vacancy driven diffusion in the presence of the TM impurities, i.e. a C atom positioned at the nearest neighbor C position to a TM impurity moves to a vacant C position at another nearest neighbor position to the TM impurity. For further details see Paper II. The different defects considered are illustrated in Fig. 5.7. It is seen in Table 5.1 that the energy required to form the substitutional TM defects,  $E_s$ , increases the further to the right of the Periodic Table the defect element is positioned. This energy is also very high, suggesting a very low solubility of these TM in TiC, which implies that alloyed solutions of  $\text{Ti}_{1-x}\text{M}_x\text{C}$ , discussed previously, are indeed metastable. Furthermore, the energy of formation of creating a C vacancy close to the TM impurity,  $E_v$ ,

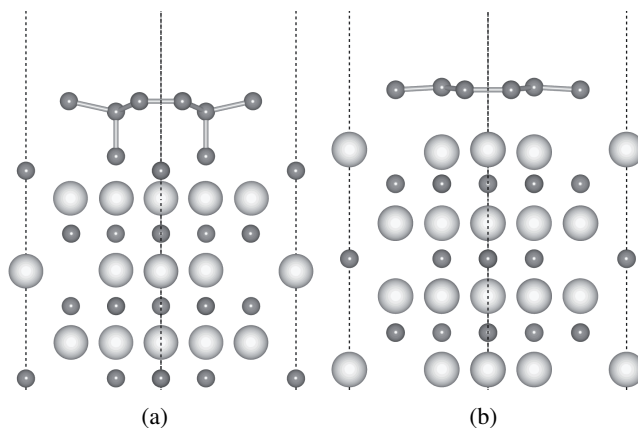
is lower in the vicinity of the impurity than in pure TiC, which means that the C atoms close to impurities are much more loosely bonded. In fact, as can be seen in Table 5.1, for Fe, Co, Ni, Cu and Zn the vacancy formation energy is negative which means that these vacancies will be formed spontaneously. These observations can be explained by different elements ability to form carbides. However, the activation energy barriers for vacancy mediated C diffusion do not decrease monotonously when changing the TM. The barriers are lower for the weak carbide formers than in pure TiC, however, the barrier in the presence of Sc is higher than in pure TiC and towards the end of the series there is an increase of the height of the barrier. This behavior follows the behavior of the lattice parameters of the 3d TMC in the B1 crystal structure which is also shown in Table 5.1. Therefore the behavior of the activation energy barriers is attributed to both a decreased ability for the TM to form carbides as well as to an atomic size effect due to the correlation with the lattice parameters in the 3d TMC. Based on these results it is possible to conclude that the introduction of impurities in TiC affects the distribution of C vacancies, since the vacancies tend to be closer to the impurities, and that it also has an effect on the mobility of C atoms in the carbide. These results suggest that the ability for alloyed solutions of carbides to release carbon will set in at lower or higher temperatures depending on the alloying element.



*Figure 5.8:* The  $\sqrt{3} \times \sqrt{3}R30$  surface geometry of graphene/graphite on TiC(111) when the carbide surface is terminated by Ti. C atoms are represented by dark grey spheres and Ti atoms by light grey spheres.

## 5.4 Properties of carbide-carbon interfaces

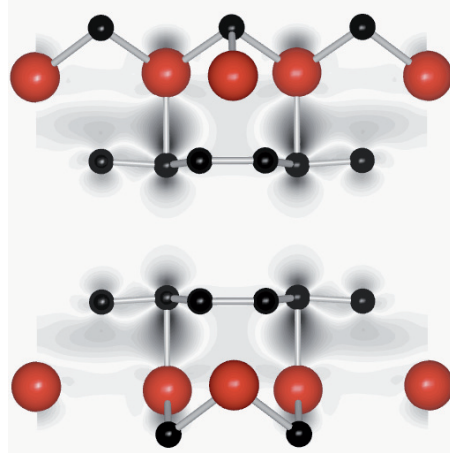
It is already established that the carbides have many favorable properties and have therefore been used in many applications. One such application is as coating materials. A widely studied carbide coating material is nanocompos-



*Figure 5.9:* Relaxed surface structure of the TiC(111) surface and monolayer of graphite when (a) the carbide surface is C terminated and (b) when the surface is Ti terminated. C atoms are represented by dark grey spheres and Ti atoms by light grey spheres. For more details see Paper III.

ites of carbide grains dispersed in an amorphous carbon matrix, nc-MC/a-C, where M can be any TM. Since these materials contain grains of carbides in a C matrix the interaction between the interfaces is an important issue to understand. In Paper III the interface properties of the TiC(111) surface and layers of graphene/graphite were investigated. Graphene, a 2 dimensional allotrope of carbon has during recent years attracted great interest due to its special properties, which has spawned many investigations on how to make this material and how it interacts with other materials [53, 54]. The investigation in Paper III was therefore motivated by the recent interest in graphene and how it interacts with different surfaces and also to model the carbide grain and C matrix interface bonding in nc-TiC/a-C. The way graphene was placed on TiC(111) is shown in Fig. 5.8. Due to the crystal structure of TiC, the TiC(111) surface can be terminated in two different ways; either completely by C or completely by Ti. The termination of the carbide surface was found to influence the structural relaxations at the interface, which is shown in Fig. 5.9, as well as the chemical bonding between carbide and graphene. However, irrespective of the surface termination, the graphene layer directly on top of the surface was found to have a metallic density of states at the Fermi level. The same results were obtained in the model calculations on TiC grains in a C matrix, where layers of graphene were sandwiched in between layers of TiC(111) surfaces.

Furthermore, by using Bader analysis [55, 56, 57, 58] it was established that a transfer of electrons from the carbide to the C atoms on the Ti terminated surface occurs. This is shown in Fig. 5.10 where the difference in the charge



*Figure 5.10:* Calculated interface structure of bi-layers of graphite sandwiched between two TiC(111) surfaces. Here Ti atoms are illustrated by the red spheres while C atoms is illustrated by black spheres. Also shown is a charge density difference plot along a plane that cuts right through the interface model. For details see Papers III and IV.

density is plotted for a plane that cuts the interface model perpendicular to the (111) surface. As can be seen in Fig. 5.10, there is an accumulation of charge between C atoms in the graphene/graphite and the Ti atoms of the carbide surface that has a larger weight on the C side. This electron transfer from the carbide will lead to carbide grains depleted in electrons. In Paper IV, the effects of this charge depletion was investigated and found to yield an increase of the lattice parameter of the carbide. The increase in the lattice parameter of electron deficient TiC nicely correlates with an experimental observation, that the lattice parameter of TiC grains in an amorphous C matrix increases when the size of the grains becomes smaller.

## 5.5 Magnetic properties of $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$

In Paper VI, we investigated the magnetic properties of thin films of  $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$  from both theory and experiment. Here the Kohn-Korringa-Rostoker (KKR) method [59, 60] in connection with the atomic sphere approximation (ASA) [61, 62] was used to solve the electronic structure problem. This is a Green's function based method which is perfectly adopted to be used together with the coherent potential approximation (CPA).

The magnetic moments, magnetic exchange parameters and electronic structure of completely random  $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$  were calculated while varying the Fe content  $x$  and the C vacancy concentration  $y$ . By using the magnetic

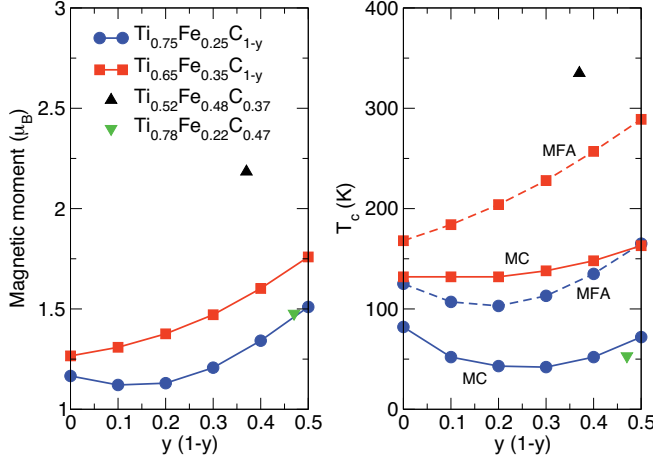


Figure 5.11: The calculated magnetic moment and transition temperatures for  $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$  for  $x = 0.25$  and  $0.35$  as a function of  $y$ . Also shown are the specific cases of  $(x, y) = (0.48, 0.63)$  and  $(x, y) = (0.22, 0.53)$ . For these specific points the data is given as a function of  $1 - y$ .

exchange parameters the critical temperatures of the system was obtained by means of both the mean field approximation (MFA) as well as by performing Monte Carlo simulations (MC). For more details see Paper VI. The results are given in Fig. 5.11. The general conclusion is that the magnetic properties (magnetic moments and critical temperature  $T_c$ ) increase when increasing the amount of Fe and when lowering the C content. Furthermore, it was found that the exchange parameters clearly reflect the changes in the chemical bonding in the system when lowering the C content. The exchange parameters for  $x = 0.35$  and different values for  $y$  are given in Fig. 5.12. Note that the behavior of the exchange parameters varies when changing the C content. For low C vacancy concentrations the nearest neighbor interaction is smaller than the second nearest neighbor interaction, while for large vacancy concentrations the nearest neighbor interaction is the largest. This behavior comes from the difference in the chemical bonding in these situations. The bonding in TiC is, which was discussed in Section 5.1, known to be primarily due to covalent bonds between Ti and C, however, when the number of vacancies on the carbon lattice increases the influence of the d-electron interaction between metal atoms will become more pronounced. It is this change in behavior that is reflected in Fig. 5.12.

The calculations of the magnetic properties of  $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$  were all performed for a system where Fe as well as C vacancies were randomly dispersed on each of the sublattices. However, as was pointed out in Section 5.2, these ternary carbide phases are highly metastable and possess a driving force for phase separation into more stable phases. After annealing,  $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$ -

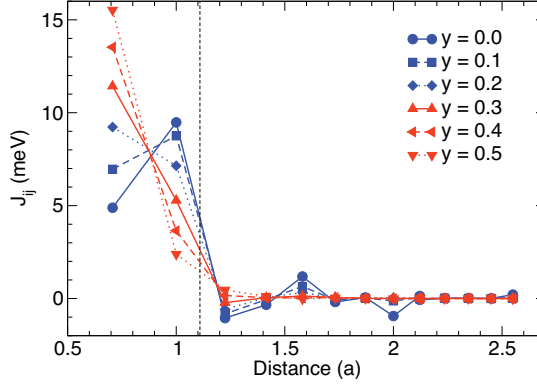


Figure 5.12: The calculated interatomic exchange parameters,  $J_{ij}$ , between Fe atoms in  $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$  for  $x = 0.35$  for different C vacancy concentrations,  $y$ , as a function of distance. Where the distance is given in terms of the lattice parameter of the crystal.

phases were found (see Paper VI) to phase separate into Fe-rich regions and TiC-rich regions as depicted in the tunnel electron microscopy (TEM) images in Fig. 5.13. The experimentally measured moments and critical temperatures were found to be rather substantial and to reflect the formation of Fe-rich phases upon annealing. The trend of phase separation into Fe-rich regions inside the carbide shown in Fig. 5.13 is an interesting avenue for the creation of magnetic tri- or multilayers that can be used as wear-resistant magnetic thin-film materials.

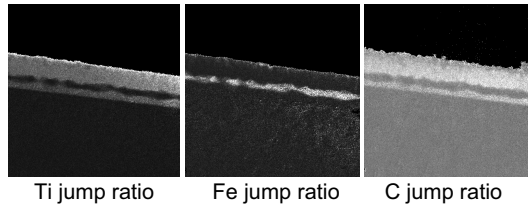
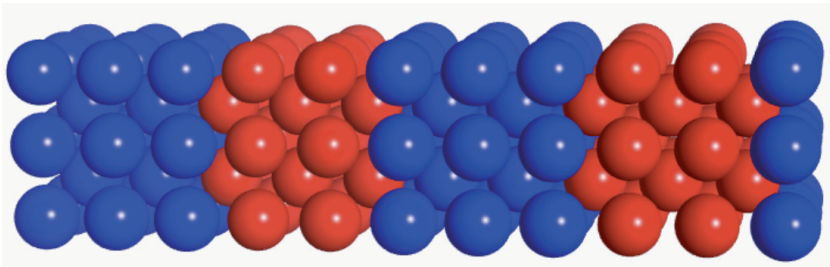


Figure 5.13: TEM images of a  $\text{Ti}_{1-x}\text{Fe}_x\text{C}_{1-y}$  film deposited on  $\text{MgO}(100)$  showing Ti-, Fe- and C-rich regions (brighter contrast indicate higher element concentration), signifying a phase separation into a Fe-rich phase and TiC.

## 6. Structure of multilayered materials

By growing materials, layer by layer, in a controlled fashion has opened a venue for new properties and functionality. Often atoms can be grown epitaxially, i.e. on top of each other, so that the same crystal structure is maintained as the interface between different materials is traversed. One of the most studied examples of such materials are the multilayer structured materials, which is illustrated in Fig. 6.1. In these multilayer structures it has been observed that the physical properties are coupled to the structural arrangement of the atoms in the multilayers.

From a theoretical perspective, the detailed geometry of multilayer structures is a very complicated problem to treat in a realistic fashion, since the number of atoms involved in any calculations of this type is necessarily large. For this reason, it is necessary to use simple methods to predict the structure of multilayers.



*Figure 6.1:* Illustration of a multilayered system where the multilayer components have the same thickness. Blue and red spheres represent different types of elements.

When performing first principles calculations on multilayers there are several approximations that are commonly used. One way is to assume that one subsystem in the multilayer completely dominates the other and that it is possible to use the same lattice parameter in the whole system. This approximation works the best when one of the sublayers is thin in comparison to the other. However, for multilayers with comparable thickness this approximation does not work as good. Another approximation is the use of Vegard's law, which is a phenomenological observation from alloyed systems, which states that the lattice parameter of an  $A_{1-x}B_x$  alloy is a linear combination of the lattice parameters of the two subsystems, i.e.  $a_{A_{1-x}B_x} = (1-x) \cdot a_A + x \cdot a_B$ . This

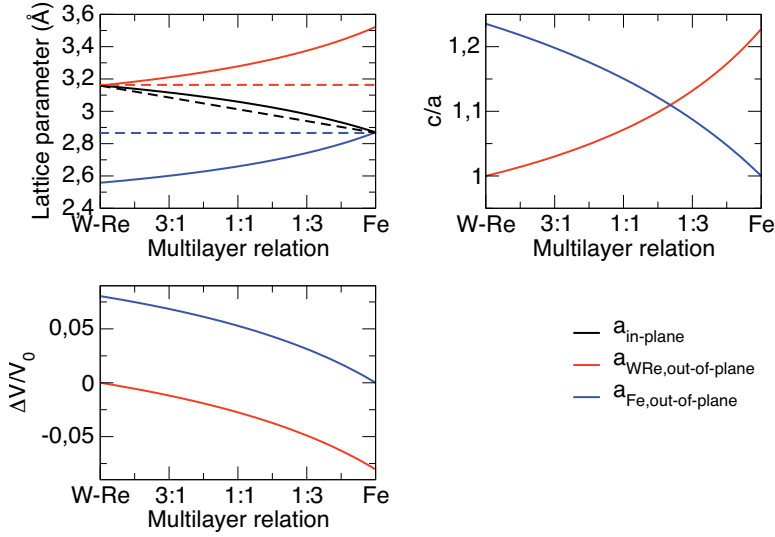


Figure 6.2: Calculated in- and out-of-plane lattice parameters of  $W_{0.8}Re_{0.2}/Fe$  multilayers,  $c/a$ -ratio and relative change in the volume in each sublayer as obtained by the elasticity model presented in Paper VIII.  $\Delta V$  is the difference in volume of a component in the multilayer compared to the single crystal bulk value  $V_0$ . On the x axis the relation between  $W_{0.8}Re_{0.2}$  and Fe is given.

approximation can give reliable results, however, the structure is still assumed to be the same throughout the multilayer, which may not be the case in the experimental situation.

In Paper VIII we have evaluated a model which is based on elasticity theory, which can in a more realistic fashion consider different structural relaxations within each subsystem of the multilayer. The model assumes perfect lattice matching at the interface between the different subsystems and that the elastic properties within each layer are the same in the multilayer as they are in the pure bulk crystals. This model gives more reliable structural parameters than the previously mentioned approximations and the structures generated by this model serves as a good starting point for the evaluation of physical properties of various kinds of multilayers. In Figure 6.2 results are shown for calculations using the elasticity model for multilayers consisting of Fe and a  $W_{0.8}Re_{0.2}$  alloy grown along the [100] direction of the body centered cubic lattice. The in-plane lattice parameter, defined as the lattice parameter parallel to the interface between the two multilayer components, is identical for the two components by construction and deviates from Vegard's law. The out-of-plane lattice parameters, defined as the lattice parameters in the directions perpendicular to the interface, are different in the two components which is impossible to obtain for a multilayer where only Vegard's law behavior is



assumed. Furthermore, the  $c/a$  ratio, which here is defined as the quotient between the largest and smallest value of the in- and out-of-plane lattice parameters, shows large deviations from unity depending on the relative amount of Fe and  $\text{W}_{0.8}\text{Re}_{0.2}$  components. This model is proposed to yield good structures for multilayers, upon which more accurate calculations can be based.



## 7. Conclusion and outlook

This thesis has been concerned with the application of theoretical methods to investigate properties related to chemical bonding and structure of materials. In essence two different types of materials have been investigated: transition metal carbides and multilayers. First principles density functional theory calculations have been used extensively to calculate properties of alloyed solutions of transition metal carbides where a stable monocarbide has been alloyed with metal atoms that by themselves possess a weak ability to form carbides. The alloying results in a metastable phase which allow for decomposition into more stable phases. For example, carbon has been shown to be released from the carbides as a response to the alloying. This carbon release was also found to yield lowered friction coefficients which extends the usefulness of the transition metal carbides when regarding industrial applications. To continue the study of these alloyed carbides it would be interesting to study the decomposition of these materials in more detail. Kinetic Monte Carlo simulations would be a perfect tool for such studies since by using this method it is possible to simulate growth processes as well as diffusion processes at any temperature in an efficient manner.

The principle of alloying transition metal carbides to increase the functionality of the carbide phases can also be used for other systems, such as the MAX phases or the transition metal nitrides. In those cases the aim will not be to make them release carbon but other properties could be affected due to the alloying, such as the hardness or the conductivity of the material.

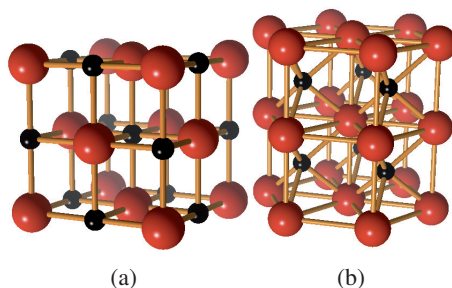
Interface properties of TiC and carbon were investigated between the TiC(111) surface and carbon in the form of graphene/graphite in order to model carbide grain to carbon matrix interactions in nc-TiC/a-C and to investigate the properties of graphene on TiC. The carbon was found to be strongly bonded to the carbide surface. Furthermore, the interface properties were discovered to depend on the termination of the carbide. The theoretical studies on the interface properties performed here are limited when it comes to the size of the system of interest and to simulate grains of carbides in a carbon matrix is impossible using modern implementations of density functional theory calculations. For this reason, it would be interesting to use for example molecular dynamics with classical force fields or a parametrized tight binding method to perform calculations for much larger systems with carbide grains dispersed in a carbon matrix.

For multilayered systems, a model based on elasticity theory has been investigated that in a simple fashion makes it possible to calculate reliable structural parameters. The model can be useful as a starting point for accurate first principles calculations and as an aid in the evaluation of experimental data. What remains to be done is to extend the model to general geometries. So far the model has been set up to be able to calculate the structural parameters for cubic multilayers. Many different geometries can be imagined however, and to extend the model to work for these geometries is a natural step.

## 8. Svensk sammanfattning

Vi lever i en värld som styrs av partiklar och deras interaktioner. Det finns elektroner, kvarkar, neutriner och alla andra partiklar som tillsammans utgör det stora utbudet av partiklar som beskrivs av standardmodellen. För vår vardag är de viktigaste partiklarna elektronerna. Tillsammans med protoner och neutroner, utgör elektronerna grunden för alla grundämnen i periodiska systemet. Det är elektronerna och deras samspel som avgör hur molekyler bildas av atomer och hur atomer kombineras för att bilda fasta ämnen. Inom materialfysiken är målet att kunna förstå egenskaper hos olika typer av material, från atomnivå till kondenserade former av materia som kristaller och vätskor.

I denna avhandling används teoretiska metoder som grundar sig på första principer för att besvara frågor angående kemisk bindning, struktur och stabilitet hos material som är av stort intresse, både från ett rent vetenskapligt och ur ett industriellt perspektiv. I stor utsträckning handlar denna avhandling om egenskaper hos metallkarbider. I Figur 8.1 finns en illustration av vanligt förekommande kristallstrukturer hos metallkarbider. Dessa material har un-



*Figure 8.1:* Illustration av kristallstrukturen hos metallkarbider i B1- eller NaCl-strukturen (a) och i B<sub>h</sub>- eller WC-strukturen (b). De röda sfärerna representerar metallatomer medan de svarta sfärerna representerar kolatomer.

der lång tid varit av intresse på grund av sina många intressanta fysikaliska egenskaper. På grund av deras kombination av intressanta egenskaper har de blivit använda i många olika tekniska tillämpningar. Ett exempel på en sådan tillämpning är som hårda metallytebeläggningar på olika komponenter. Materials ytor täcks ofta av olika ytbeläggningar för att skydda ytan och där igenom

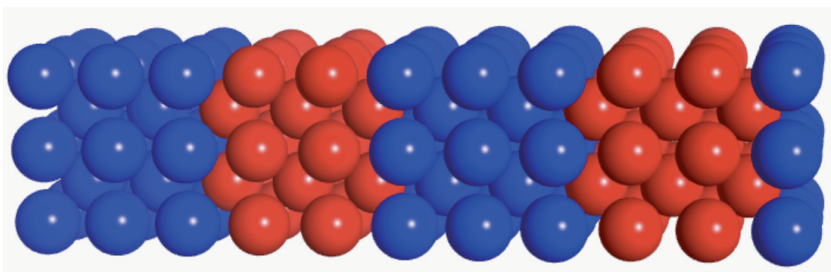


Figure 8.2: Illustration av ett multilagermaterial där olika atomer är markerade med olika färg.

förlängs livstiden för olika komponenter. Därför är det naturligt att mycket energi har lagts på att ta fram nya ytelägningsmaterial. Som en del i denna avhandling presenteras en strategi med vilken det är möjligt att framställa nya yteläggningar med utökade egenskaper.

En traditionell kristall är ett arrangemang av atomer i någon form av kristallstruktur. Detta är i princip en homogen ordning med identiska positioner i kristallen där atomer populerar de olika positionerna i strukturen. Numera är det praktisk möjligt att skapa nya typer av strukturer där atomerna arrangerats i ett specifikt mönster. Ett sådant material är så kallade multilagermaterial där olika typer av material arrangerats i olika, på varandra följande, lager. I Figur 8.2 finns en illustration av strukturen hos ett multilagermaterial. Det har visat sig att dessa typer av material har nya egenskaper och funktioner, ett exempel är upptäckten av den gigantiska magnetoresistanseffekten (GMR) för vilken Albert Fert och Peter Grünberg belönades med Nobelpriset i fysik 2007.

Teoretiska undersökningar har alltid spelat en avgörande roll för förståelsen av den fysiska världen. Syftet är här att få en beskrivning av alla partiklar och hur de samverkar genom att veta endast antalet partiklar och genom att basera beskrivningen på grundläggande naturlagar, dvs från första principer eller *ab initio*. För en kristall eller en vätska är det mycket komplicerat att teoretiskt modellera och beräkna olika fysiska egenskaper på ett sådant sätt. Detta beror på det stora antalet partiklar som utgör dessa mångpartikelsystem. För att komma vidare är det nödvändigt att utföra en serie approximationer och att konstruera bra modeller. I detta arbete har täthetsfunktionalteorin [1, 2], vilken utvecklades av Walter Kohn och hans medarbetare, använts för att beräkna olika materials egenskaper. Kärnan i täthetsfunktionalteorin är att omvandla problemet med många interagerande partiklar till ett effektivt enpartikelproblem som är mycket lättare att lösa. Olika implementationer av täthetsfunktionalteorin är idag bland de mest använda metoderna för att utföra beräkningar av elektronstrukturen hos olika material.

Denna avhandling är uppdelad i två delar. I del I presenteras vanligt förekommande teorier för kristaller vilka använts flitigt i denna avhandling. Denna del av avhandlingen är inte materialspecifik och diskussionen kan tillämpas på vilket material som helst. Del II är en sammanfattning av de forskningsresultat som presenteras i de medföljande forskningsrapporterna tillsammans med ytterliggare diskussion gällande egenskaper hos metallkarbider och multilagerstrukturer.





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